

Telangana State Council Higher Education

Notations :

- Options shown in green color and with ✓ icon are correct.
- Options shown in red color and with ✗ icon are incorrect.

Question Paper Name :	EngineeringEnglish 18th Jul 2022 Shift 2
Subject Name :	Engineering (English)
Creation Date :	2022-07-19 13:06:33
Duration :	180
Total Marks :	160
Display Marks:	No
Calculator :	None
Magnifying Glass Required? :	No
Ruler Required? :	No
Eraser Required? :	No
Scratch Pad Required? :	No
Rough Sketch/Notepad Required? :	No
Protractor Required? :	No
Show Watermark on Console? :	Yes
Highlighter :	No
Auto Save on Console?	Yes
Change Font Color :	No
Change Background Color :	No
Change Theme :	No
Help Button :	No
Show Reports :	No
Show Progress Bar :	No

Engineering (English)

Group Number :	1
Group Id :	1056152
Group Maximum Duration :	0
Group Minimum Duration :	180
Show Attended Group? :	No
Edit Attended Group? :	No
Break time :	0
Group Marks :	160
Is this Group for Examiner? :	No
Examiner permission :	Cant View
Show Progress Bar? :	No

Mathematics

Section Id :	1056154
Section Number :	1
Section type :	Online
Mandatory or Optional :	Mandatory

Number of Questions :	80
Number of Questions to be attempted :	80
Section Marks :	80
Enable Mark as Answered Mark for Review and Clear Response :	Yes
Maximum Instruction Time :	0
Sub-Section Number :	1
Sub-Section Id :	1056154
Question Shuffling Allowed :	Yes

Question Number : 1 Question Id : 105615161 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

Let \mathbb{R} be the set of all real numbers.

Statement I : The function $f : \left(-\frac{\pi}{2}, \frac{\pi}{2}\right) \rightarrow \mathbb{R}$ defined by $f(x) = \sec x + \tan x$ is a one - one function.

Statement II : The function $f : [0, \infty) \rightarrow \mathbb{R}$ defined by $f(x) = x^2$ is a one – one function.

Which of the above statements is(are) true?

Options :

Statement I is true, but Statement II is false

1. ✖

Statement II is true, but Statement I is false

2. ✖

Both Statement I and Statement II are true

3. ✔

Both Statement I and Statement II are false

4. ✖

Question Number : 2 Question Id : 105615162 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

Let \mathbb{R} be the set of all real numbers. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be a function defined by

$$f(x) = \begin{cases} 2x - 5, & \text{if } x < -3 \\ x + 2, & \text{if } -3 \leq x < 5 \\ 3x + 1, & \text{if } x \geq 5 \end{cases}$$

Match the following

List - I	List - II
A) $f(-5) + f(0) + f(-1) =$	D) 16
B) $f(f(5) + 10f(-3)) =$	II) 40
C) $f(f(-4)) =$	III) -32
D) $f(f(f(1))) =$	IV) -12
	V) 19

The correct match is

Options :

1. ✘

A	B	C	D
III	II	V	I

2. ✘

A	B	C	D
V	IV	I	III

3. ✔

A	B	C	D
IV	V	II	I

4. ✘

A	B	C	D
IV	V	III	I

Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0
Correct Marks : 1 Wrong Marks : 0

$$\text{If } A + B = \begin{bmatrix} 2 & 1 & 2 \\ 1 & 2 & 0 \\ 0 & 2 & 2 \end{bmatrix}, AB = \begin{bmatrix} 1 & 2 & 2 \\ 1 & 1 & 0 \\ 1 & 2 & 1 \end{bmatrix} \text{ then } A^2 + B(A + B) =$$

Options :

$$\begin{bmatrix} 4 & 6 & 6 \\ 3 & 4 & 2 \\ 1 & 6 & 3 \end{bmatrix}$$

1. ✓

$$\begin{bmatrix} 4 & 9 & 6 \\ 3 & 3 & 2 \\ 4 & 7 & 4 \end{bmatrix}$$

2. ✗

$$\begin{bmatrix} 6 & 10 & 8 \\ 4 & 5 & 2 \\ 4 & 9 & 6 \end{bmatrix}$$

3. ✗

$$\begin{bmatrix} 3 & 4 & 4 \\ 2 & 3 & 2 \\ 0 & 4 & 2 \end{bmatrix}$$

4. ✗

Question Number : 4 Question Id : 105615164 Question Type : MCQ Option Shuffling : Yes Display Question Number :
Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0
Correct Marks : 1 Wrong Marks : 0

A, P, B are 3×3 matrices. If $|-B| = 5$, $|BA^T| = 15$, $|P^TAP| = -27$, then one of the values of $|P|$ is

Options :

3

1. ✓

-5

2. ✘

9

3. ✘

6

4. ✘

Question Number : 5 Question Id : 105615165 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If A is a 3×3 matrix and $|A| = \frac{1}{2}$ then $|A^{-1}(\text{Adj}(\text{Adj}A))|^{-1} =$

Options :

8

1. ✓

$\frac{1}{8}$

2. ✘

$\frac{1}{2}$

3. ✘

2

4. ✘

Question Number : 6 Question Id : 105615166 Question Type : MCQ Option Shuffling : Yes Display Question Number :

Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0
Correct Marks : 1 Wrong Marks : 0

Let $x = \alpha, y = \beta, z = \gamma$ be the unique solution of the system of simultaneous linear equations $2x + 3y - 2z + 4 = 0, 3x - 4y + 3z + 5 = 0, kx - 2y + z + 3 = 0$. If $\alpha = -2$ then $k =$

Options :

$$\begin{vmatrix} 1 & 2 \\ 3 & 5 \end{vmatrix}$$

1. ✖

$$\begin{vmatrix} 5 & 3 \\ 1 & 2 \end{vmatrix}$$

2. ✖

$$\begin{vmatrix} 3 & 5 \\ 1 & 2 \end{vmatrix}$$

3. ✔

$$\begin{vmatrix} 3 & 5 \\ 2 & 1 \end{vmatrix}$$

4. ✖

Question Number : 7 Question Id : 105615167 Question Type : MCQ Option Shuffling : Yes Display Question Number :
Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0
Correct Marks : 1 Wrong Marks : 0

If the point (x, y) satisfies the equation $\frac{x+i(x-2)}{3+i} - i = \frac{2y+i(1-3y)}{i-3}$, then $x + y =$

Options :

$$4$$

1. ✖

2

2. ✓

0

3. ✘

-2

4. ✘

Question Number : 8 Question Id : 105615168 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If $\cos \alpha + \cos \beta + \cos \gamma = 0$ and $\sin \alpha + \sin \beta + \sin \gamma = 0$ then
 $\cos 2\alpha + \cos 2\beta + \cos 2\gamma =$

Options :

$\frac{3}{2}$

1. ✘

$$\cos^2 \frac{\alpha}{2} + \cos^2 \frac{\beta}{2} + \cos^2 \frac{\gamma}{2}$$

2. ✘

$$3 \sin(\alpha + \beta + \gamma)$$

3. ✘

$$\cos(\alpha + \beta) + \cos(\beta + \gamma) + \cos(\gamma + \alpha)$$

4. ✓

Question Number : 9 Question Id : 105615169 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

One of the values of $(-32i)^{\frac{2}{5}}$ is

Options :

$$4 \operatorname{cis} \frac{2\pi}{5}$$

1. ✖

$$4 \operatorname{cis} \frac{3\pi}{5}$$

2. ✔

$$4 \operatorname{cis} \frac{4\pi}{5}$$

3. ✖

$$4 \operatorname{cis} \frac{6\pi}{5}$$

4. ✖

Question Number : 10 Question Id : 105615170 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If the quadratic equations $x^2 - 7x + 3c = 0$ and $x^2 + x - 5c = 0$ have a common root, then for non-zero real value of c the sign of the expression $x^2 - 3x + c$ is

Options :

negative for all $x \in \mathbb{R}$

1. ✖

positive for all $x \in (1, 3)$

2. ✖

negative for all $x \in (1, 3)$

3. ✖

positive for all $x \in \mathbb{R}$

4. ✔

Question Number : 11 Question Id : 105615171 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

Let $f(x) = \frac{6x^2 - 18x + 21}{6x^2 - 18x + 17}$. If m is the maximum value of $f(x)$ and $f(x) > n \forall x \in \mathbb{R}$
Then $14m - 7n =$

Options :

-1

1. ✖

23

2. ✔

35

3. ✖

42

4. ✖

Question Number : 12 Question Id : 105615172 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If α, β, γ are the roots of the equation $x^3 + x^2 + x + r = 0$ and $\alpha^3 + \beta^3 + \gamma^3 = 5$, then
 $r =$

Options :

$$\frac{-1}{2}$$

1. ✘

$$1$$

2. ✘

$$-1$$

3. ✔

$$\frac{1}{2}$$

4. ✘

Question Number : 13 Question Id : 105615173 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If $\frac{5}{2}$ is the sum of two roots of the equation $6x^6 - 25x^5 + 31x^4 - 31x^2 + 25x - 6 = 0$ then the sum of all non-real roots of the equation is

Options :

does not exist

1. ✘

$$0$$

2. ✘

$$\frac{5}{3}$$

3. ✔

$\frac{2}{5}$

4. ✖

Question Number : 14 Question Id : 105615174 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If $1 + \sqrt{2}$ and $2 - i$ are the roots of the equation $x^4 + bx^3 + cx^2 + dx + e = 0$ where b, c, d, e are rational numbers, then the roots of the equation $bx^2 + cx + d = 0$ are

Options :

real and different

1. ✖

real and equal

2. ✔

purely imaginary

3. ✖

complex conjugate

4. ✖

Question Number : 15 Question Id : 105615175 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

Let the transformed equation of $2x^4 - 8x^3 + 3x^2 - 1 = 0$ so that the term containing the cubic power of x is absent be $2x^4 + bx^2 + cx + d = 0$. Then $b =$

Options :

-18

1. ✖

-15

2. ✖

-9

3. ✔

-16

4. ✖

Question Number : 16 Question Id : 105615176 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

a, b, c are three particular speakers among the 10 speakers of a meeting. The number of ways of arranging all the 10 speakers on the dias in a row so that all the three speakers a, b, c do not sit together is

Options :

714 (7!)

1. ✖

89 (8!)

2. ✖

719 (7!)

3. ✖

84 (8!)

4. ✔

Question Number : 17 Question Id : 105615177 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

The exponent of 6 in 72! is

Options :

1. ✓ 34

2. ✗ 70

3. ✗ 17

4. ✗ 35

Question Number : 18 Question Id : 105615178 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If the 4th term in the expansion of $\left(\frac{x}{2} - \frac{2y}{3}\right)^6$ is -20 , then $xy =$

Options :

1. ✗ 2

2. ✓ 3

3. ✗ 8

4. ✖

Question Number : 19 Question Id : 105615179 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

$$\text{If } \int \frac{x+3}{(x-1)^2(2x-1)} dx = \frac{A}{x-1} + B \log(2x-1) + C \log(x-1) + K \text{ then } A + B + C =$$

Options :

3

1. ✖

11

2. ✖

-4

3. ✔

-11

4. ✖

Question Number : 20 Question Id : 105615180 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

$$\text{If } \frac{x^2+7}{(x^2+1)(x-2)} = \frac{A}{x-2} + \frac{Bx+C}{x^2+1}, \text{ then the determinant of the matrix } \begin{pmatrix} A & B \\ C & \frac{2}{5} \end{pmatrix} \text{ is}$$

Options :

5

1. ✖

-5

2. ✖

$\frac{94}{25}$

3. ✖

-2

4. ✔

Question Number : 21 Question Id : 105615181 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If $\tan 15^\circ$ and $\tan 30^\circ$ are the roots of the equation $x^2 + px + q = 0$, then $pq =$

Options :

$\frac{6\sqrt{3} + 10}{\sqrt{3}}$

1. ✖

$\frac{10 - 6\sqrt{3}}{3}$

2. ✔

$\frac{10 + 6\sqrt{3}}{3}$

3. ✖

$\frac{10 - 6\sqrt{3}}{\sqrt{3}}$

4. ✖

Question Number : 22 Question Id : 105615182 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If $\cos x + \cos y = p$, $\sin x + \sin y = q$, then $\cos\left(\frac{x-y}{2}\right) =$

Options :

1. ✓ $\pm \frac{\sqrt{p^2 + q^2}}{2}$

2. ✗ $\pm \frac{pq}{2}$

3. ✗ $\pm \left(\frac{p+q}{2}\right)$

4. ✗ $\pm \frac{\sqrt{p^2 + q^2}}{4}$

Question Number : 23 Question Id : 105615183 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If $A + B + C = \frac{3\pi}{2}$ then $4 \sin A \sin B \sin C + \cos 2A + \cos 2B + \cos 2C =$

Options :

1. ✓ $-\sin(A+B+C)$

2. ✗ $\cos(A+B+C)$

$$\sin(A+B+C)$$

3. ✖

$$2 - \cos(A+B+C)$$

4. ✖

Question Number : 24 Question Id : 105615184 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

$$\frac{e^{4x} + e^{-4x} + 14}{4(e^x - e^{-x})^2} =$$

Options :

$$\sinh^2 x + \cosh^2 x$$

1. ✔

$$\sinh^2 x + \operatorname{sech}^2 x$$

2. ✖

$$\cosh^2 x + \operatorname{sech}^2 x$$

3. ✖

$$\cosh^2 x + \tanh^2 x$$

4. ✖

Question Number : 25 Question Id : 105615185 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

$$\text{If } \tanh x = \frac{1}{2} \text{ then } \sinh 2x - \operatorname{sech} 2x =$$

Options :

$$\frac{29}{15}$$

1. ✖

$$\frac{11}{15}$$

2. ✔

$$3$$

3. ✖

$$\frac{-13}{15}$$

4. ✖

Question Number : 26 Question Id : 105615186 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

In triangle ABC, if A is acute, C is obtuse, $\sin A = \frac{3\sqrt{3}}{14}$, $a = 3$ and $b = 5$, then $c =$

Options :

$$\frac{16}{7}$$

1. ✖

$$7$$

2. ✔

$$\frac{14}{3}$$

3. ✖

$$6$$

4. ✖

Question Number : 27 Question Id : 105615187 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If Δ denotes the area of triangle ABC, then $(b \sin C + c \sin B) (b \cos C + c \cos B) =$

Options :

$ab \cos C$

1. ✘

2Δ

2. ✘

$bc \cos A$

3. ✘

4Δ

4. ✔

Question Number : 28 Question Id : 105615188 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

Let A be the area of in-circle and A_1, A_2, A_3 be the areas of ex-circles of a triangle. If $A_1 = 4, A_2 = 9, A_3 = 16$, then $A =$

Options :

81

1. ✘

$\frac{61}{169}$

2. ✘

$\frac{144}{61}$

3. ✘

$$\frac{144}{169}$$

4. ✓

Question Number : 29 Question Id : 105615189 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If $3\bar{i} - 5\bar{j} + 2\bar{k}$, $7\bar{i} + 2\bar{j} - 4\bar{k}$, $\bar{i} - 3\bar{j} + 4\bar{k}$ and $-7\bar{i} - 17\bar{j} + 16\bar{k}$ are position vectors of the points A, B, C and D respectively, then the angle between \overline{AB} and \overline{CD} is

Options :

1. 0°

1. ✘

2. $\frac{\pi}{4}$

2. ✘

3. $\frac{\pi}{2}$

3. ✘

4. π

4. ✓

Question Number : 30 Question Id : 105615190 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If $A(2\bar{i} + \bar{j} - \bar{k})$, $B(\lambda\bar{i} + 5\bar{j} + 4\bar{k})$, $C(-4\bar{i} + 3\bar{j} + 2\bar{k})$ and $D(-\bar{i} - 2\bar{j} + 3\bar{k})$ are four points in space such that $\overline{AB} = x\overline{AC} + y\overline{AD}$ for some real numbers $x \neq 0, y \neq 0$ then $17(\lambda + 9) =$

Options :

1. 5

1. ✘

3

2. ✖

7

3. ✔

9

4. ✖

Question Number : 31 Question Id : 105615191 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

Let a plane P has the points \bar{i} , \bar{j} and $\bar{i} + \bar{j} + \bar{k}$. Let L be the line through the point A and parallel to the vector $\bar{i} - \bar{j} + \bar{k}$. If the plane P and line L intersect at a point B(0,3,2) and the distance from A to B is 3 units, then equations of the normal to the plane P through A are

Options :

$$\frac{x-3}{1} = \frac{y}{1} = \frac{z-5}{-1}$$

1. ✔

$$\frac{x+3}{1} = \frac{y-6}{1} = \frac{z-1}{-1}$$

2. ✖

$$\frac{x+3}{1} = \frac{y}{1} = \frac{z-5}{-1}$$

3. ✖

$$\frac{x+3}{1} = \frac{y-6}{-1} = \frac{z+1}{1}$$

4. ✖

Question Number : 32 Question Id : 105615192 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

Let $\vec{a} = \vec{i} + \vec{j} + \vec{k}$ and \vec{b} be two vectors such that $\vec{a} \cdot \vec{b} = 1$, $\cos(\vec{a}, \vec{b}) = \frac{1}{3}$ and the components of \vec{b} w.r.t $(\vec{i}, \vec{j}, \vec{k})$ be integers. Then the number of possible vectors that represent \vec{b} is

Options :

- 1. ✖
- 2. ✖
- 3. ✔
- 4. ✖

Question Number : 33 Question Id : 105615193 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

Let π_1 be the plane passing through the point $2\vec{i} - \vec{j} + \vec{k}$ and perpendicular to the vector $a\vec{i} + 2\vec{j} - 3\vec{k}$ and π_2 be the plane passing through the point $\vec{i} + 2\vec{j} - \vec{k}$ and perpendicular to the vector $\vec{i} - 2\vec{j} + \vec{k}$. If θ is the angle between the planes π_1 and π_2 and $\cos \theta = -\sqrt{\frac{3}{7}}$, then the integral value of a is

Options :

- 1. ✖

-1

2. ✘

2

3. ✘

1

4. ✔

Question Number : 34 Question Id : 105615194 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If \vec{a} and \vec{b} are two vectors such that $\vec{a} = 2\vec{i} + 2\vec{j} + p\vec{k}$, $|\vec{b}| = 7$, $\vec{a} \cdot \vec{b} = 4$ and $|\vec{a} \times \vec{b}| = 5\sqrt{17}$ then $p =$

Options :

± 5

1. ✘

± 6

2. ✘

± 1

3. ✔

± 3

4. ✘

Question Number : 35 Question Id : 105615195 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

The mean deviation from the mean of the discrete data 1, 3, 4, 7, 11, 18, 29, 47, 78 is

Options :

22

1. ✖

24

2. ✖

$\frac{176}{9}$

3. ✔

$\frac{182}{9}$

4. ✖

Question Number : 36 Question Id : 105615196 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

When two dice are thrown, the probability of getting a prime number on one die and a composite number on the other is

Options :

$\frac{1}{3}$

1. ✔

$\frac{1}{4}$

2. ✖

$\frac{1}{2}$

3. ✖

$$\frac{1}{6}$$

4. ✖

Question Number : 37 Question Id : 105615197 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

Let A, B, C be three pairwise independent events of a random experiment. If

$$P(\overline{B} \cup \overline{C}) = \frac{1}{2}, P(A) > 0, P(B) = b \text{ and } P(C) = c, \text{ then } P((\overline{B} \cap \overline{C}) | A) =$$

Options :

$$1 + b - c$$

1. ✖

$$2 + b - c$$

2. ✖

$$\frac{3}{2} - b - c$$

3. ✔

$$2 - b - c$$

4. ✖

Question Number : 38 Question Id : 105615198 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

Two dice are thrown and the sum of the numbers appearing on the dice is observed to be a multiple of 4. If p is the conditional probability that number 4 has appeared atleast once, then $3p + 2 =$

Options :

$$\frac{25}{12}$$

1. ✖

$$\frac{1}{6}$$

2. ✘

$$\frac{7}{3}$$

3. ✔

$$\frac{5}{2}$$

4. ✘

Question Number : 39 Question Id : 105615199 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

In a random experiment of throwing 5 coins, the number of heads is defined as a random variable. The mean of the random variable is

Options :

$$\frac{2}{3}$$

1. ✘

$$\frac{3}{2}$$

2. ✘

$$\frac{7}{9}$$

3. ✘

$$\frac{5}{2}$$

4. ✔

Question Number : 40 Question Id : 105615200 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

The variance of a Poisson variate X is 2. Then $P(X \geq 3) =$

Options :

$$\frac{e^2 - 7}{e^2}$$

1. ✖

$$\frac{e^2 - 3}{e^2}$$

2. ✖

$$\frac{e^2 - 5}{e^2}$$

3. ✔

$$1 - \frac{4}{e^2}$$

4. ✖

Question Number : 41 Question Id : 105615201 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If the perimeter of a triangle is 20 and two of its vertices are $(-5, 0)$ and $(6, 0)$, then the locus of the third vertex is

Options :

$$40x^2 - 81y^2 - 40x - 800 = 0$$

1. ✔

$$40x^2 + 9y^2 - 25x + 800 = 0$$

2. ✖

$$40x^2 - 9y^2 = 800$$

3. ✖

$$5x^2 - 3y^2 + 3x - 4y + 25 = 0$$

4. ✖

Question Number : 42 Question Id : 105615202 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

The transformed equation of $3x^2 + 4xy + y^2 - 8x - 4y - 4 = 0$ is

$f(X,Y) = aX^2 + 2hXY + bY^2 + c = 0$ when the origin is shifted to a new point by the translation of axes. Then $f(1,1) =$

Options :

0

1. ✔

1

2. ✖

-1

3. ✖

-8

4. ✖

Question Number : 43 Question Id : 105615203 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If the line $2x - 3y + 4 = 0$ divides the line segment joining the points $A(-2, 3)$ and $B(3, -2)$ in the ratio $m:n$, then the point which divides AB in the ratio $-4m:3n$ is

Options :

$$(-17, 18)$$

1. ✓

$$\left(-\frac{59}{7}, \frac{66}{7}\right)$$

2. ✘

$$(-5, 6)$$

3. ✘

$$\left(-\frac{5}{7}, \frac{12}{7}\right)$$

4. ✘

Question Number : 44 Question Id : 105615204 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If the lines $L_1 \equiv 2x + y + 3 = 0$, $L_2 \equiv kx + 2y - 3 = 0$ and $L_3 \equiv 3x - 2y + 1 = 0$ are concurrent then the cosine of the acute angle between the lines $L_2 = 0$ and $2x - 5y + 7 = 0$ is

Options :

$$\frac{1}{\sqrt{2}}$$

1. ✘

$$\left(\frac{15}{2\sqrt{29}}\right)$$

2. ✘

$$\left(\frac{25}{29}\right)$$

3. ✘

$$\left(\frac{20}{29}\right)$$

4. ✓

Question Number : 45 Question Id : 105615205 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If Q is the image of the point P(1,1) with respect to the straight line $x + y + 1 = 0$, then the length of the perpendicular drawn from Q to the line $3x - 4y + 3 = 0$ is

Options :

$$\frac{5}{2}$$

1. ✘

$$2$$

2. ✘

$$1$$

3. ✓

$$\frac{1}{2}$$

4. ✘

Question Number : 46 Question Id : 105615206 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

The centroid of the triangle formed by the lines $x - 3y + 3 = 0$, $x + 3y + 3 = 0$, $x + y - 1 = 0$ is

Options :

$$\left(0, \frac{-1}{3}\right)$$

1. ✓

$$\left(\frac{2}{3}, -1\right)$$

2. ✖

$$\left(\frac{-1}{3}, 1\right)$$

3. ✖

$$\left(1, \frac{-1}{3}\right)$$

4. ✖

Question Number : 47 Question Id : 105615207 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If the slope of one of the lines represented by $5x^2 + \frac{40}{3}xy + ky^2 = 0$ is 3, then the angle between the pair of lines is

Options :

$$0^\circ$$

1. ✖

$$\frac{\pi}{4}$$

2. ✖

$$\frac{\pi}{3}$$

3. ✖

$$\frac{\pi}{2}$$

4. ✔

Question Number : 48 Question Id : 105615208 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0

Correct Marks : 1 Wrong Marks : 0

If a line L is common to the pairs of lines $6x^2 - xy - 12y^2 = 0$ and $15x^2 + 14xy - 8y^2 = 0$, then the combined equation the other two lines is

Options :

$$10x^2 - 19xy + 6y^2 = 0$$

1. ✓

$$5x^2 - 4xy + 7y^2 = 0$$

2. ✗

$$x^2 - 9xy + y^2 = 0$$

3. ✗

$$3x^2 + 6xy + 11y^2 = 0$$

4. ✗

Question Number : 49 Question Id : 105615209 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If L is a line passing through the point $(-1,1)$ and parallel to the common line of the pairs of lines $6x^2 - xy - 12y^2 = 0$ and $15x^2 + 14xy - 8y^2 = 0$, then the equation of pair of lines joining the origin to the points of intersection of the curve $2x^2 - xy - y^2 + x - y = 0$ and the line L is

Options :

$$x^2 - xy - y^2 = 0$$

1. ✗

$$x^2 + xy - y^2 = 0$$

2. ✗

$$x^2 - y^2 = 0$$

3. ✓

$$2x^2 + 3xy - 6y^2 = 0$$

4. ✘

Question Number : 50 Question Id : 105615210 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

From a point A(0, 3) on the circle $(x+2)^2 + (y-3)^2 = 4$, a chord AB is drawn and it is extended to a point Q such that $AQ = 2AB$. Then the locus of Q is

Options :

$$(x+4)^2 + (y-3)^2 = 16$$

1. ✓

$$(x+1)^2 + (y-3)^2 = 32$$

2. ✘

$$(x+1)^2 + (y-3)^2 = 4$$

3. ✘

$$(x+1)^2 + (y-3)^2 = 1$$

4. ✘

Question Number : 51 Question Id : 105615211 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If m_1, m_2 are the slopes of the tangents drawn from a point $(1, -3)$ to the circle $x^2 + y^2 - 6x + 4y + 12 = 0$ then $9(m_1^2 + m_2^2) =$

Options :

16

1. ✓

25

2. ✘

4

3. ✘

1

4. ✘

Question Number : 52 Question Id : 105615212 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If A, B are the points of contact of the tangents drawn from the point $P(-2, -3)$ to the circle $x^2 + y^2 - 8x - 10y + 5 = 0$ and the chord AB subtends an angle θ at P then $\tan \theta =$

Options :

$\frac{3}{4}$

1. ✘

$\frac{24}{7}$

2. ✓

$\frac{7}{24}$

3. ✘

$\frac{4}{3}$

4. ✘

Question Number : 53 Question Id : 105615213 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

The equation of the transverse common tangent of the circles $x^2 + y^2 - 6x - 8y + 9 = 0$ and $x^2 + y^2 + 2x - 2y + 1 = 0$ is

Options :

$$4x + 3y - 4 = 0$$

1. ✓

$$3x + y - 1 = 0$$

2. ✗

$$2x - y + 2 = 0$$

3. ✗

$$x + 2y - 3 = 0$$

4. ✗

Question Number : 54 Question Id : 105615214 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If θ is the angle between the circles $x^2 + y^2 - 2x - 4y - 4 = 0$ and $x^2 + y^2 - 8x - 12y + 43 = 0$ then $|7 \sec \theta - 18 \cos \theta| =$

Options :

11

1. ✓

9

2. ✗

0

3. ✖

1

4. ✖

Question Number : 55 Question Id : 105615215 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If $(0, \frac{3}{4})$ is the radical centre of the circles $S \equiv x^2 + y^2 + \alpha x + 6y = 0$, $S' \equiv x^2 + y^2 + 2\alpha x + \alpha y + 6 = 0$ and $S'' \equiv x^2 + y^2 + 6\alpha x - \alpha y + 3 = 0$ then the distance between the radical centre and the centre of the circle $S' = 0$ is

Options :

8

1. ✖

15

2. ✖

$\frac{\sqrt{65}}{4}$

3. ✔

$\frac{\sqrt{5}}{4}$

4. ✖

Question Number : 56 Question Id : 105615216 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

The vertex and the focus of the parabola $2x^2 + 5y - 6x + 1 = 0$ respectively, are

Options :

$$\left(\frac{-3}{2}, \frac{7}{10}\right), \left(\frac{-3}{2}, \frac{53}{40}\right)$$

1. ✖

$$\left(\frac{-3}{2}, \frac{7}{10}\right), \left(\frac{-3}{2}, \frac{3}{40}\right)$$

2. ✖

$$\left(\frac{3}{2}, \frac{7}{10}\right), \left(\frac{3}{2}, \frac{53}{40}\right)$$

3. ✖

$$\left(\frac{3}{2}, \frac{7}{10}\right), \left(\frac{3}{2}, \frac{3}{40}\right)$$

4. ✔

Question Number : 57 Question Id : 105615217 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

The axis of a parabola is along the line $y = x$ and the distance of its vertex A from $(0, 0)$ is $\sqrt{2}$ and that of its focus S from $(0, 0)$ is $2\sqrt{2}$. If A and S lie in first quadrant, then the equation of the parabola in parametric form is

Options :

$$x = (t+1)^2, y = (t-1)^2$$

1. ✔

$$x = t^2, y = 2t$$

2. ✖

$$x = (t - \sqrt{2})^2, y = (t + \sqrt{2})^2$$

3. ✖

$$x = t^2 + 5, y = t^2 - 5$$

4. ✖

Question Number : 58 Question Id : 105615218 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

Let $S \equiv \frac{x^2}{a^2} + \frac{y^2}{b^2} - 1 = 0$, $S' \equiv \frac{x^2}{\alpha^2} + \frac{y^2}{\beta^2} - 1 = 0$ be two intersecting ellipses. If

$P(a \cos \theta, b \sin \theta)$ and $Q\left(a \cos\left(\frac{\pi}{2} + \theta\right), b \sin\left(\frac{\pi}{2} + \theta\right)\right)$ are their points of

intersection then $\frac{1}{2}(a^2 \beta^2 + b^2 \alpha^2) =$

Options :

$$a^2 b^2$$

1. ✖

$$\alpha^2 + \beta^2$$

2. ✖

$$a^2 + b^2$$

3. ✖

$$\alpha^2 \beta^2$$

4. ✔

Question Number : 59 Question Id : 105615219 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

$P(\theta_1)$ and $Q(\theta_2)$ are two points on the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ with eccentricity e . If PSQ is a focal chord and $\tan\left(\frac{\theta_1}{2}\right)\tan\left(\frac{\theta_2}{2}\right) = -(2\sqrt{2} + 3)$, then e and S are

Options :

$$\frac{1}{\sqrt{3}}, \left(\frac{a}{\sqrt{3}}, 0\right)$$

1. ✖

$$\frac{1}{\sqrt{3}}, \left(\frac{-a}{\sqrt{3}}, 0\right)$$

2. ✖

$$\frac{1}{\sqrt{2}}, \left(\frac{a}{\sqrt{2}}, 0\right)$$

3. ✖

$$\frac{1}{\sqrt{2}}, \left(\frac{-a}{\sqrt{2}}, 0\right)$$

4. ✔

Question Number : 60 Question Id : 105615220 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

Let S be the focus of the hyperbola $\frac{x^2}{16} - \frac{y^2}{9} = 1$ lying on the positive X -axis and $P(5, y_1)$ be point on the hyperbola. Then $SP =$

Options :

$$\frac{1}{4}$$

1. ✖

$$\frac{3}{4}$$

2. ✖

$$\frac{9}{4}$$

3. ✔

$$\frac{5}{4}$$

4. ✖

Question Number : 61 Question Id : 105615221 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If $P(\theta) = \left(x_1, \frac{3\sqrt{5}}{2} \right)$, $0 < \theta < \frac{\pi}{2}$ is a point on the hyperbola $\frac{x^2}{25} - \frac{y^2}{9} = 1$, where θ is the parameter in its parametric form, then $2x_1 + 9 \sin^2 \theta =$

Options :

8

1. ✖

10

2. ✖

20

3. ✔

34

4. ✖

Question Number : 62 Question Id : 105615222 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If the points A(1, 3, 5), B(2, 4, 6), C(4, 5, k) form a right angled triangle then the number of possible values of k is

Options :

2

1. ✓

3

2. ✗

0

3. ✗

1

4. ✗

Question Number : 63 Question Id : 105615223 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

Let $A=(3,4,0)$, $B=(4,4,4)$, $C=(-6,2,3)$ and $D=(1,1,2)$. If θ is the acute angle between the lines AB and CD then $\cos \theta =$

Options :

$$\frac{4}{17\sqrt{3}}$$

1. ✗

$$\frac{3}{17\sqrt{3}}$$

2. ✓

$$\frac{12}{17\sqrt{3}}$$

3. ✗

$$\frac{11}{17\sqrt{3}}$$

4. ✖

Question Number : 64 Question Id : 105615224 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

A plane containing two lines whose direction ratios are $(-1, 2, 1)$ and $(1, 3, 2)$ passes through the point $(2, 1, k)$. If this plane also passes through the point $(3, -1, 4)$, then $k =$

Options :

1. ✓ 5

2. ✖ 3

3. ✖ 6

4. ✖ -3

Question Number : 65 Question Id : 105615225 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

Let $A = (a_{ij})$ be an $n \times n$ matrix defined by $a_{ij} = \begin{cases} k^i, & \forall i = j \\ 0, & \text{otherwise} \end{cases}$. If $m = \text{trace of } A$

and $\lim_{k \rightarrow 1} \frac{n-m}{1-k} = 171$ then the value of n is

Options :

18

1. ✓

23

2. ✘

35

3. ✘

42

4. ✘

Question Number : 66 Question Id : 105615226 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

$$\lim_{x \rightarrow \infty} x^3 \left[\sqrt{x^2 + \sqrt{x^4 + 1}} - \sqrt{2x} \right] =$$

Options :

0

1. ✘

1

2. ✘

$\frac{1}{4\sqrt{2}}$

3. ✓

$\frac{3}{2\sqrt{2}}$

4. ✘

Question Number : 67 Question Id : 105615227 Question Type : MCQ Option Shuffling : Yes Display Question Number :

Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0
Correct Marks : 1 Wrong Marks : 0

Let $f(x) = \begin{cases} 3-x & \text{if } x < -3 \\ 6 & \text{if } -3 \leq x \leq 3 \\ 3+x & \text{if } x > 3 \end{cases}$. Let α be the number of points of discontinuity of f and β be the number of points where f is not differentiable. Then $\alpha + \beta =$

Options :

6

1. ✘

3

2. ✘

2

3. ✔

0

4. ✘

Question Number : 68 Question Id : 105615228 Question Type : MCQ Option Shuffling : Yes Display Question Number :
Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0
Correct Marks : 1 Wrong Marks : 0

If $a f(x) + b f\left(\frac{1}{x}\right) = x + 1$, and $\frac{d}{dx}(x^2 f(x)) = 2x^2 + 2x + \frac{1}{3}$, then $a - b =$

Options :

2

1. ✘

3

2. ✔

0

3. ✖

1

4. ✖

Question Number : 69 Question Id : 105615229 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If $f(x) = \sin\left(\cosh\left(\frac{x^2+1}{x^2+2}\right)\right)$ then $f'(1) =$

Options :

$$\frac{2}{9} \sinh\left(\frac{2}{3}\right) \cos\left(\cosh\left(\frac{2}{3}\right)\right)$$

1. ✔

$$\sinh\left(\frac{2}{3}\right) \cos\left(\cosh\left(\frac{2}{3}\right)\right)$$

2. ✖

$$\frac{2}{9} \cos\left(\cosh\left(\frac{2}{3}\right)\right)$$

3. ✖

$$\frac{2}{9} \cosh\left(\frac{2}{3}\right) \cos\left(\sinh\left(\frac{2}{3}\right)\right)$$

4. ✖

Question Number : 70 Question Id : 105615230 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If an error of 0.02 sq.cm is found in the surface area of a sphere when its radius is measured as 10 cm, then the approximate error that occurs in the volume of the sphere, in cubic centimetres, is

Options :

0.2

1. ✘

0.01

2. ✘

0.3

3. ✘

0.1

4. ✔

Question Number : 71 Question Id : 105615231 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If θ is the angle between the curves $y^2 = 4x$ and $x^2 + y^2 = 5$ then $|\tan \theta| =$

Options :

5

1. ✘

4

2. ✘

3

3. ✔

2

4. ✖

Question Number : 72 Question Id : 105615232 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

The local maximum value of the function $f(x) = -(x-2)^3(x+2)^2$ is

Options :

0

1. ✖

$$\frac{12^3 \cdot 8^2}{5^5}$$

2. ✔

125

3. ✖

$$\frac{2^9 \cdot 3^2}{5^6}$$

4. ✖

Question Number : 73 Question Id : 105615233 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If $\int \frac{1 + \cos 8x}{\tan 2x - \cot 2x} dx = f(x) \cdot \cos(g(x)) + c$, then $f\left(\frac{1}{4}\right) + g\left(\frac{1}{4}\right) =$

Options :

2

1. ✖

$$\frac{17}{8}$$

2. ✖

$$\frac{15}{8}$$

3. ✖

$$\frac{33}{16}$$

4. ✔

Question Number : 74 Question Id : 105615234 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

$$\text{Let } x \neq \frac{-3}{5}, \frac{2}{5}, \text{ if } f\left(\frac{2x+1}{5x+3}\right) = x+2, \text{ then } \int f(x) dx =$$

Options :

$$\frac{7}{5}x - \frac{1}{5} \log|5x+3| + c$$

1. ✖

$$\frac{7}{5}x - \frac{1}{25} \log|5x+3| + c$$

2. ✖

$$\frac{7}{5}x - \frac{1}{25} \log|5x-2| + c$$

3. ✔

$$\frac{7}{5}x - \frac{1}{5} \log|5x-2| + c$$

4. ✖

Question Number : 75 Question Id : 105615235 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

$$\text{If } \int e^x \cos x \, dx = \frac{e^x}{2} (\cos x + \sin x) \text{ and } \int \frac{\cos\left(\log\left(\frac{2x+3}{3-2x}\right)\right)}{(3-2x)^2} dx = \frac{f(x)}{24} [\cos(g(x)) + \sin(g(x))] + c \text{ then } g(1) =$$

Options :

5

1. ✖

$\log f(2)$

2. ✖

$\log f(1)$

3. ✔

0

4. ✖

Question Number : 76 Question Id : 105615236 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

$$\int_1^2 x\sqrt{4-x^2} \, dx =$$

Options :

$\sqrt{3}$

1. ✔

2

2. ✖

$\frac{1}{\sqrt{3}}$

3. ✖

$\frac{1}{2}$

4. ✖

Question Number : 77 Question Id : 105615237 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

If $[x]$ denotes the greatest integer function of x and $\int_{-\frac{3}{2}}^{\frac{3}{2}} [2x - 3] dx = k$, then $\left|k + \frac{1}{2}\right| =$

Options :

7

1. ✖

8

2. ✖

10

3. ✔

12

4. ✖

Question Number : 78 Question Id : 105615238 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

The differential equation corresponding to the family of curves given by $ax^2 + by^2 = 1$ where a and b are arbitrary constants is

Options :

$$x \frac{d^2 y}{dx^2} = \frac{dy}{dx}$$

1. ✖

$$xy \frac{d^2 y}{dx^2} + x \left(\frac{dy}{dx} \right)^2 - y \frac{dy}{dx} = 0$$

2. ✔

$$xy \frac{d^2 y}{dx^2} + y \left(\frac{dy}{dx} \right)^2 - x \frac{dy}{dx} = 0$$

3. ✖

$$xy \frac{d^2 y}{dx^2} - x \left(\frac{dy}{dx} \right)^2 + y \frac{dy}{dx} = 0$$

4. ✖

Question Number : 79 Question Id : 105615239 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

For the differential equation $\sqrt{\frac{d^2 y}{dx^2}} = \sqrt[3]{\left[y \frac{dy}{dx} + x \sin \left(\frac{dy}{dx} \right) \right]^2}$

Options :

Order is 2 and degree is 3

1. ✖

Order is 3 and degree is 3

2. ✖

Order is 3 and degree is 2

3. ✖

Order is 2 and degree is not defined

4. ✔

Question Number : 80 Question Id : 105615240 Question Type : MCQ Option Shuffling : Yes Display Question Number : Yes Is Question Mandatory : No Calculator : None Response Time : N.A Think Time : N.A Minimum Instruction Time : 0 Correct Marks : 1 Wrong Marks : 0

The general solution of the differential equation $\frac{dy}{dx} = \frac{xy + x - 2y - 2}{xy - 2x + y - 2}$ is

Options :

$$x + y + 3 \log \left| \frac{x+1}{y+1} \right| = c$$

1. ✖

$$x + y + 3 \log \left| \frac{y+1}{x+1} \right| = c$$

2. ✖

$$x - y + 3 \log \left| \frac{x+1}{y+1} \right| = c$$

3. ✖

$$x - y + 3 \log \left| \frac{y+1}{x+1} \right| = c$$

4. ✔