XE (B): Q. 1 – Q. 9 carry one mark each & Q. 10 – Q. 22 carry two marks each.

Q.1 Rheological diagram of different types of fluids is shown in figure. Column I represents the nature of the fluid and column II represents the curve showing the variation of shear stress against shear strain rate.



The most appropriate match between columns I and II is,

- (A) (i) O; (ii) N; (iii) P; (iv) M(B) (i) - O; (ii) - P; (iii) - N; (iv) - M(C) (i) - P; (ii) - O; (iii) - M; (iv) - N
- (D) (i) -P; (ii) -O; (iii) -N; (iv) -M

Q.2 In a two-dimensional, incompressible and irrotational flow, stream function ($\psi = \psi(x, y)$) and velocity potential ($\phi = \phi(x, y)$) exist. The velocities in x and y directions are non-zero.

The product of
$$\frac{dy}{dx}\Big|_{\phi=\text{constant}}$$
 and $\frac{dy}{dx}\Big|_{\psi=\text{constant}}$, is
(A) -1 (B) 0 (C) 1 (D) ∞

Q.3 The inviscid flow past a rotating circular cylinder can be generated by the superposition of

- (A) uniform flow, source and vortex (B) uniform flow, doublet (C) uniform flow, sink and vortex (D) uniform flow, doublet and vortex
- The velocity field and the surface normal vector are given by, $\vec{V} = u\hat{i} + v\hat{j} + w\hat{k}$ and Q.4 $\vec{n} = n_1 \hat{i} + n_2 \hat{j} + n_3 \hat{k}$, respectively. If Euler equations are to be solved, the boundary condition that must be satisfied at the wall is.

(A)
$$\vec{V} \cdot \vec{n} = 0$$
 (B) $\vec{V} = 0$ (C) $\nabla \cdot \vec{V} = 0$ (D) $\vec{V} \times \vec{n} = 0$

- The influence of Froude number is most significant in Q.5
 - (A) capillary flows (B) creeping flows
 - (C) free surface flows (D) compressible flows

Q.6 If the stream function $(\psi(x, y))$ for a two-dimensional incompressible flow field is given as $2y(x^2 - y^2)$, the corresponding velocity field is

(A) $\vec{V} = 2(x^2 - 3y^2)\hat{i} + 4xy\,\hat{j}$ (B) $\vec{V} = 2(x^2 - 3y^2)\hat{i} - 4xy\,\hat{j}$ (C) $\vec{V} = 2(x^2y)\hat{i} - 4xy\,\hat{j}$ (D) $\vec{V} = 2(x^2y)\hat{i} + 4xy\,\hat{j}$

Q.7 Water is flowing in two different tubes of diameters *D* and 2*D*, with the same velocity. The ratio of laminar friction factors for the larger diameter tube to the smaller diameter tube is

(A) 0.5 (B) 1.0 (C) 2.0 (D) 4.0

- Q.8 If the velocity field is $\vec{V} = xy^2 \hat{i} + 4xy \hat{j}$ m/s, vorticity of the fluid element in the field at (x=1, y=2) in s⁻¹ is _____.
- Q.9 A pitot-static tube is used to measure air velocity in a duct by neglecting losses. The density of air is 1.2 kg/m³. If the difference between the total and static pressures is 1 kPa, the velocity of air at the measuring location, in m/s, is _____.
- Q.10 A parallelepiped of $(2 \text{ m} \times 2 \text{ m})$ square cross-section and 10 m in length, is partially floating in water upto a depth of 1.2 m, with its longest side being horizontal. The specific gravity of the block is

(A) 0.8 (B) 0.6 (C) 0.5 (D) 0.4

- The velocity in a two-dimensional, unsteady Q.11 field flow is given by $\vec{V}(x, y, t) = 2xy^2 \hat{i} + 3xyt \hat{j}$ m/s. The magnitude of acceleration of a fluid particle located at x = 1 m, y = 1 m at the time t = 1 s, in m/s², is (A) 16.0 (B) 18.1 (C) 24.1 (D) 34.1
- Q.12 In a two-dimensional, incompressible and irrotational flow, fluid velocity (v) in the y
 - direction is given by v = 2x 5y. The velocity (*u*) in the x-direction is

(A) u = 2x - 5y (B) u = 2x + 5y (C) u = 5x + 2y (D) u = 5x - 2y

Q.13 A two-dimensional laminar viscous liquid film of constant thickness (*h*) steadily flows down an incline as shown in figure. Acceleration due to gravity is *g*. If the velocity profile in the liquid film is given as, u = ky(2h - y); v = 0, the value of constant *k* is



Q.14 A water jet of 100 mm diameter issuing out of a nozzle at a speed of 50 m/s strikes a vane and flows along it as shown in figure. The vane is attached to a cart which is moving at a constant speed of 20 m/s on a frictionless track. The jet is deflected at an angle of 30°. Take the density of water as 1000 kg/m³. Neglecting the friction between the vane and the fluid, the magnitude of the force exerted by water on the cart in the *x*-direction, in N, is _____.



Q.15 Capillary waves are generated in the sea. The speed of propagation (*C*) of these waves is known to be a function of density (ρ), wave length (λ), and surface tension (σ). Assume, ρ and λ to be constant. If the surface tension is doubled, in the functional form of the relevant non-dimensional group, the percentage increase in propagation speed (*C*) is _____.

- Q.16 Consider a fully developed, two-dimensional and steady flow of a viscous fluid between two fixed parallel plates separated by a distance of 30 mm. The dynamic viscosity of the fluid is 0.01 kg/m-s and the pressure drop per unit length is 300 Pa/m. The fluid velocity at a distance of 10 mm from the bottom plate, in m/s, is _____.
- Q.17 A 2.6 gram smooth table-tennis (ping-pong) ball has a diameter of 38 mm. Density (ρ) of air is 1.2 kg/m³. Neglect the effect of gravity. Take coefficient of drag as 0.5. If the ball is struck with an initial velocity of 30 m/s, the initial deceleration, in m/s², is _____.
- Q.18 On a flat plate, transition from laminar to turbulent boundary layer occurred at a critical Reynolds number (Re_{cr}). The empirical relations for the laminar and turbulent boundary layer thickness are given by $\frac{\delta_{lam}}{x} = 5.48 \text{Re}_x^{-0.5}$ and $\frac{\delta_{turb}}{x} = 0.37 \text{Re}_x^{-0.2}$, respectively. The ratio of laminar to turbulent boundary layer thickness, at the location of transition, is 0.3. The value of Re_{cr} is _____.
- Q.19 In a capillary tube of radius R = 0.25 mm, a fully developed laminar velocity profile is defined as, $u = \frac{R^2}{4\mu} \left(-\frac{dp}{dx}\right) \left(1 \frac{r^2}{R^2}\right)$. In this expression, $-\frac{dp}{dx} = 1$ MPa/m, μ is the dynamic viscosity of the fluid, and *r* is the radial position from the centerline of the tube. If the flow rate through the tube is 1000 mm³/s, the viscosity of the fluid, in Pa-s, is ______.
- Q.20 The skin friction coefficient for a turbulent pipe flow is defined as, $C_f = \frac{\tau_w}{1/2 \rho V^2}$, where τ_w is the wall shear stress and V is the average flow velocity. The value of C_f is empirically given by the relation: $C_f = 0.065 \left(\frac{2}{Re}\right)^{0.25}$, where *Re* is the Reynolds number. If the average flow velocity is 10 m/s, diameter of the pipe is 250 mm, kinematic viscosity of the fluid is 0.25×10^{-6} m²/s, and density of the fluid is 700 kg/m³, the skin friction drag induced by the flow over 1 m length of the pipe, in N, is _____.

A (150 mm \times 150 mm) square pillar is located in a river with water flowing at a velocity of Q.21 2 m/s, as shown in figure. The height of the pillar in water is 8 m. Take density of water as 1000 kg/m³ and kinematic viscosity as 1×10^{-6} m/s². The coefficient of drag of the pillar is 2.0. The drag force exerted by water on the pillar in N is _



Q.22 An orifice plate is used to measure flow rate of air (density = 1.23 kg/m^3) in a duct of 250 mm diameter as shown in figure. The volume flow rate is $1 \text{ m}^3/\text{s}$. Flow at sections 1 and 3 is uniform and section 2 is located at vena contracta. The diameter ratio, D_t/D_1 , is 0.66. The flow area at vena contracta, $A_2 = 0.65A_t$, where A_t is area of the orifice. The pressure difference between locations 2 and 3 in N/m² is _



END OF THE QUESTION PAPER

GATE 2018