

ALLE



**11.** Which of the following Boolean expressions is **not** a tautology ?

$$(1) (p \Rightarrow q) \lor (\sim q \Rightarrow p)$$

(2) 
$$(q \Rightarrow p) \lor (\sim q \Rightarrow p)$$

$$(3) (p \Rightarrow \sim q) \lor (\sim q \Rightarrow p)$$

$$(4) (\sim p \Rightarrow q) \lor (\sim q \Rightarrow p)$$

## Official Ans. by NTA (4)

12. Let  $A = [a_{ij}]$  be a real matrix of order  $3 \times 3$ , such that  $a_{i1} + a_{i2} + a_{i3} = 1$ , for i = 1, 2, 3. Then, the sum of all the entries of the matrix  $A^3$  is equal to : (1) 2 (2) 1 (3) 3 (4) 9

- 13. Let [x] denote the greatest integer less than or equal to x. Then, the values of  $x \in \mathbf{R}$  satisfying the equation  $[e^x]^2 + [e^x + 1] - 3 = 0$  lie in the interval :
  - (1)  $\left[0,\frac{1}{e}\right]$  (2)  $\left[\log_{e}2,\log_{e}3\right)$
  - (3) [1, e) (4)  $[0, \log_{e} 2)$

## Official Ans. by NTA (4)

14. Let the circle  $S : 36x^2 + 36y^2 - 108x + 120y + C = 0$ be such that it neither intersects nor touches the co-ordinate axes. If the point of intersection of the lines, x - 2y = 4 and 2x - y = 5 lies inside the circle S, then :

(1) 
$$\frac{25}{9} < C < \frac{13}{3}$$
 (2)  $100 < C < 165$   
(3)  $81 < C < 156$  (4)  $100 < C < 156$ 

## Official Ans. by NTA (4)

15. Let n denote the number of solutions of the equation  $z^2 + 3\overline{z} = 0$ , where z is a complex

number. Then the value of 
$$\sum_{k=0}^{k} \frac{1}{n^k}$$
 is equal to

(1) 1 (2) 
$$\frac{4}{3}$$
 (3)  $\frac{3}{2}$  (4) 2

## Official Ans. by NTA (2)

16. The number of solutions of  $\sin^7 x + \cos^7 x = 1$ ,  $x \in [0, 4\pi]$  is equal to

17. If the domain of the function  $f(x) = \frac{\cos^{-1}\sqrt{x^2 - x + 1}}{\sqrt{\sin^{-1}\left(\frac{2x - 1}{2}\right)}}$ 

is the interval ( $\alpha$ ,  $\beta$ ], then  $\alpha + \beta$  is equal to :

(1) 
$$\frac{3}{2}$$
 (2) 2 (3)  $\frac{1}{2}$  (4) 1

Official Ans. by NTA (1)

**18.** Let  $f : \mathbf{R} \to \mathbf{R}$  be defined as

$$f(\mathbf{x}) = \begin{cases} \frac{\mathbf{x}^{3}}{(1 - \cos 2\mathbf{x})^{2}} \log_{e} \left( \frac{1 + 2\mathbf{x}e^{-2\mathbf{x}}}{(1 - \mathbf{x}e^{-\mathbf{x}})^{2}} \right) &, \quad \mathbf{x} \neq 0 \\ \alpha &, \quad \mathbf{x} = 0 \end{cases}$$

If f is continuous at x = 0, then  $\alpha$  is equal to :

## Official Ans. by NTA (1)

- 19. Let a line L : 2x + y = k, k > 0 be a tangent to the hyperbola  $x^2 y^2 = 3$ . If L is also a tangent to the parabola  $y^2 = \alpha x$ , then  $\alpha$  is equal to :
  - (1) 12 (2) -12 (3) 24 (4) -24 Official Ans. by NTA (4)
- **20.** Let  $E_1: \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ , a > b. Let  $E_2$  be another ellipse such that it touches the end points of major axis of  $E_1$  and the foci of  $E_2$  are the end points of minor axis of  $E_1$ . If  $E_1$  and  $E_2$  have same eccentricities, then its value is :

(1) 
$$\frac{-1+\sqrt{5}}{2}$$
 (2)  $\frac{-1+\sqrt{8}}{2}$   
(3)  $\frac{-1+\sqrt{3}}{2}$  (4)  $\frac{-1+\sqrt{6}}{2}$ 

Official Ans. by NTA (1)

## **SECTION-B**

1. Let A = {0, 1, 2, 3, 4, 5, 6, 7}. Then the number of bijective functions  $f : A \rightarrow A$  such that f(1) + f(2) = 3 - f(3) is equal to

Official Ans. by NTA (720)

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- 2. If the digits are not allowed to repeat in any 8. number formed by using the digits 0, 2, 4, 6, 8, then the number of all numbers greater than 10,000 is equal to \_\_\_\_\_. **Official Ans. by NTA (96)** 9. Let  $A = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ . Then the number of  $3 \times 3$ 3. matrices B with entries from the set  $\{1, 2, 3, 4, 5\}$ and satisfying AB = BA is \_\_\_\_\_. Official Ans. by NTA (3125) 10. Consider the following frequency distribution : 4. Class: 0-6 6-12 12-18 18-24 24-30 Frequency : b 12 9 a 5 If mean =  $\frac{309}{22}$  and median = 14, then the value  $(a - b)^2$ is equal to \_\_\_\_\_. Official Ans. by NTA (4) 5. The sum of all the elements in the set  $\{n \in \{1, 2, \dots, 100\}$ H.C.F. of n and 2040 is 1} is equal to \_\_\_\_\_ Official Ans. by NTA (1251)
- 6. The area (in sq. units) of the region bounded by the curves  $x^2 + 2y 1 = 0$ ,  $y^2 + 4x 4 = 0$  and  $y^2 4x 4 = 0$ , in the upper half plane is \_\_\_\_\_.

### **Official Ans. by NTA (2)**

7. Let  $f : \mathbf{R} \to \mathbf{R}$  be a function defined as

$$f(\mathbf{x}) = \begin{cases} 3\left(1 - \frac{|\mathbf{x}|}{2}\right) & \text{if } |\mathbf{x}| \le 2\\ 0 & \text{if } |\mathbf{x}| > 2 \end{cases}$$

Let  $g : \mathbf{R} \to \mathbf{R}$  be given by g(x) = f(x + 2) - f(x - 2). If n and m denote the number of points in **R** where g is not continuous and not differentiable, respectively, then n + m is equal to \_\_\_\_\_.

### Official Ans. by NTA (4)

If the constant term, in binomial expansion of  $\left(2x^{r} + \frac{1}{x^{2}}\right)^{10}$  is 180, then r is equal to \_\_\_\_\_.

### Official Ans. by NTA (8)

Let 
$$y = y(x)$$
 be the solution of the differential

equation 
$$\left( (x+2)e^{\left(\frac{y+1}{x+2}\right)} + (y+1) \right) dx = (x+2) dy,$$

y(1) = 1. If the domain of y = y(x) is an open interval  $(\alpha, \beta)$ , then  $|\alpha + \beta|$  is equal to \_\_\_\_\_.

### Official Ans. by NTA (4)

10. The number of elements in the set  $\{n \in \{1, 2, 3, ..., 100\} | (11)^n > (10)^n + (9)^n\}$  is \_\_\_\_\_.

Official Ans. by NTA (96)