



JEE (Main)

PAPER-1 (B.E./B. TECH.)

2023

COMPUTER BASED TEST (CBT) Memory Based Questions & Solutions

Date: 01 February, 2023 (SHIFT-1) | TIME : (9.00 a.m. to 12.00 p.m)

Duration: 3 Hours | Max. Marks: 300

SUBJECT: MATHEMATICS

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PART : MATHEMATICS

1. $\lim_{n \rightarrow \infty} \left(\frac{1}{1+n} + \frac{1}{2+n} + \dots + \frac{1}{2n} \right) =$

- (1) 0 (2) $\frac{1}{n^2}$ (3) 1 (4) $\frac{1}{n^3}$

Ans. (2)

Sol. $\lim_{n \rightarrow \infty} \left(\frac{1}{1+n} + \frac{1}{2+n} + \dots + \frac{1}{2n} \right)$

$$= \lim_{n \rightarrow \infty} \sum_{r=1}^n \frac{1}{r+n}$$

$$= \lim_{n \rightarrow \infty} \sum_{r=1}^n \frac{1}{\left(\frac{r}{n} + 1\right)} \cdot \frac{1}{n}$$

$$\int_0^1 \frac{dx}{1+x} = [n \ln(1+x)]_0^1$$

$$n \ln 2 - n \ln 1 = n \ln 2$$

2. Sum of series $\frac{1}{1+1^2+1^4} + \frac{2}{1+2^2+2^4} + \frac{3}{1+3^2+3^4} + \dots$ upto 10 terms is

(1) $\frac{53}{111}$

(2) $\frac{54}{111}$

(3) $\frac{55}{111}$

(4) $\frac{56}{111}$

Ans. (3)

Sol. $t_n = \frac{n}{1+n^2+n^4} = \frac{n}{(n^2+n+1)(n^2-n+1)}$

$$= \frac{1}{2} \left(\frac{1}{n^2-n+1} - \frac{1}{n^2+n+1} \right)$$

$$t_1 = \frac{1}{2} \left(1 - \frac{1}{3} \right)$$

$$t_2 = \frac{1}{2} \left(\frac{1}{3} - \frac{1}{7} \right)$$

$$t_3 = \frac{1}{2} \left(\frac{1}{7} - \frac{1}{13} \right)$$

|

|

|

$$t_{10} = \frac{1}{2} \left(\frac{1}{91} - \frac{1}{111} \right)$$

$$\therefore S_{10} = t_1 + t_2 + t_3 + \dots + t_{10}$$

$$= \frac{1}{2} \left(1 - \frac{1}{111} \right) = \frac{55}{111}$$

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3. Number of three digit numbers which are divisible by 2 or 3 but not divisible by 7, is

Ans. (557)

Sol.

Divisible by 2

$$100, 102, 104, \dots, 998$$

$$t_n = a + (n-1)d \Rightarrow 998 = 100 + (n-1)2$$

$$\Rightarrow \frac{898}{2} = n-1$$

$$\Rightarrow n = 449 + 1 = 450$$

Divisible by 3

$$102, 105, 108, \dots, 999$$

$$t_n = a + (n-1)d \Rightarrow 999 - 102 = (n-1)3$$

$$\Rightarrow \frac{897}{3} = n-1$$

$$\Rightarrow n = 299 + 1 = 300$$

Divisible by 6

$$102, 108, 114, \dots, 996$$

$$996 - 102 = (n-1)6$$

$$n = 1 + \frac{894}{6} = 1 + 149 = 150$$

$$\therefore \text{No. divisible by 2 or 3} = 450 + 300 - 150 = 600$$

No. divisible by 21

$$105, 126, 147, \dots, 987$$

$$987 - 105 = (n-1)21$$

$$\Rightarrow n = 1 + 42 = 43$$

$$\therefore \text{Total required No.} = 600 - 43 = 557$$

4. If $f'(x) + f(x) = \int_0^2 f(t) dt$ and $f(0) = e^{-2}$, then find value of $2f(0) - f(2)$

(1) 0

(2) -1

(3) 1

(4) 2

Ans. (3)

Sol. Given $f'(x) + f(x) = \int_0^2 f(t) dt$

$$\text{Let } \int_0^2 f(t) dt = a$$

$$\therefore f'(x) + f(x) = a$$

$$f'(x) = a - f(x)$$

$$\frac{f'(x)}{a - f(x)} = 1$$

$$\therefore -\ln(a - f(x)) = x + c$$

$$\text{Put } x = 0$$

$$-\ln(a - e^{-2}) = c$$

$$\therefore -\ln(a - f(x)) = x - \ln(a - e^{-2})$$

$$\ln \frac{a - e^{-2}}{a - f(x)} = x$$

$$\Rightarrow \frac{a - e^{-2}}{a - f(x)} = e^x$$

$$a - f(x) = (a - e^{-2}) e^{-x}$$

$$f(x) = a - (a - e^{-2}) e^{-x}$$

$$\text{Now } \int_0^2 f(t) dt = a$$

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PAGE # 2

$$\Rightarrow \int_0^2 (a - (a - e^{-2}) e^{-t}) dt = a$$

$$\Rightarrow [at + (a - e^{-2}) e^{-t}]_0^2 = a$$

$$\Rightarrow 2a + (a - e^{-2}) e^{-2} - (a - e^{-2}) = a$$

$$\Rightarrow a + a e^{-2} - e^{-4} - a + e^{-2} = 0$$

$$a = \frac{e^{-4} - e^{-2}}{e^{-2}} = e^{-2} - 1$$

$$\text{Now } 2f(0) - f(2)$$

$$= 2e^{-2} - a + (a - e^{-2}) e^{-2}$$

$$= 2e^{-2} - e^{-2} + 1 - e^{-2}$$

$$= 1$$

5. If $19^{200} + 23^{200}$ is divided by 49, then remainder is

Ans. (29)

Sol. $(21 - 2)^{200} + (21 + 2)^{200} = 49\lambda + 2^{201}$

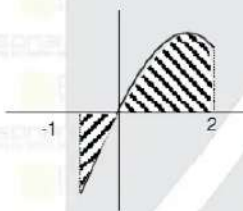
$$2^{201} = 8^{67} = (7 + 1)^{67} = 49\lambda + 7 \times 67 + 1$$

$$= 49\lambda + 470$$

$$= 49(\lambda + 9) + 29$$

6. If area divided by curve $f(x) = x|x - 3|$ and x-axis form $x = -1$ to $x = 2$ is A, then value of $12A$ is equal to

Ans. (62)



$$A = -\int_{-1}^0 (3x - x^2) dx + \int_0^2 (3x - x^2) dx$$

$$= \left(\frac{3x^2}{2} - \frac{x^3}{3} \right)_{-1}^0 + \left(\frac{3x^2}{2} - \frac{x^3}{3} \right)_0^2$$

$$= \left(-\frac{3}{2} + \frac{1}{3} \right) + \left(6 - \frac{8}{3} \right)$$

$$= \frac{3}{2} + \frac{1}{3} + 6 - \frac{8}{3} = \frac{31}{6}$$

$$\Rightarrow 12A = 62$$

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7. Negation of statement $q \vee ((\sim q) \wedge p)$ is

- (1) $\sim p \wedge q$ (2) $\sim p \vee q$ (3) $\sim p \vee \sim q$ (4) $\sim q \wedge \sim p$

Ans. (4)

Sol. Negation of given statement is

$$\begin{aligned} & \sim (q \vee (\sim q) \wedge p) \\ & = \sim q \wedge \sim ((\sim q) \wedge p) \\ & = \sim q \wedge (q \vee \sim p) \\ & \equiv (\sim q \wedge q) \vee (\sim q \wedge \sim p) \\ & \sim q \wedge \sim p \end{aligned}$$

8. Sum of series $\frac{1}{1!50!} + \frac{1}{3!48!} + \dots + \frac{1}{51!0!}$ is

- (1) $\frac{2^{50}}{5!}$ (2) $\frac{2^{51}}{5!}$ (3) $\frac{2^{50}}{50!}$ (4) $\frac{2^{51}}{50!}$

Ans. (1)

Sol.
$$\frac{1}{1!50!} + \frac{1}{3!48!} + \dots + \frac{1}{51!0!}$$

$$\frac{1}{5!} \left(\frac{5!}{1!50!} + \frac{5!}{3!48!} + \dots + \frac{5!}{51!0!} \right)$$

$$\frac{1}{5!} ({}^{51}C_1 + {}^{51}C_3 + \dots + {}^{51}C_{51})$$

$$\frac{1}{5!} \left(\frac{2^{51}}{2} \right) = \frac{2^{50}}{5!}$$

9. If a curve $y = y(x)$ satisfy differential equation $\frac{dy}{dx} + y \tan x = x \sec x$ and $y(0) = 1$ then equation of curve is

- (1) $y = \frac{x \tan x - \int \sec x + 1}{\sec x}$ (2) $y = \frac{x \cot x + 1}{\sec x}$
 (3) $y = \frac{\int \sec x + 1}{\sec x}$ (4) $y = \frac{x \tan x - \int \sec x + 1}{\sec x}$

Ans. (1)

Sol. $\frac{dy}{dx} + y \tan x = x \sec x$ linear in y

I. F. = $e^{\int \tan x dx} = e^{\int \sec x} = \sec x$

\therefore solution is

$$y \cdot \sec x = \int x \sec x \cdot \sec x dx + c$$

$$y \sec x = \int x \sec^2 x dx + c$$

$$y \sec x = x \tan x - \int \tan x dx + c$$

$$y \sec x = x \tan x - \int \sec x + c$$

$y(0) = 1 \quad \therefore 1 = 0 - 0 + c$
 $c = 1$

$\therefore y \sec x = x \tan x - \int \sec x + 1$

$$y = \frac{x \tan x - \int \sec x + 1}{\sec x}$$

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PAGE # 4

10. If $\left| \frac{z-2}{z-3} \right| = 2$ then locus of z is a circle whose centre is (α, β) and radius is γ then value of $3(\alpha+\beta+\gamma)$ is

Ans. (12)

Sol. $\left| \frac{z-2}{z-3} \right| = 2$

$$(z-2)(\bar{z}-2) = 4(\bar{z}-3)(z-3)$$

$$\Rightarrow z\bar{z} - 2z - 2\bar{z} + 4 = 4(z\bar{z} - 3z - 3\bar{z} + 9)$$

$$3z\bar{z} - 10z - 10\bar{z} + 32 = 0$$

$$z\bar{z} - \frac{10}{3}z - \frac{10}{3}\bar{z} + \frac{32}{3} = 0$$

$$\alpha = -\frac{10}{3} \quad c = \frac{32}{3}$$

$$\text{centre} \left(\frac{10}{3}, 0 \right) \quad \gamma = \sqrt{|\alpha|^2 - c}$$

$$= \sqrt{\frac{100}{9} - \frac{32}{3}} = \frac{2}{3}$$

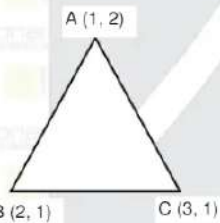
$$\therefore \alpha + \beta + \gamma = \frac{10}{3} + \frac{2}{3} = \frac{12}{3} \quad \therefore 3(\alpha + \beta + \gamma) = 12$$

11. Orthocentre of a triangle whose vertices are $(1, 2)$, $(2, 1)$ and $(3, 1)$ is

- (1) $(1, 1)$ (2) $(-1, 1)$ (3) $(1, -1)$ (4) $(0, 0)$

Ans. (3)

Sol.



$$M_{AB} = \frac{2-1}{1-2} = -1$$

\therefore Eq. of altitude through C is

$$y - 1 = 1(x - 3)$$

$$x - y = 2 \quad \text{---(1)}$$

$$M_{BC} = 0$$

\therefore Altitude through A is

$$y - 2 = \frac{1}{0}(x - 1) \Rightarrow x = 1 \quad \text{---(2)}$$

\therefore Orthocentre is $(1, -1)$

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PAGE # 5

12. If mean and variance of $1, 3, 5, \alpha, \beta$ are 5 and 8 respectively then the value of $\alpha^3 + \beta^3$ is

Ans. (1072)

Sol. Mean = $\frac{1+3+5+\alpha+\beta}{5} = 5$

$$\alpha + \beta = 16 \quad \text{---(1)}$$

$$\sigma^2 = \frac{1+9+25+\alpha^2+\beta^2}{5} = 8$$

$$8 = \frac{35 + \alpha^2 + \beta^2}{5} - 25$$

$$33 \times 5 - 35 = \alpha^2 + \beta^2$$

$$\alpha^2 + \beta^2 = 130 \quad \text{--- (2)}$$

$$(\alpha + \beta)^2 = \alpha^2 + \beta^2 + 2\alpha\beta$$

$$256 - 130 = 2\alpha\beta \Rightarrow \alpha\beta = 63$$

$$\begin{aligned} \alpha^3 + \beta^3 &= (\alpha + \beta)^3 - 3\alpha\beta(\alpha + \beta) \\ &= 4096 - 3024 \\ &= 1072 \end{aligned}$$

13. Set $S = \{x : (\sqrt{3} + \sqrt{2})^{x^2-4} + (\sqrt{3} - \sqrt{2})^{x^2-4} = 10\}$ then $n(S)$ equals.

(1) 2

(2) 3

(3) 4

(4) 6

Ans. (3)

Sol. $(\sqrt{3} + \sqrt{2})^{x^2-4} + (\sqrt{3} - \sqrt{2})^{x^2-4} = 10$

$$\left(\frac{(\sqrt{3} + \sqrt{2})^{x^2-4}}{(\sqrt{3} + \sqrt{2})^2}\right) + \left(\frac{(\sqrt{3} - \sqrt{2})^{x^2-4}}{(\sqrt{3} - \sqrt{2})^2}\right) = 10$$

$$\Rightarrow \left(\frac{5 + 2\sqrt{6}}{2}\right)^{\frac{x^2-4}{2}} + \left(\frac{5 - 2\sqrt{6}}{2}\right)^{\frac{x^2-4}{2}} = 10$$

$$\text{Now } (5 + 2\sqrt{6})(5 - 2\sqrt{6}) = 25 - 24 = 1$$

$$\& (5 + 2\sqrt{6}) + (5 - 2\sqrt{6}) = 10$$

$$\therefore \frac{x^2-4}{2} = \pm 1 \Rightarrow x^2 = 4 \pm 2$$

$$\Rightarrow x = \pm\sqrt{6} \pm \sqrt{2}$$

$$\therefore n(S) = 4$$

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14. If $8, a_2, a_3, \dots$, are in A.P. such that sum of first 4 terms is 50 and sum of last 4 terms is 170, then find product of middle terms.

Ans. (754)

Sol. $S_4 = 50$

$$2(16 + 3d) = 50$$

$$d = 3$$

$$4a + d(4n - 10) = 170$$

$$32 + 3(4n - 10) = 170$$

$$4n - 10 = 46$$

$$n = 14$$

Middle terms are T_7, T_8

$$T_7 T_8 = (8 + 6 \times 3)(8 + 7 \times 3) = 26 \times 29$$

$$= 754$$

15. Number of all possible words by using all letters of the word "ASSASSINATION" with meaning or without meaning such that all vowels are together, is

(1) (10) 7!

(2) (8) 7!

(3) 9!

(4) (12) 7!

Ans. (1)

Sol. ASSASSINATION

Vowels \rightarrow AAIAIO

all vowels are together

$$\therefore \text{Now words} = \frac{(13-6+1)!}{4!2!} \times \frac{6!}{3!2!}$$

$$8! \times 5 \times 4!$$

$$= \frac{4! \cdot 2 \times 6 \times 2}{(10)!}$$

16. If $f(x) = x^2 + g'(1)x + g''(2)$ and $g(x) = 2x + f'(1)$ then value of $f(4) - g(4)$ is equal to

Ans. (12)

Sol. $g(x) = 2x + f'(1)$
 $g'(x) = 2$ and $g''(x) = 0$
 $g'(1) = 2$ and $g''(2) = 0$
 $f(x) = x^2 + 2x$ (1)
 $f'(x) = 2x + 2$
 $f'(1) = 4$
 So, $g(x) = 2x + 4$
 Now $f(4) - g(4)$
 $= 16 + 8 - (8 + 4)$
 $= 24 - 12 = 12$

17. Let region for $x \in [0, 1]$ given by

A : $2x \leq y \leq \sqrt{4(x-1)^2}$ with y-axis.

B : $y = \min \left\{ 2x, \sqrt{4(x-1)^2} \right\}$ with x-axis then $\frac{A}{B}$ equals

- (1) 1 (2) 2 (3) 3 (4) 4

Ans. (1)

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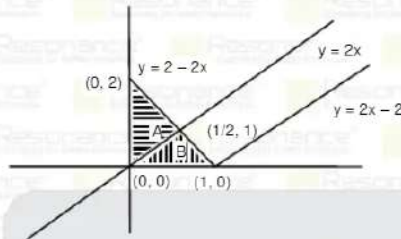
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PAGE # 7

Sol.



$$A = \frac{1}{2} \times 2 \times \frac{1}{2} = \frac{1}{2}$$

$$B = \frac{1}{2} \times 1 \times 1 = \frac{1}{2}, \text{ So } \frac{A}{B} = 1$$

18. If system of linear equations $\lambda x + y + z = 1$, $x + \lambda y + z = 1$ and $x + y + \lambda z = 1$ is inconsistent for some values of λ then find value of $\sum(|\lambda|^2 + |\lambda|)$

- (1) 2 (2) 6 (3) 4 (4) 1

Ans. (2)

Sol. $D = \begin{vmatrix} \lambda & 1 & 1 \\ 1 & \lambda & 1 \\ 1 & 1 & \lambda \end{vmatrix} = \begin{vmatrix} \lambda-1 & 0 & 1-\lambda \\ 0 & \lambda-1 & 1-\lambda \\ 1 & 1 & \lambda \end{vmatrix}$

$$= (\lambda-1)^2 \begin{vmatrix} 1 & 0 & -1 \\ 0 & 1 & -1 \\ 1 & 1 & \lambda \end{vmatrix} = (\lambda-1)^2 (1+1+\lambda)$$

$$D = (\lambda-1)^2 (\lambda+2)$$

$$D = 0 \Rightarrow \lambda = 1, -2$$

$$D_1 = \begin{vmatrix} 1 & 1 & 1 \\ 1 & \lambda & 1 \\ 1 & 1 & \lambda \end{vmatrix} = \begin{vmatrix} 1 & 1 & 1 \\ 0 & \lambda-1 & 0 \\ 0 & 0 & \lambda-1 \end{vmatrix} = (\lambda-1)^2$$

$$D_1 \neq 0 \text{ for } \lambda = -2$$

When $\lambda = 1$, all equations are identical, so number of solutions are infinite.

$$\Sigma(\lambda_1^2 + |\lambda_1|) = |-2|^2 + |-2| = 6$$

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19. $\int_0^1 (x^{2l} + x^{13} + x^7)(2x^{14} + 3x^7 + 6)^{1/7} dx = \frac{1}{l} (11)^{m/n}$ then value of $l + m + n$ is equal to

Ans. (63)

Sol. $\int (x^{2l} + x^{13} + x^7)(2x^{14} + 3x^7 + 6x^7)^{1/7} dx$

$$2x^{2l} + 3x^{14} + 6x^7 = t$$

$$42(x^{2l} + x^{13} + x^7) dx = dt$$

$$\frac{1}{42} \int t^{1/7} dt = \left(\frac{t^{8/7}}{8/7} \times \frac{1}{42} \right)_0^{11}$$

$$= \frac{1}{48} \left(\frac{t^8}{t^7} \right)_0^{11} = \frac{1}{48} (11)^{8/7}$$

$$l = 48, m = 8, n = 7$$

$$l + m + n = 63$$

20. The shortest distance between lines.

$$\frac{x-5}{3} = \frac{y-1}{7} = \frac{z-3}{5} \text{ \& } \frac{x+7}{5} = \frac{y+5}{11} = \frac{z+1}{3} \text{ is}$$

(1) $\frac{80}{\sqrt{354}}$

(2) $\frac{40}{\sqrt{354}}$

(3) $\frac{160}{\sqrt{354}}$

(4) $\frac{320}{\sqrt{354}}$

Ans. (3)

Sol. $\vec{b}_1 \times \vec{b}_2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & 7 & 5 \\ 5 & 11 & 3 \end{vmatrix} = -34\hat{i} + 16\hat{j} - 2\hat{k}$

$$S.D. = \frac{|(\vec{a}_2 - \vec{a}_1) \cdot (\vec{b}_1 \times \vec{b}_2)|}{|\vec{b}_1 \times \vec{b}_2|} = \frac{|(12 + 6i + 4k) \cdot (-34i + 16j + 2k)|}{\sqrt{34^2 + 16^2 + 2^2}}$$

$$\frac{408 - 96 + 8}{\sqrt{1156 + 256 + 4}} = \frac{320}{\sqrt{1416}} = \frac{160}{\sqrt{354}}$$

21. Let $R = \{(a, b) : 3a - 3b + \sqrt{7} \text{ is irrational}\}$ then

(1) R is an equivalence relation

(2) R is symmetric but not reflexive.

(3) R is reflexive but not symmetric

(4) R is reflexive and symmetric but not transitive

Ans. (3)

Sol. Clearly $\left(\frac{\sqrt{7}}{3}, 0\right) \in R$ but $\left(0, \frac{\sqrt{7}}{3}\right) \notin R$

So it is not symmetric

C is correct option

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PAGE # 9

22. Let S be solution set for values of x satisfying $\cos^{-1}(2x) + \cos^{-1}\sqrt{1-x^2} = \pi$ then $\sum_{x \in S} 2 \sin^{-1}(x^2-1)$ is equal to

- (1) 0 (2) $-\sin^{-1}\left(\frac{24}{25}\right)$ (3) $\sin^{-1}\left(\frac{\sqrt{3}}{4}\right)$ (4) $\pi - \sin^{-1}\left(\frac{\sqrt{3}}{4}\right)$

Ans. (2)

Sol. $x \in \left[-\frac{1}{2}, \frac{1}{2}\right]$

$\sqrt{1-x^2} = -\cos(\cos^{-1} 2x)$ (1)

$\Rightarrow 1-x^2 = 4x^2 \Rightarrow x = \pm \frac{1}{\sqrt{5}} \Rightarrow x = \frac{-1}{\sqrt{5}}$ from (1)

$\sum_{x \in S} 2 \sin^{-1}(x^2-1) = 2 \sin^{-1}\left(\frac{-4}{5}\right) = -\sin^{-1}\frac{24}{25}$

23. A triangle be such that $\cos 2A + \cos 2B + \cos 2C$ is minimum, if in radius of the triangle is 3 then which of the following is correct.

- (1) area of Δ is $\frac{6\sqrt{3}}{2}$ (2) perimeter of Δ is $18\sqrt{3}$
 (3) area of Δ is $2\sqrt{3}$ (4) perimeter of Δ is $9\sqrt{3}$

Ans. (2)

Sol. min when $A = B = C = 60^\circ$

$r = \frac{\Delta}{S} = 3 \Rightarrow \frac{\frac{\sqrt{3}}{4} a^2}{\frac{3a}{2}} = 3$

$\frac{a}{2\sqrt{3}} = 3 \Rightarrow a = 6\sqrt{3}$

Perimeter = $3a = 18\sqrt{3}$

24. If solution of $\frac{dy}{dx} + \frac{x+a}{y-2} = 0$ is a circle and $y(0) = 1$, area of circle is 2π . P and Q are point of intersection of circle with y-axis. Normal at P and Q intersect. x-axis at R and S the length of RS is.

Ans. (4)

Sol. $(y-2)dy + (x+a)dx = 0$

$\frac{x^2}{2} + ax + \frac{y^2}{2} - 2y = c \Rightarrow y(0) = 1 \Rightarrow c = \frac{-3}{2}$

$x^2 + y^2 + 2ax - 4y + 3 = 0$

area = 2π

$\pi \times (a^2 + 4 - 3) = 2\pi \Rightarrow a = 1$

P(0, 1) Q(0, 3)

Normal at P(0, 1) $\Rightarrow x + y = 1$

$\Rightarrow R(1, 0)$

Normal at Q(0, 3) $\Rightarrow y - x = 3$

$\Rightarrow S(-3, 0)$

length of RS = 4

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