



Series WX1YZ/4



SET ~ 3

प्रश्न-पत्र कोड  
Q.P. Code

30/4/3

रोल नं.  
Roll No.

1	4	1	2	5	1	1	8
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परीक्षार्थी प्रश्न-पत्र कोड को उत्तर-पुस्तिका के मुख-पृष्ठ पर अवश्य लिखें।  
Candidates must write the Q.P. Code on the title page of the answer-book.

## गणित (मानक) - सैद्धान्तिक MATHEMATICS (STANDARD) - Theory

#

निर्धारित समय : 3 घण्टे  
Time allowed : 3 hours

अधिकतम अंक : 80  
Maximum Marks : 80

नोट / NOTE :

- कृपया जाँच कर लें कि इस प्रश्न-पत्र में मुद्रित पृष्ठ 15 हैं।  
*Please check that this question paper contains 15 printed pages.*
- प्रश्न-पत्र में दाहिने हाथ की ओर दिए गए प्रश्न-पत्र कोड को छात्र उत्तर-पुस्तिका के मुख-पृष्ठ पर लिखें।  
*Q.P. Code given on the right hand side of the question paper should be written on the title page of the answer-book by the candidate.*
- कृपया जाँच कर लें कि इस प्रश्न-पत्र में 38 प्रश्न हैं।  
*Please check that this question paper contains 38 questions.*
- कृपया प्रश्न का उत्तर लिखना शुरू करने से पहले, उत्तर-पुस्तिका में प्रश्न का क्रमांक अवश्य लिखें।  
*Please write down the Serial Number of the question in the answer-book before attempting it.*
- इस प्रश्न-पत्र को पढ़ने के लिए 15 मिनट का समय दिया गया है। प्रश्न-पत्र का वितरण पूर्वाह्न में 10.15 बजे किया जाएगा। 10.15 बजे से 10.30 बजे तक छात्र केवल प्रश्न-पत्र को पढ़ेंगे और इस अवधि के दौरान वे उत्तर-पुस्तिका पर कोई उत्तर नहीं लिखेंगे।  
*15 minute time has been allotted to read this question paper. The question paper will be distributed at 10.15 a.m. From 10.15 a.m. to 10.30 a.m., the students will read the question paper only and will not write any answer on the answer-book during this period.*

### GENERAL INSTRUCTIONS :

Read the following instructions carefully and follow them :

- (i) This question paper contains 38 questions. All questions are compulsory.
- (ii) Question paper is divided into FIVE sections – Section A, B, C, D and E.
- (iii) In section A – question number 1 to 18 are multiple choice questions (MCQs) and question number 19 and 20 are Assertion-Reason based questions of 1 mark each.
- (iv) In section B – question number 21 to 25 are Very Short Answer (VSA) type questions of 2 marks each.
- (v) In section C – question number 26 to 31 are Short Answer (SA) type questions carrying 3 marks each.
- (vi) In section D – question number 32 to 35 are Long Answer (LA) type questions carrying 5 marks each.
- (vii) In section E – question number 36 to 38 are case based integrated units of assessment questions carrying 4 marks each. Internal choice is provided in 2 marks question in each case-study.
- (viii) There is no overall choice. However, an internal choice has been provided in 2 questions in Section B, 2 questions in Section C, 2 questions in Section D and 3 questions in Section E.
- (ix) Draw neat figures wherever required. Take  $\pi = 22/7$  wherever required if not stated.
- (x) Use of calculators is **NOT** allowed.

### SECTION - A

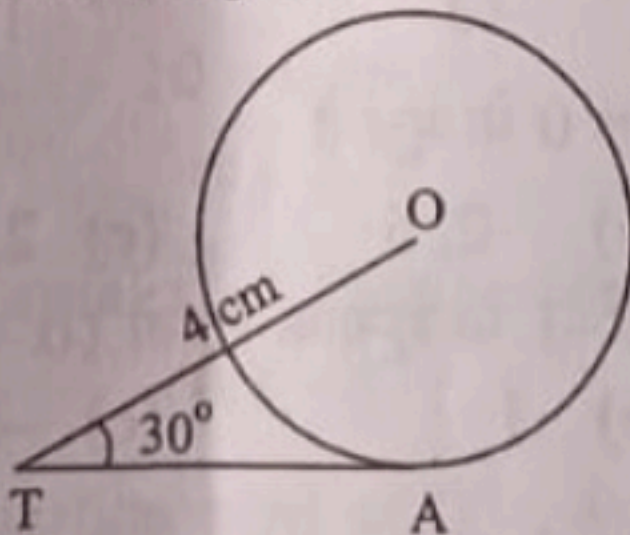
Section - A consists of Multiple Choice type questions of 1 mark each.

1. The pair of linear equations  $2x = 5y + 6$  and  $15y = 6x - 18$  represents two lines which are :

- (a) intersecting (b) parallel  
(c) coincident (d) either intersecting or parallel

2. In the given figure, TA is a tangent to the circle with centre O such that  $OT = 4$  cm,  $\angle OTA = 30^\circ$ , then length of TA is :

- (a)  $2\sqrt{3}$  cm  
(b) 2 cm  
(c)  $2\sqrt{2}$  cm  
(d)  $\sqrt{3}$  cm



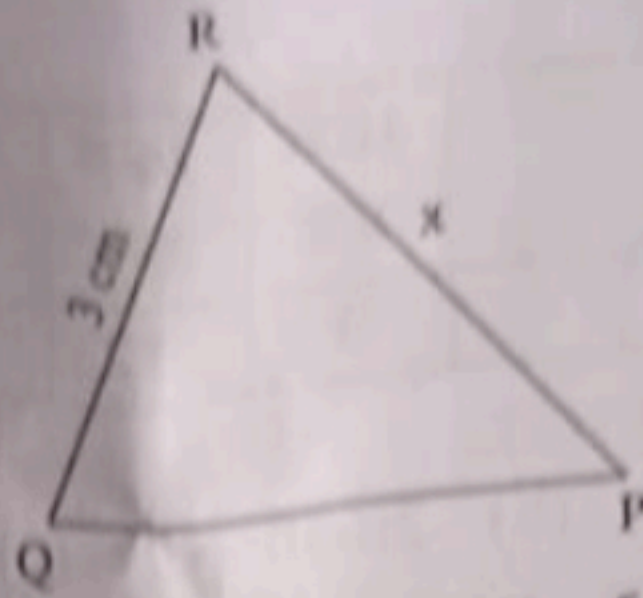
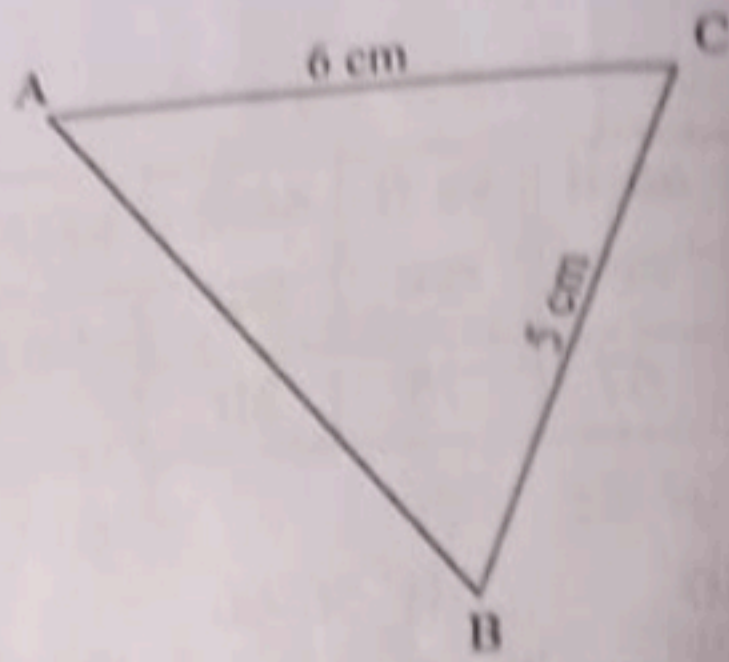
3. The ratio of HCF to LCM of the least composite number and the least prime number is :

- (a) 1:2 (b) 2:1 (c) 1:1 (d) 1:3

4. If a pole 6 m high casts a shadow  $2\sqrt{3}$  m long on the ground, then sun's elevation is :

- (a)  $60^\circ$  (b)  $45^\circ$  (c)  $30^\circ$  (d)  $90^\circ$





In the given figure,  $\Delta ABC \sim \Delta QPR$ . If  $AC = 6$  cm,  $BC = 5$  cm,  $QR = 3$  cm and  $PR = x$ ; then the value of  $x$  is :

- (a) 3.6 cm      (b) 2.5 cm      (c) 10 cm      (d) 3.2 cm

The distance of the point  $(-6, 8)$  from origin is :

- (a) 6      (b) -6      (c) 8      (d) 10

The next term of the A.P. :  $\sqrt{7}, \sqrt{28}, \sqrt{63}$  is :

- (a)  $\sqrt{70}$       (b)  $\sqrt{80}$       (c)  $\sqrt{97}$       (d)  $\sqrt{112}$

$(\sec^2 \theta - 1)(\operatorname{cosec}^2 \theta - 1)$  is equal to :

- (a) -1      (b) 1      (c) 0      (d) 2

Two dice are thrown together. The probability of getting the difference of numbers on their upper faces equals to 3 is :

- (a)  $\frac{1}{9}$       (b)  $\frac{2}{9}$       (c)  $\frac{1}{6}$       (d)  $\frac{1}{12}$

A card is drawn at random from a well-shuffled pack of 52 cards. The probability that the card drawn is not an ace is :

- (a)  $\frac{1}{13}$       (b)  $\frac{9}{13}$       (c)  $\frac{4}{13}$       (d)  $\frac{12}{13}$

The roots of the equation  $x^2 + 3x - 10 = 0$  are :

- (a) 2, -5      (b) -2, 5      (c) 2, 5      (d) -2, -5

If  $\alpha, \beta$  are zeroes of the polynomial  $x^2 - 1$ , then value of  $(\alpha + \beta)$  is :

- (a) 2      (b) 1      (c) -1      (d) 0

If  $\alpha, \beta$  are the zeroes of the polynomial  $p(x) = 4x^2 - 3x - 7$ , then

$\left(\frac{1}{\alpha} + \frac{1}{\beta}\right)$  is equal to :

- (a)  $\frac{7}{3}$       (b)  $\frac{-7}{3}$       (c)  $\frac{3}{7}$       (d)  $\frac{-3}{7}$

What is the area of a semi-circle of diameter 'd' ?

- (a)  $\frac{1}{16}\pi d^2$       (b)  $\frac{1}{4}\pi d^2$       (c)  $\frac{1}{8}\pi d^2$       (d)  $\frac{1}{2}\pi d^2$



15. For the following distribution :

Marks Below	10	20	30	40	50	60
Number of Students	3	12	27	57	75	80

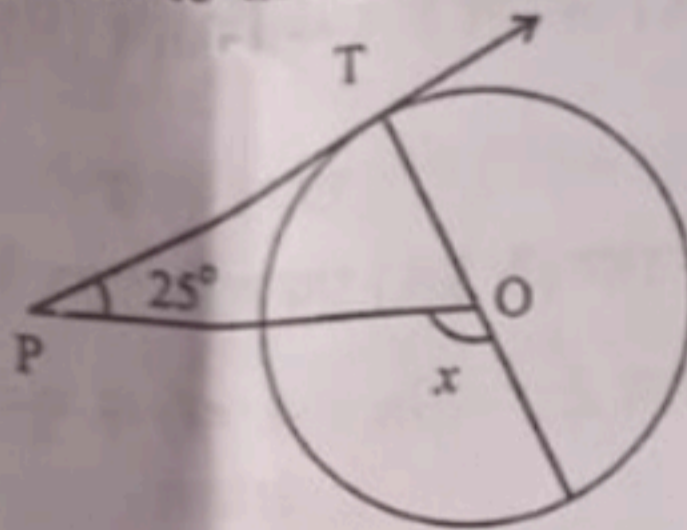
The modal class is :

- (a) 10-20      (b) 20-30      (c) 30-40      (d) 50-60

1

16. In the given figure, PT is a tangent at T to the circle with centre O. If  $\angle TPO = 25^\circ$ , then  $x$  is equal to :

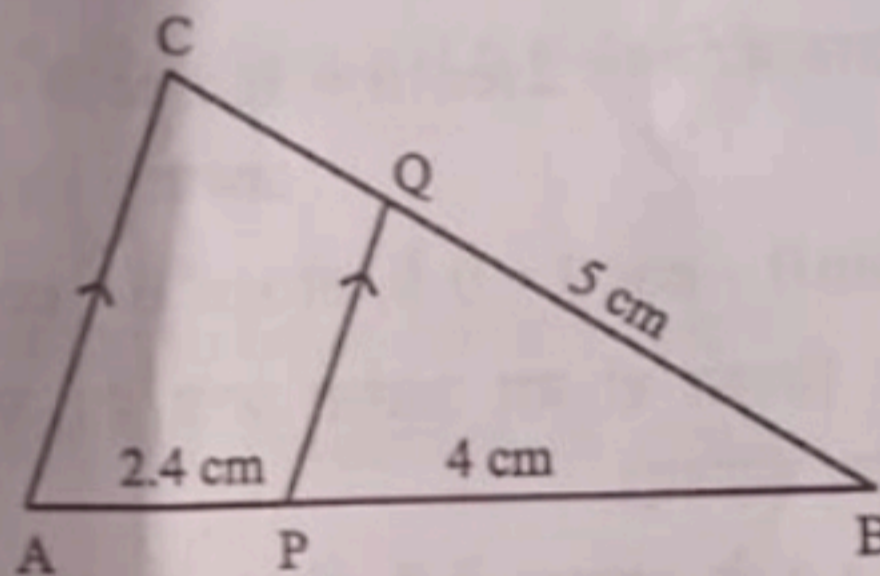
- (a)  $25^\circ$   
 (b)  $65^\circ$   
 (c)  $90^\circ$   
 (d)  $115^\circ$



1

17. In the given figure,  $PQ \parallel AC$ . If  $BP = 4$  cm,  $AP = 2.4$  cm and  $BQ = 5$  cm, then length of  $BC$  is :

- (a) 8 cm  
 (b) 3 cm  
 (c) 0.3 cm  
 (d)  $\frac{25}{3}$  cm



1

18. The points  $(-4, 0)$ ,  $(4, 0)$  and  $(0, 3)$  are the vertices of a :

- (a) right triangle      (b) isosceles triangle  
 (c) equilateral triangle      (d) scalene triangle

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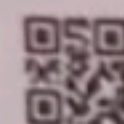
**DIRECTIONS :** In the question number 19 and 20, a statement of Assertion (A) is followed by a statement of Reason (R). Choose the correct option out of the following :

19. Assertion (A) : The probability that a leap year has 53 Sundays is  $\frac{2}{7}$ .

Reason (R) : The probability that a non-leap year has 53 Sundays is  $\frac{5}{7}$ .

1

- (a) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).  
 (b) Both Assertion (A) and Reason (R) are true and Reason (R) is not the correct explanation of Assertion (A).  
 (c) Assertion (A) is true but Reason (R) is false.  
 (d) Assertion (A) is false but Reason (R) is true.



20. Assertion (A) : a, b, c are in A.P. if and only if  $2b = a + c$ .  
Reason (R) : The sum of first n odd natural numbers is  $n^2$ . 1
- (a) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).  
(b) Both Assertion (A) and Reason (R) are true and Reason (R) is not the correct explanation of Assertion (A).  
(c) Assertion (A) is true but Reason (R) is false.  
(d) Assertion (A) is false but Reason (R) is true.

### SECTION - B

Section - B consists of Very Short Answer (VSA) type questions of 2 marks each.

21. (A) Find the sum and product of the roots of the quadratic equation  $2x^2 - 9x + 4 = 0$ . 2

OR

- (B) Find the discriminant of the quadratic equation  $4x^2 - 5 = 0$  and hence comment on the nature of roots of the equation. 2

22. (A) Evaluate  $2\sec^2\theta + 3\operatorname{cosec}^2\theta - 2\sin\theta\cos\theta$  if  $\theta = 45^\circ$ . 2

OR

- (B) If  $\sin\theta - \cos\theta = 0$ , then find the value of  $\sin^4\theta + \cos^4\theta$ . 2

23. If a fair coin is tossed twice, find the probability of getting 'atmost one head'. 2

24. Two numbers are in the ratio 2 : 3 and their LCM is 180. What is the HCF of these numbers? 2

25. If one zero of the polynomial  $p(x) = 6x^2 + 37x - (k - 2)$  is reciprocal of the other, then find the value of k. 2

### SECTION - C

Section - C consists of Short Answer (SA) type questions of 3 marks each.

26. Find the value of 'p' for which one root of the quadratic equation  $px^2 - 14x + 8 = 0$  is 6 times the other. 3

27. From an external point, two tangents are drawn to a circle. Prove that the line joining the external point to the centre of the circle bisects the angle between the two tangents. 3

28. Two concentric circles are of radii 5 cm and 3 cm. Find the length of the chord of the larger circle which touches the smaller circle. 3

29. (A) How many terms are there in A.P. whose first and fifth term are -14 and 2, respectively and the last term is 62. 3



(B) Which term of the A.P. : 65, 61, 57, 53, ..... is the first negative term ? 3

30. (A) Prove that  $\frac{\sin A - 2 \sin^3 A}{2 \cos^3 A - \cos A} = \tan A$  3

(B) Prove that  $\sec A (1 - \sin A) (\sec A + \tan A) = 1$ . 3

31. Prove that  $\sqrt{5}$  is an irrational number. 3

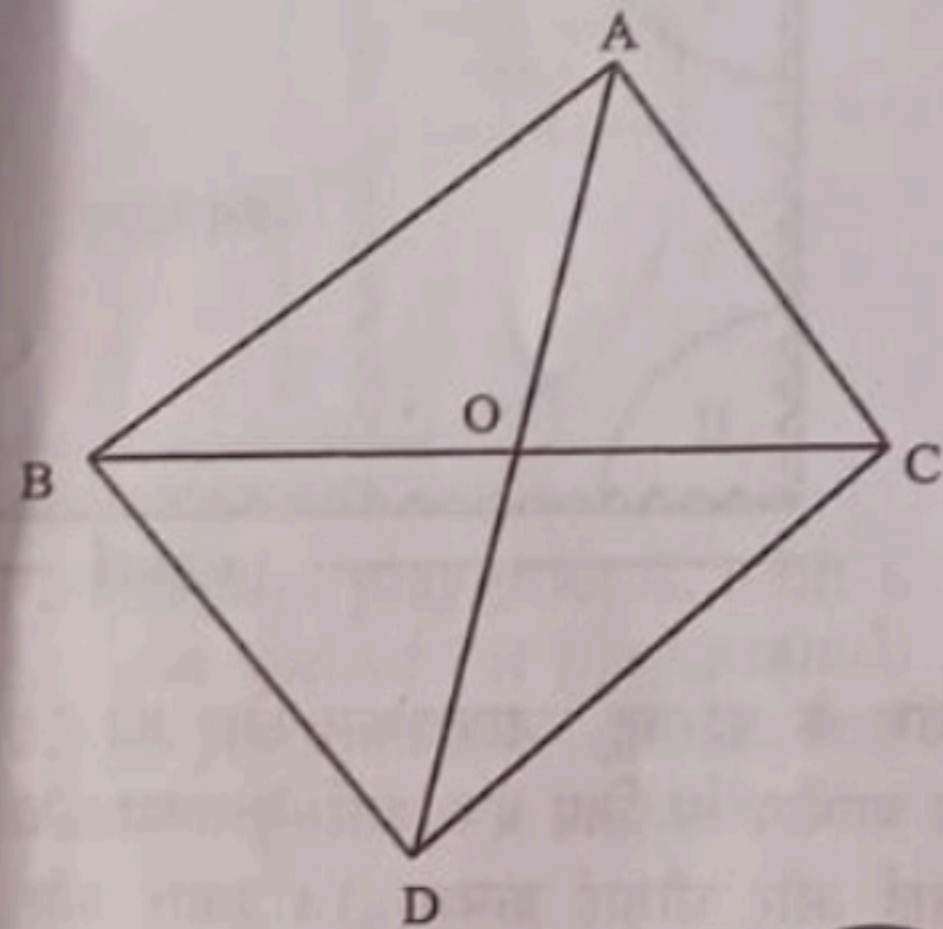
**SECTION - D**

Section - D consists of Long Answer (LA) type questions of 5 marks each.

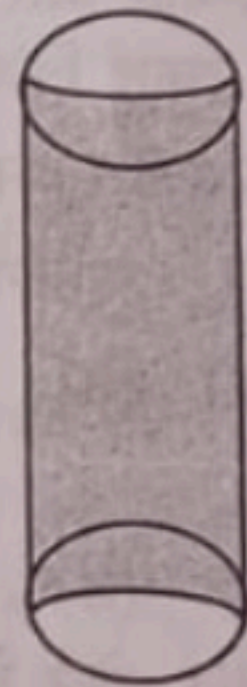
32. (A) In a  $\Delta PQR$ , N is a point on PR, such that  $QN \perp PR$ . If  $PN \times NR = QN^2$ , prove that  $\angle PQR = 90^\circ$ . 5

OR

(B) In the given figure,  $\Delta ABC$  and  $\Delta DBC$  are on the same base BC. If AD intersects BC at O, prove that  $\frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta DBC)} = \frac{AO}{DO}$



33. A wooden article was made by scooping out a hemisphere from each end of a solid cylinder, as shown in the figure. If the height of the cylinder is 10 cm and its base is of radius 3.5 cm, find the total surface area of the article. 5



34. The monthly expenditure on milk in 200 families of a Housing Society is given below :

Monthly Expenditure (in ₹)	1000-1500	1500-2000	2000-2500	2500-3000	3000-3500	3500-4000	4000-4500	4500-5000
Number of families	24	40	33	x	30	22	16	7

Find the value of x and also, find the median and mean expenditure on milk. 5



35. (A) A straight highway leads to the foot of a tower. A man standing on the top of the 75 m high tower observes two cars at angles of depression of  $30^\circ$  and  $60^\circ$ , which are approaching the foot of the tower. If one car is exactly behind the other on the same side of the tower, find the distance between the two cars. (use  $\sqrt{3} = 1.73$ )

5

OR

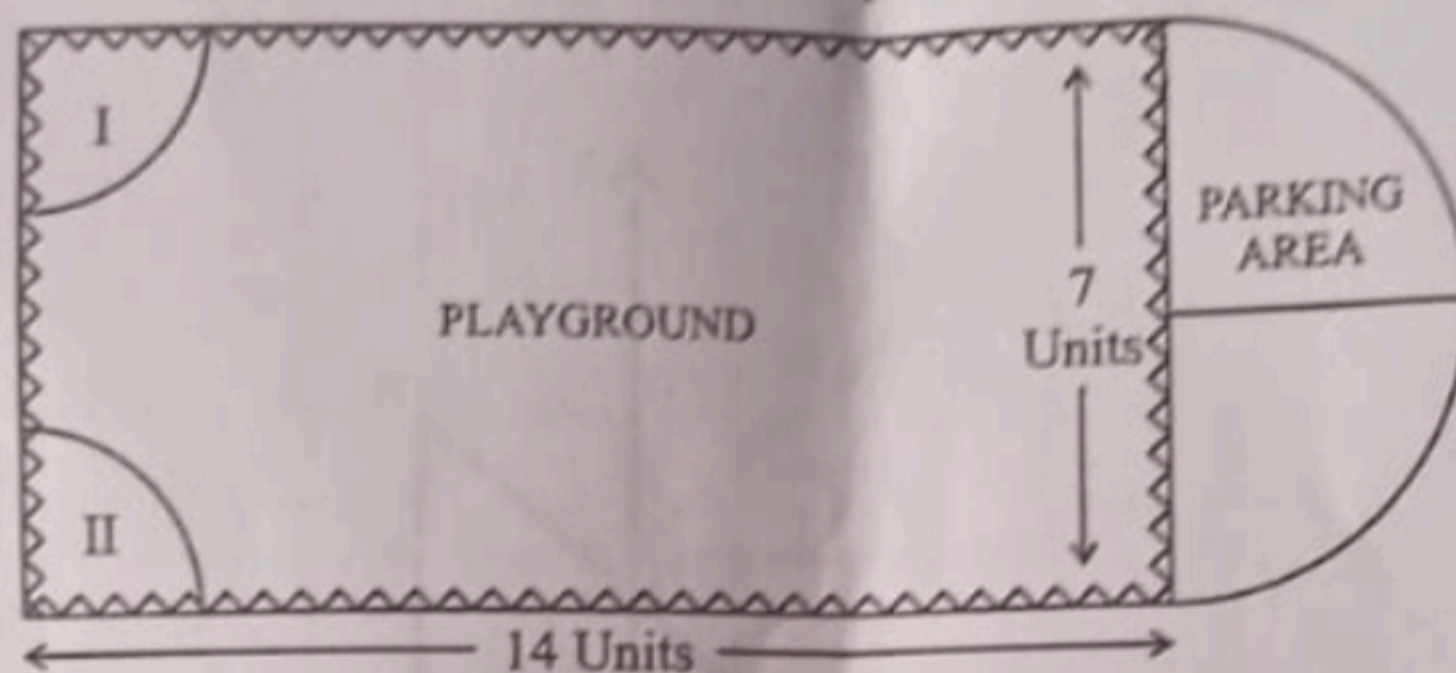
- (B) From the top of a 7 m high building, the angle of elevation of the top of a cable tower is  $60^\circ$  and the angle of depression of its foot is  $30^\circ$ . Determine the height of the tower.

5

### SECTION - E

Section - E consists of three Case Study Based questions of 4 marks each.

36. Governing council of a local public development authority of Dehradun decided to build an adventurous playground on the top of a hill, which will have adequate space for parking.



After survey, it was decided to build rectangular playground, with a semi-circular area allotted for parking at one end of the playground. The length and breadth of the rectangular playground are 14 units and 7 units, respectively. There are two quadrants of radius 2 units on one side for special seats.

Based on the above information, answer the following questions :

- (i) What is the total perimeter of the parking area ?
- (ii) (a) What is the total area of parking and the two quadrants ?

1

2

OR

- (b) What is the ratio of area of playground to the area of parking area ?
- (iii) Find the cost of fencing the playground and parking area at the rate of ₹ 2 per unit.

2

1

37. Two schools 'P' and 'Q' decided to award prizes to their students for two games of Hockey ₹  $x$  per student and Cricket ₹  $y$  per student. School 'P' decided to award a total of ₹ 9,500 for the two games to 5 and 4 students respectively; while school 'Q' decided to award ₹ 7,370 for the two games to 4 and 3 students respectively.

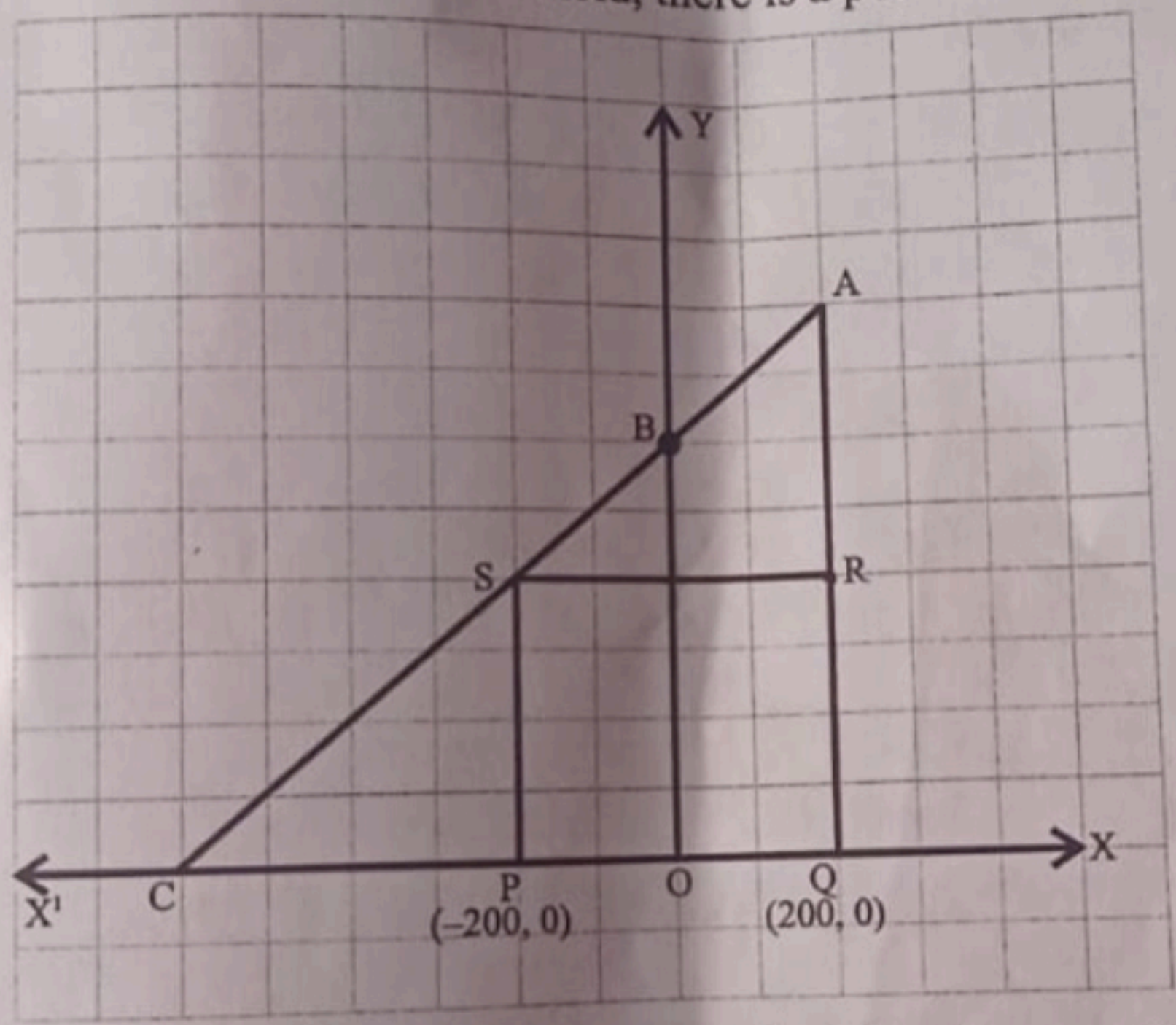


- Based on the given information, answer the following questions :
- (i) Represent the following information algebraically (in terms of  $x$  and  $y$ ). 1
  - (ii) (a) What is the prize amount for hockey ? 2

**OR**

- (b) Prize amount on which game is more and by how much ? 2
- (iii) What will be the total prize amount if there are 2 students each from two games ? 1

38. Jagdish has a field which is in the shape of a right angled triangle AQC. He wants to leave a space in the form of a square PQRS inside the field for growing wheat and the remaining for growing vegetables (as shown in the figure). In the field, there is a pole marked as O.



Based on the above information, answer the following questions :

- (i) Taking O as origin, coordinates of P are  $(-200, 0)$  and of Q are  $(200, 0)$ . PQRS being a square, what are the coordinates of R and S ? 1
- (ii) (a) What is the area of square PQRS ? 2

**OR**

- (b) What is the length of diagonal PR in square PQRS ? 2
- (iii) If S divides CA in the ratio  $K:1$ , what is the value of K, where point A is  $(200, 800)$  ? 1

