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JEE

(Main)

PAPER-1 (B.E./B. TECH.)

2022

COMPUTER BASED TEST (CBT)

Memory Based Questions & Solutions

Date: 28 July, 2022 (SHIFT-2) | TIME : (3.00 p.m. to 06.00 p.m)

Duration: 3 Hours | Max. Marks: 300

SUBJECT: MATHEMATICS

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PART : MATHEMATICS

1. If $f(x) = ax^2 + bx + c$ is a quadratic expression with $f(1) = 3$, $f(-2) = \lambda$, $f(3) = 4$ and $f(0) + f(1) + f(2) + f(3) = 14$, then the value of λ is
- (1) -4 (2) 4 (3) $2/3$ (4) $3/2$
- Ans.** (2)
- Sol.** $f(1) = 3 \Rightarrow a + b + c = 3$ (1)
 $f(3) = 4 \Rightarrow 9a + 3b + c = 4$ (2)
 $f(0) = c$

$$\text{Since } f(1) + f(-1) + f(2) + f(-2) = 14$$

$$c + 3 + 4a - 2b + c + 4 = 14$$

$$\Rightarrow 4a - 2b + 2c = 7 \dots\dots(3)$$

$$\text{By solving (1), (2) and (3) } a = \frac{1}{6}, b = -\frac{1}{6} \text{ \& } c = 3$$

$$\Rightarrow f(x) = \frac{1}{6}x^2 - \frac{1}{6}x + 3$$

$$\lambda = f(-2) = 4$$

2. The value of $60 \int_0^{\pi/2} \frac{\sin 6x}{\sin x} dx$ is

(1) 101

(2) 104

(3) 105

(4) 109

Ans. (2)

Sol. $I = \int_0^{\pi/2} \frac{\sin 6x}{\sin x} dx$

$$= \int_0^{\pi/2} \left(\frac{3 \sin 2x - 4 \sin^3 2x}{\sin x} \right) dx$$

$$= \int_0^{\pi/2} \{6 \cos x - 4(2 \cos x)^3 \cdot \sin^2 x\} dx$$

$$= \int_0^{\pi/2} (6 \cos x - 32 \sin^2 x \cos^3 x) dx$$

$$= 6 \sin x \Big|_0^{\pi/2} - 32 \int_0^{\pi/2} \sin^2 x (1 - \sin^2 x) \cos x dx$$

$$= 6 - 32 \left[\frac{\sin^3 x}{3} - \frac{\sin^5 x}{5} \right]_0^{\pi/2}$$

$$= 6 - 32 \left(\frac{1}{3} - \frac{1}{5} \right) = \frac{26}{15}$$

So $60 \int_0^{\pi/2} \frac{\sin 6x}{\sin x} dx = 60 \times \frac{26}{15} = 104$

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3. If $1 + (2 + {}^{49}C_1 + {}^{49}C_2 + \dots + {}^{49}C_{49}) ({}^{50}C_2 + {}^{50}C_4 + {}^{50}C_6 + \dots + {}^{50}C_{50}) = m \cdot 2^n$ then value of $m + n$ is

Ans. (99)

Sol. $1 + (2 + 2^{49} - 1)(2^{49} - 1) = m \cdot 2^n$
 $\Rightarrow 1 + (2^{49} + 1)(2^{49} - 1) = m \cdot 2^n$
 $\Rightarrow 1 + 2^{98} - 1 = m \cdot 2^n$
 $\Rightarrow m = 1, n = 98$ so $m + n = 99$

4. The differential equation of all the circles passing through the points (0, 2) and (0, -2) ; is

(1) $2xyy' + (x^2 + y^2 + 4) = 0$

(2) $2xyy' + (x^2 - y^2 + 4) = 0$

(3) $2xyy' + (-x^2 + y^2 + 4) = 0$

(4) $2xyy' + (x^2 + y^2 - 4) = 0$

Ans. (2)

Sol. $(x^2 + y^2 - 4) + \lambda x = 0 \dots\dots(i)$

where λ is parameter.

Now differentiate equation (i) with respect to x , we get

$$\lambda = -2(x + yy') \dots\dots(ii)$$

from (i) and (ii)

$$(x^2 + y^2 - 4) - 2(x + yy')x = 0$$

$$\Rightarrow y^2 - x^2 - 4 - 2xyy' = 0$$

$$\Rightarrow 2xy \frac{dy}{dx} + (x^2 - y^2 + 4) = 0$$

5. The sum of maximum and minimum values of $f(x) = \tan^{-1}(\sin x - \cos x)$, is (where $x \in [0, \pi]$)

(1) 0

(2) $\tan^{-1}\left(\frac{\sqrt{3}}{2} - 1\right) - \frac{\pi}{4}$

(3) $\cos^{-1}\left(\frac{1}{\sqrt{3}}\right) - \frac{\pi}{4}$

(4) $\frac{-\pi}{12}$

Ans. (3)

Sol. $f(x) = \tan^{-1}(\sin x - \cos x)$

$$f' = \frac{1}{1 + (\sin x - \cos x)^2} [\cos x + \sin x]$$

$$= \frac{\cos x + \sin x}{2 - \sin 2x}, x \in [0, \pi]$$

$$\frac{+}{-}$$

$$\frac{3\pi}{4}$$

Hence $x = \frac{3\pi}{4}$ is point of maxima

$$f\left(\frac{3\pi}{4}\right) = \tan^{-1}\left(\frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}}\right) = \tan^{-1}(\sqrt{2})$$

$$f(0) = \tan^{-1}(0-1) = -\frac{\pi}{4}$$

$$f(\pi) = \tan^{-1}(0+1) = \frac{\pi}{4}$$

So maximum value of $f(x)$ is $\tan^{-1} \sqrt{2} = \cos^{-1} \frac{1}{\sqrt{3}}$

and minimum value of $f(x)$ is $-\frac{\pi}{4}$

$$\text{sum} = \left(\cos^{-1} \frac{1}{\sqrt{3}} - \frac{\pi}{4} \right)$$

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6. If tangents drawn from $(2, 0)$ to the parabola $x = -2y^2$ are also tangents to the circle $(x-5)^2 + y^2 = r^2$ then the value of $17r^2$ is

Ans. (9)

Sol. Equation of tangent of parabola $y^2 = -\frac{1}{2}x$ in slope form is $y = mx - \frac{1}{8m}$ (i)

It passes through $(2, 0)$, so $2m = \frac{1}{8m} \Rightarrow m = \pm \frac{1}{4}$

$\Rightarrow y = \frac{x}{4} - \frac{1}{2}$ and $y = -\frac{x}{4} + \frac{1}{2}$ are also tangents to the circle $(x-5)^2 + y^2 = r^2$

$$\Rightarrow r = \left| \frac{\frac{5}{4} - \frac{1}{2}}{\sqrt{\frac{1}{16} + 1}} \right| \Rightarrow 17r^2 = 9$$

7. If α & β are the roots of the quadratic equation $x^2 - \sqrt{3}x + \sqrt{6} = 0$ and $1 + \frac{1}{\alpha^2}, 1 + \frac{1}{\beta^2}$ are the roots of

the quadratic equation $x^2 + ax + b = 0$, then roots of the quadratic equation

$$x^2 - (a + b - 2)x + (a + b + 2) = 0 \text{ are -}$$

(1) Both non-real

(2) Both real and positive

(3) Both real and negative

(4) Both real, one is positive and another is negative

Ans. (3)

Sol. $x^2 - \sqrt{3}x + \sqrt{6} = 0$ $\begin{matrix} \alpha \\ \beta \end{matrix}$

Equation having roots $1 + \frac{1}{\alpha^2}, 1 + \frac{1}{\beta^2}$

$$\frac{1}{x-1} - \frac{\sqrt{3}}{\sqrt{x-1}} + \sqrt{6} = 0$$

$$\left(\frac{1}{x-1} + \sqrt{6} \right) = \frac{\sqrt{3}}{\sqrt{x-1}}$$

$$\frac{1}{(x-1)^2} + 6 + \frac{2\sqrt{6}}{x-1} = \frac{3}{x-1}$$

$$1 + 6(x-1)^2 + 2\sqrt{6}(x-1) = 3(x-1)$$

$$\Rightarrow 6x^2 + (2\sqrt{6} - 15)x + (10 - 2\sqrt{6}) = 0$$

$$\Rightarrow x^2 + \left(\frac{2\sqrt{6} - 15}{6} \right)x + \left(\frac{10 - 2\sqrt{6}}{6} \right) = 0$$

$$\text{So, } a = \frac{2\sqrt{6} - 15}{6}, b = \frac{10 - 2\sqrt{6}}{6}$$

$$\Rightarrow a + b = -\frac{5}{6}$$

Now quadratic equation $x^2 - (a + b - 2)x + (a + b + 2) = 0$ is also $6x^2 + 17x + 7 = 0$

Since, $D = (17)^2 - 4(6)(7) > 0$, sum of roots = $-\frac{17}{6}$ and product of roots = $\frac{7}{6}$

Hence both roots are real negative

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8. If $\frac{6}{3^{12}} + \frac{10}{3^{11}} + \frac{20}{3^{10}} + \frac{40}{3^9} + \dots + \frac{10240}{3^1} = 2^m \cdot n$ then the value of m.n is

Ans. (12)

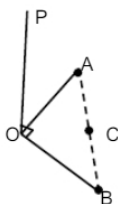
Sol.
$$\begin{aligned} n \cdot 2^m &= \frac{6}{3^{12}} + 10 \left(\frac{1}{3^{11}} + \frac{2}{3^{10}} + \frac{2^2}{3^9} + \dots + \frac{2^{10}}{3^1} \right) \\ &= \frac{6}{3^{12}} + \frac{10}{3^{11}} \left(\frac{6^{11}-1}{6-1} \right) \\ &= \frac{6}{3^{12}} + \frac{2}{3^{11}} (6^{11}-1) \\ &\Rightarrow n \cdot 2^m = \frac{6^{12}}{3^{12}} = 2^{12} \\ &\Rightarrow n = 1, m = 12 \\ &\Rightarrow mn = 12 \end{aligned}$$

9. If OAB is a triangular park and OP is a vertical tower such that $AB = 16$, $\angle PAO = 15^\circ = \angle PBO$, $\angle PCO = 45^\circ$ where C is mid-point of AB, then height of tower is

- (1) $16 \left(\frac{2}{\sqrt{3}} - 1 \right)$ (2) $32 \left(\frac{2}{\sqrt{3}} - 1 \right)$ (3) $32 \left(\frac{2}{\sqrt{3}} + 1 \right)$ (4) $16 \left(\frac{2}{\sqrt{3}} + 1 \right)$

Ans. (2)

Sol.



$OP = OA \tan 15^\circ = OB \tan 15^\circ$ (i)
 and $OP = OC \tan 45^\circ \Rightarrow OP = OC$ (ii)
 also $OA = OB$ (iii)
 so $OC^2 + 8^2 = OA^2$
 $OP^2 + 64 = \left(\frac{OP}{\tan 15^\circ} \right)^2$
 $OP^2 + 64 = OP^2 \left(\frac{\sqrt{3}+1}{\sqrt{3}-1} \right)^2$
 $64 = OP^2 \left[\frac{(\sqrt{3}+1)^2 - (\sqrt{3}-1)^2}{(\sqrt{3}-1)^2} \right] = OP^2 \left(\frac{4\sqrt{3}}{(\sqrt{3}-1)^2} \right)$
 $OP^2 = \frac{64(\sqrt{3}-1)^2}{4\sqrt{3}} = 32 \left(\frac{2}{\sqrt{3}} - 1 \right)$

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10. If curves $y = f(x)$ satisfying differential equation $\frac{dy}{dx} + \left(\frac{1}{x^2-1}\right)y = \left(\frac{x-1}{x+1}\right)^{\frac{1}{2}}$ such that $f(2) = \sqrt{3}$ then the value of $\sqrt{7} f(8)$ is

- (1) $7-3/\sqrt{3}$ (2) $21-6/\sqrt{3}$ (3) $21-6/\sqrt{3}$ (4) $7+3/\sqrt{3}$

Ans. (3)

Sol. $\frac{dy}{dx} + \left(\frac{1}{x^2-1}\right)y = \left(\frac{x-1}{x+1}\right)^{\frac{1}{2}}$ is linear differential equation

$$I. F. = e^{\int \frac{1}{x^2-1} dx} = \sqrt{\frac{x-1}{x+1}}$$

So, solution of given differential equation is

$$y \sqrt{\frac{x-1}{x+1}} = \int \left(\frac{x-1}{x+1}\right)^{\frac{1}{2}} \left(\frac{x-1}{x+1}\right)^{\frac{1}{2}} dx + C$$

$$= y \sqrt{\frac{x-1}{x+1}} = x - 2/\sqrt{3} \ln(x+1) + C$$

It is passing through $(2, \sqrt{3}) \Rightarrow C = 2/\sqrt{3} - 1$

$$\Rightarrow y \sqrt{\frac{x-1}{x+1}} = x - 2/\sqrt{3} \ln(x+1) + 2/\sqrt{3} - 1$$

$$\text{put } x = 8 \Rightarrow \frac{y\sqrt{7}}{3} = 8 - 2/\sqrt{3} \ln 9 + 2/\sqrt{3} - 1$$

$$\Rightarrow y\sqrt{7} = \sqrt{7} f(8) = 21 - 6/\sqrt{3}$$

11. If b and g are number of boys and girls in a class respectively such that number of ways to select 3 boys and 2 girls is 168, then the value of $(b+2g)$ is equal to

Ans. (14)

Sol. ${}^bC_3 \cdot {}^gC_2 = 168$

$$\frac{b(b-1)(b-2)}{6} \cdot \frac{g(g-1)}{2} = 168$$

$$b(b-1)(b-2) \cdot g(g-1) = 2 \cdot 6 \cdot 14 \cdot 12 = 2^5 \cdot 3^2 \cdot 7^1$$

$$\therefore b \in \mathbb{N} \text{ and } b \geq 3, g \in \mathbb{N}, g \geq 2$$

$$\Rightarrow b(b-1)(b-2) \cdot g(g-1) = 8 \cdot 7 \cdot 6 \cdot 3 \cdot 2$$

$$\Rightarrow b=8, g=3 \text{ so } b+2g=14$$

12. If A and B are two 3×3 order matrices such that A is symmetric and B is skew-symmetric, then which of the following is incorrect.

- (1) $A^4 - B^4$ is symmetric matrix (2) $AB - BA$ is symmetric matrix
(3) $A^5 - B^5$ is skew-symmetric (4) $AB + BA$ is skew-symmetric

Ans. (3)

Sol. Given $A^T = A, B^T = -B$

$$(1) P = A^4 - B^4$$

$$P^T = (A^4 - B^4)^T$$

$$= (A^T)^4 - (B^T)^4$$

$$= A^4 - B^4 = P, \text{ So } A^4 - B^4 \text{ is symmetric matrix}$$

(1) is correct

$$(2) \text{ Let } Q = AB - BA$$

$$Q^T = (AB - BA)^T = B^T A^T - A^T B^T$$

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$$= -BA + AB = Q \Rightarrow AB - BA \text{ is symmetric matrix}$$

(2) is correct

$$(3) \text{ Let } P = A^5 - B^5$$

$$P^T = (A^5 - B^5)^T$$

$$= A^5 - (-B)^5$$

$$= A^5 + B^5 \Rightarrow$$

$$A^5 - B^5 \text{ is not skew-symmetric}$$

(3) is incorrect

$$(4) \text{ Let } Q = AB + BA$$

$$Q^T = (AB + BA)^T = B^T A^T + A^T B^T$$

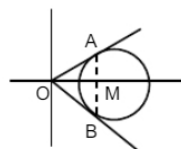
$$= -BA + AB = Q \Rightarrow AB - BA \text{ is symmetric matrix}$$

(4) is correct

13. If OA and OB are tangents to the circle $(x-2)^2 + y^2 = 1$ from origin (O) then the area of $\triangle OAB$ is

- (1) $\frac{3}{4}$ (2) $\frac{3\sqrt{3}}{4}$ (3) $\frac{3\sqrt{3}}{2}$ (4) $\frac{\sqrt{3}}{4}$

Ans. (2)
Sol.



Equation of chord AB is $2x=3$

$$\Rightarrow OA = OB = \sqrt{3}$$

$$\Rightarrow AM = \frac{\sqrt{3}}{2}$$

$$\text{Area of } \triangle OAB = \frac{1}{2}(2AM)(OM) = \frac{\sqrt{3}}{2} \cdot \frac{3}{2} = \frac{3\sqrt{3}}{4}$$

14. Consider the following statements

P: Ramesh is singing

Q: Ramesh is out of his village

R: It is Sunday

S: It is Saturday

Now which of the following option is logically equivalent to the compound statement "Ramesh is singing only if he is in his village and it is either Sunday or Saturday"

- (1) $((\sim q) \wedge (r \vee s)) \rightarrow P$ (2) $P \rightarrow (\sim q \wedge (s \vee r))$
(3) $P \rightarrow (q \wedge (r \vee s))$ (4) $P \rightarrow (q \wedge (r \vee s))$

Ans. (2)

Sol. $\therefore p \rightarrow q$ convey the same meaning as P only if q

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15. If $x(t) = 2\sqrt{2} \cos t \sqrt{\sin 2t}$ and $y(t) = 2\sqrt{2} \sin t \sqrt{\sin 2t}$, where $t \in \left(0, \frac{\pi}{2}\right)$ then the value of $\left\{ \frac{1 + \left(\frac{dy}{dx}\right)^2}{\frac{d^2y}{dx^2}} \right\}$ at $x =$

$$\frac{\pi}{4}$$

- (1) $-\frac{1}{2}$ (2) $\frac{1}{2}$ (3) 2 (4) $-\frac{2}{3}$

Ans. (4)

Sol. $\frac{y}{x} = \tan t$ and $x^2 + y^2 = 8 \sin 2t$

$$x^2 + y^2 = \frac{16 \tan t}{1 + \tan^2 t}$$

$$(x^2 + y^2) = \frac{16xy}{x^2 + y^2}$$

$$\Rightarrow (x^2 + y^2)^2 = 16xy$$

$$\Rightarrow 2(x^2 + y^2) \left(2x + 2y \frac{dy}{dx} \right) = 16 \left(x \frac{dy}{dx} + y \right) \quad \dots (i)$$

$$\Rightarrow \text{when } t = \frac{\pi}{4} \Rightarrow x = 2 = y \text{ and } \frac{dy}{dx} = -1 \quad \dots (ii)$$

Differentiate of equation (i) w.r. to x

$$2(2x + 2y \frac{dy}{dx})^2 + 2(x^2 + y^2) \left(2 + 2 \left(\left(\frac{dy}{dx} \right)^2 + y \frac{d^2y}{dx^2} \right) \right) = 16 \left(x \frac{d^2y}{dx^2} + 2 \frac{dy}{dx} \right)$$

$$\text{at } x = \frac{\pi}{4} \Rightarrow 0 + 16(2+2+4 \frac{d^2 y}{dx^2}) = 16 \left(2 \frac{d^2 y}{dx^2} - 2 \right) \Rightarrow \frac{d^2 y}{dx^2} = -3$$

$$\left\{ 1 + \left(\frac{dy}{dx} \right)^2 \right\} \frac{d^2 y}{dx^2} \text{ at } x = \frac{\pi}{4} = -\frac{2}{3}$$

16. The coefficient of middle terms of the expansions $\left(\frac{1}{\sqrt{6}} + \beta x \right)^4$, $(1-3\beta x)^2$, and $\left(1 - \frac{\beta x}{2} \right)^6$ are in AP with common difference $d > 0$ then the value of $50 - \frac{2d}{\beta^2}$ is

Ans. 46

Sol. ${}^4C_2 \left(\frac{1}{\sqrt{6}} \right)^2 (\beta)^2, -6\beta, -{}^6C_3 \frac{\beta^3}{8}$ in AP

$$\beta^2, -6\beta, -\frac{5}{2}\beta^3 \text{ are in AP}$$

$$-12\beta = \beta^2 - \frac{5}{2}\beta^3$$

$$-24\beta = 2\beta^2 - 5\beta^3$$

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$$5\beta^3 - 2\beta^2 - 24\beta = 0$$

$$5\beta^2 - 2\beta^2 - 24 = 0 \quad (\beta \neq 0)$$

$$\Rightarrow 5\beta^2 - 12\beta + 10\beta - 24 = 0$$

$$(5\beta - 12)(\beta + 2) = 0$$

$$\beta = \frac{12}{5} \quad \text{or} \quad \beta = -2$$

$$\text{when } \beta = \frac{12}{5} \Rightarrow d = -\beta - \beta^2 = -\frac{72}{5} - \frac{144}{25} = -\frac{504}{25} \text{ not possible because } d > 0$$

$$\text{when } \beta = -2 \Rightarrow d = -6\beta - \beta^2 = 12 - 4 = 8$$

$$\text{so } 50 - \frac{2d}{\beta^2} = 50 - \frac{16}{4} = 46$$

17. If $S = \left\{ x : x \in [-6, 3] - \{-2, 2\}, \frac{|x+3|-1}{|x|-2} \geq 0 \right\}$ and $T = \{x : x \in \mathbb{Z}; x^2 - 7|x| + 9 \leq 0\}$, then number of elements

in $S \cap T$ is

(1) 2

(2) 3

(3) 5

(4) 7

Ans. (3)

Sol. $T = \{x : x \in \mathbb{Z}; x^2 - 7|x| + 9 \leq 0\}$

$$|x^2| - 7|x| + 9 \leq 0$$

$$\Rightarrow |x| \in \left[\frac{7-\sqrt{13}}{2}, \frac{7+\sqrt{13}}{2} \right]$$

$$\Rightarrow |x| = 2, 3, 4, 5$$

$$\Rightarrow S = \left\{ x : x \in [-6, 3] - \{-2, 2\}, \frac{|x+3|-1}{|x|-2} \geq 0 \right\}$$

To find $n(S \cap T)$

$$|x| \neq 2 \Rightarrow |x| = 3, 4, 5, x \in [-6, 3] - \{-2, 2\} \text{ and } |x+3| \geq 1 \Rightarrow x = 3, -4, -5 \Rightarrow n(S \cap T) = 3$$

18. There are 4 girls and 6 boy in a class. Three students are selected randomly from the class. If a random variety 'x' represents the number of selected girls, then the value of $100(\sigma^2)$ is : where (σ^2) is the variance of distribution

Ans. (56)

Sol. By probability distribution

x	0	1	2	3
P(x)	$\frac{{}^6C_3}{{}^{10}C_3}$	$\frac{{}^4C_1 \cdot {}^6C_2}{{}^{10}C_3}$	$\frac{{}^4C_2 \cdot {}^6C_1}{{}^{10}C_3}$	$\frac{{}^4C_3}{{}^{10}C_3}$

$$\text{Variance} = \sum p_i \cdot x_i^2 - (\mu)^2$$

$$= \left(0 + \frac{60}{120} \cdot 1 + \frac{36}{120} \cdot 4 + \frac{4}{120} \cdot 9 \right) - \left(0 + \frac{60.1}{120} + \frac{36.2}{120} + \frac{4.3}{120} \right)^2 = \frac{240}{120} - \left(\frac{144}{120} \right)^2$$

$$= \frac{240}{120} - \frac{144}{120} = 2$$

$$\sigma^2 = 2 - \left(\frac{9}{5}\right)$$

$$= \frac{50-36}{25}$$

$$\Rightarrow 100\sigma^2 = 100 \left(\frac{14}{25}\right) = 56$$

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19 If $f(x) = \lim_{n \rightarrow \infty} \left(\frac{\cos 2\pi x + x^{2n} \sin(x-1)}{1 + x^{2n+1} - 2^n} \right)$, $n \in \mathbb{N}$ then $f(x)$ is continuous for x belong to :

Ans. (1) $\mathbb{R} - \{-1\}$ (2) $\mathbb{R} - \{1\}$ (3) $\mathbb{R} - \{-1, 1\}$ (4) $\mathbb{R} - \{0\}$

Sol. Case-1 when $|x| > 1 \Rightarrow f(x) = \lim_{n \rightarrow \infty} \frac{x^{2n}}{x^{2n+1}} \left(\frac{\frac{1}{x^{2n}} \cdot \cos 2\pi x + \sin(x-1)}{\frac{1}{x^{2n+1}} + 1 - \frac{1}{x}} \right) = \frac{\sin(x-1)}{x-1}$

Case-2 When $-1 < x < 1 \Rightarrow f(x) = \lim_{n \rightarrow \infty} \left(\frac{\cos 2\pi x + x^{2n} \sin(x-1)}{1 + x^{2n+1} - x^{2n}} \right)$

$f(x) = \cos 2\pi x$

Case-3 When $x = 1 \Rightarrow f(1) = 1$

Case-4 when $x = -1 \Rightarrow f(-1) = \sin 2 - 1$

So, $f(x) = \begin{cases} \frac{\sin(x-1)}{x-1}, & x < -1 \text{ or } x > 1 \\ \cos 2\pi x, & -1 < x < 1 \\ 1, & x = 1 \\ \sin 2 - 1, & x = -1 \end{cases}$

function $f(x)$ is continuous except $x = -1$

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