# PART -A (PHYSICS)

1. At a given instant, say t = 0, two radioactive substances A and B have equal activates. The ratio  $\frac{R_B}{R_B}$  of their activities. The ratio  $\frac{R_B}{R_B}$  of their activates after time t itself decays

with time t as  $e^{-3t}$ . If the half-life of A is  $\ell n2$ , the half-life of B is:

(A) 4ℓn2

(B)  $\frac{\ell n2}{2}$ 

(C)  $\frac{\ell n2}{4}$ 

(D) 2ℓn2

2. A power transmission line feeds input power at 2300 V to a step down transformer with its primary windings having 4000 turns. The output power is delivered at 230 V by the transformer. If the current in the primary of the transformer is 5A and its efficiency is 90%, the output current would be:

(A) 50 A

(B) 45 A (D) 25 A

(C) 35 A

The energy associated with electric field is (UE) and with magnetic field is (UB) for 3. an electromagnetic wave in free space. Then:

(A)  $U_{E} = \frac{U_{B}}{2}$ 

(B)  $U_E > U_B$ 

(C)  $U_E < U_B$ 

(D)  $U_E = U_B$ 

A force acts on a 2 kg object so that its position is given as a function of time as  $x = 3t^2 +$ 4. 5. What is the work done by this force in first 5 seconds?

(A) 850 J

(B) 950 J

(C) 875 J

(D) 900 J

5. A particle having the same charge as of electron moves in a circular path of radius 0.5 cm under the influence of a magnetic field of 0.5 T. If an electric field of 100 V/m makes it to move in a straight path, then the mass of the particle is (given charge of electron  $= 1.6 \times 10^{-19} \,\mathrm{C})$ 

(A)  $9.1 \times 10^{-31}$  kg

(B)  $1.6 \times 10^{-27}$  kg (D)  $2.0 \times 10^{-24}$  kg

(C)  $1.6 \times 10^{-19} \text{ kg}$ 

Two point charges  $q_1(\sqrt{10} \mu C)$  and  $q_2(-25 \mu C)$  are placed on the x-axis at x = 1 m6. and x = 4 m respectively. The electric field (in V/m) at a point y = 3 m on y-axis is,

 $\tan \frac{1}{4\pi\varepsilon_0} = 9 \times 10^9 \text{Nm}^2 \text{C}^{-2}$ 

(A)  $(63\hat{i} - 27\hat{i}) \times 10^2$ 

(B)  $(-63\hat{i} + 27\hat{i}) \times 10^2$ 

(C)  $(81\hat{i} - 81\hat{i}) \times 10^2$ 

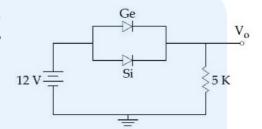
(D)  $(-81\hat{i} + 81\hat{i}) \times 10^2$ 

- 7. Expression for time in terms of G (universal gravitational constant), h (Planck constant) and c (speed of light) is proportional to:
  - (A)  $\sqrt{\frac{hc^5}{G}}$

(B)  $\sqrt{\frac{c^3}{Gh}}$ 

(C)  $\sqrt{\frac{Gh}{c^5}}$ 

- 8. Ge and Si diodes start conducting at 0.3 V and 0.7 V respectively. In the following figure if Ge diode connection are reversed, the value of V<sub>o</sub> changes by: (assume that the Ge diode has large breakdown voltage)



- (A) 0.8 V
- (B) 0.6 V
- (C) 0.2 V
- (D) 0.4 V
- 9. The top of a water tank is open to air and its water level is maintained. It is giving out 0.74 m<sup>3</sup> water per minute through a circular opening of 2 cm radius in its wall. The depth of the centre of the opening from the level of water in the tank is close to:
  - (A) 6.0 m

(B) 4.8 m

(C) 9.6 m

- (D) 2.9 m
- The energy required to take a satellite to a height 'h' above Earth surface (radius of 10. Earth =  $6.4 \times 10^3$  km) is E<sub>1</sub> and kinetic energy required for the satellite to be in a circular orbit at this height is  $E_2$ . The value of h for which  $E_1$  and  $E_2$  are equal is
  - (A)  $1.6 \times 10^3$  km

(B)  $3.2 \times 10^3$  km

(C) 6.4 × 10<sup>3</sup> km

- (D)  $1.28 \times 10^4$  km
- 11. Two Carnot engines A and B are operated in series. The first one, A, receives heat at  $T_1$ (= 600 K) and rejects to a reservoir at temperature  $T_2$ . The second engine B receives heat rejected by the first engine and, in turns, rejects to a heat reservoir at  $T_3$  (=400 K). Calculate the temperature T<sub>2</sub> if the work outputs of the two engines are equal:
  - (A) 600 K

(B) 400 K

(C) 300 K

- (D) 500 K
- 12. A series AC circuit containing an inductor (20 mH), a capacitor (120 μF) and a resistor (60  $\Omega$ ) is driven by an AC source of 24 V/50 Hz. The energy dissipated in the circuit in 60 s is:
  - (A)  $5.65 \times 10^2 \text{ J}$

(B)  $2.26 \times 10^3 \text{ J}$ (D)  $3.39 \times 10^3 \text{ J}$ 

(C)  $5.17 \times 10^2 \text{ J}$ 

- A particle is executing simple harmonic motion (SHM) of amplitude A, along the x-axis, 13. about x = 0. When its potential energy (PE) equals kinetic energy (KE), the position of the particle will be

(B)  $\frac{A}{2\sqrt{2}}$ 

(C)  $\frac{A}{\sqrt{2}}$ 

(D) A

14. A mass of 10 kg is suspended vertically by a rope from the roof. When a horizontal force is applied on the rope at some point, the rope deviated at an angle of 45° at the roof point. If the suspended mass is at equilibrium, the magnitude of the force applied is (g = 10 ms<sup>-2</sup>)

(A) 200 N

(B) 140 N

(C) 70 N

(D) 100 N

A 15 g mass of nitrogen gas is enclosed in a vessel at a temperature 27°C. Amount of 15. heat transferred to the gas, so that rms velocity of molecules is doubled, is about: [Take R = 8.3 J/K mole

(A) 0.9 kJ

(B) 6 kJ

(C) 10 kJ

(D) 14 kJ

16. In a Young's double slit experiment, the slits are placed 0.320 mm apart. Light of wavelength  $\lambda = 500$  nm is incident on the slits. The total number of bright fringes that are observed in the angular range  $-30^{\circ} \le \theta \le 30^{\circ}$  is:

(A) 640

(B) 320

(C) 321

(D) 641

17. Two plane mirrors are inclined to each other such that a ray of light incident to the first mirror (M<sub>1</sub>) and parallel to the second mirror (M<sub>2</sub>) is finally reflected from the second mirror (M<sub>2</sub>) parallel to the first mirror (M<sub>1</sub>). The angle between the two mirrors will be:

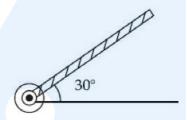
(A) 45°

(B) 60°

(C) 75°

(D) 90°

18. A rod of length 50 cm is pivoted at one end. It is raised such that if makes an angle of 30° fro the horizontal as shown and released from rest. Its angular speed when it passes through the horizontal (in rad s<sup>-1</sup>) will be (g = 10 ms<sup>-2</sup>).



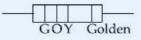
(A)  $\sqrt{\frac{30}{2}}$ 

(B)  $\sqrt{30}$ 

(C)  $\sqrt{\frac{20}{2}}$ 

(D)  $\frac{\sqrt{30}}{3}$ 

19. A carbon resistance has a following colour code. What is the value of the resistance?



(A) 530 k $\Omega \pm 5\%$ 

(B) 5.3 M $\Omega \pm 5\%$ 

(C) 6.4 M $\Omega \pm 5\%$ 

(D) 64 k $\Omega \pm 10\%$ 

20. One of the two identical conducing wires of length L is bent in the form of a circular loop and the other one into a circular coil of N identical turns. If the same current is passed in both, the ratio of the magnetic field at the central of the loop (B<sub>L</sub>) to that at the centre of

the coil (B<sub>C</sub>), i.e.  $\frac{B_L}{B_C}$  will be

(A) N

(B)  $\frac{1}{N}$ 

(C) N<sup>2</sup>

(D)  $\frac{1}{N^2}$ 

- 21. A rod of mass 'M' and length '2L' is suspended at its middle by a wire. It exhibits torsional oscillations; If two masses each of 'm' are attached at distance 'L/2' from its centre on both sides, it reduces the oscillation frequency by 20%. The value of ratio m/M is close to:
  - (A) 0.77

(B) 0.57 (D) 0.17

(C) 0.37

Charge is distributed within a sphere of radius R with a volume charge density 22.  $\rho(r) = \frac{A}{r^2} e^{-2r/a}$ , where A and a are constants. If Q is the total charge of this charge distribution, the radius R is:

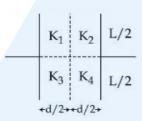
(A) 
$$a \log \left(1 - \frac{Q}{2\pi aA}\right)$$

(B) 
$$\frac{a}{2} \log \left( \frac{1}{1 - \frac{Q}{2\pi aA}} \right)$$

(C) 
$$\frac{a}{2} \log \left( \frac{1}{1 - \frac{Q}{2\pi a A}} \right)$$

(D) 
$$\frac{a}{2} log \left(1 - \frac{1}{2\pi aA}\right)$$

23. A parallel palate capacitor with square plates is filled with four dielectrics of dielectric constants K<sub>1</sub>, K<sub>2</sub>, K<sub>3</sub>, K<sub>4</sub> arranged as shown in the figure. The effective dielectric constant K will be:



(A) 
$$K = \frac{(K_1 + K_3)(K_2 + K_4)}{K_1 + K_2 + K_3 + K_4}$$
  
(C)  $K = \frac{(K_1 + K_2)(K_3 + K_4)}{K_1 + K_2 + K_3 + K_4}$ 

(B) 
$$K = \frac{(K_1 + K_2)(K_3 + K_4)}{2(K_1 + K_2 + K_3 + K_4)}$$
  
(D)  $K = \frac{(K_1 + K_4)(K_2 + K_3)}{2(K_1 + K_2 + K_3 + K_4)}$ 

(C) 
$$K = \frac{(K_1 + K_2)(K_3 + K_4)}{K_1 + K_2 + K_3 + K_4}$$

(D) 
$$K = \frac{(K_1 + K_4)(K_2 + K_3)}{2(K_1 + K_2 + K_3 + K_4)}$$

24. The pitch and the number of divisions, on the circular scale, for a given screw gauge are 0.5 mm and 100 respectively. When the screw gauge is fully tightened without any object, the zero of its circular scale lies 3 divisions below the mean line.

The readings of the main scale and the circular scale for a thin sheet, are 5.5 mm and 48 respectively, the thickness of this sheet is

(A) 5.755 mm

(B) 5.950 mm

(C) 5.725 mm

- (D) 5.740 mm
- 25. A musician using an open flute of length 50 cm produces second harmonic sound

A person runs towards the musician from another end of a hall at a speed of 10 km/h. If the wave speed is 330 m/s, the frequency heard by the running person shall be close to:

(A) 666 Hz

(B) 753 Hz

(C) 500 Hz

(D) 333 Hz

26. In a car race on straight road, car A takes a time 't' less than car B at the finish and passes finishing point with a speed 'v' more than that of car B. Both the cars start from rest and travel with constant acceleration a<sub>1</sub> and a<sub>2</sub> respectively. Then 'v' is equal to

(A) 
$$\frac{2a_1a_1}{a_1+a_2}t$$

(B) 
$$\sqrt{2a_1a_2}$$
 t

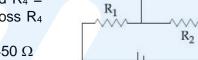
(C) 
$$\sqrt{a_1 a_2}$$
 t

(D) 
$$\frac{a_1 + a_2}{2}t$$

27. The magnetic field associated with a light wave is given, at the origin, by

If this light falls on a silver plate having a work function of 4.7 eV, what will be the maximum kinetic energy of the photo electrons?

28. In the given circuit the internal resistance of the 18 V cell is negligible. If  $R_1 = 400~\Omega$ ,  $R_3 = 100~\Omega$  and  $R_4 = 500~\Omega$  and the reading of an ideal voltmeter across  $R_4$  is 5 V, then the value of  $R_2$  will be



18 V

(A) 300 
$$\Omega$$

(B) 450 
$$\Omega$$

(C) 550 
$$\Omega$$

(D) 230 
$$\Omega$$

29. In a communication system operating at wavelength 800 nm, only one percent of source frequency is available as signal bandwidth. The number of channels accommodated for transmitting TV signals of band width 6 MHz are (Take velocity of light  $c = 3 \times 10^8$  m/s,  $h = 6.6 \times 10^{-34}$  J-s)

(A) 
$$3.75 \times 10^6$$

(B) 
$$3.86 \times 10^6$$

$$(C)$$
 6.25 × 10<sup>5</sup>

(D) 
$$4.87 \times 10^5$$

30. The position co-ordinates of a particle moving in a 3-D coordinates system is given by

$$x = a \cos \omega t$$

$$y = a \sin \omega t$$

and 
$$z = a\omega t$$

The speed of the particle is:

(A) 
$$\sqrt{2}$$
 a $\omega$ 

(C) 
$$\sqrt{3}$$
 a $\omega$ 

# **PART -B (CHEMISTRY)**

- 31. The entropy change associated with the conversion of 1 kg of ice at 273 K to water vapours at 383 K is: (Specific heat of water liquid and water vapours are 4.2 kJ  $K^{-1}$  kg<sup>-1</sup> and 2.0 kJ  $K^{-1}$  kg<sup>-1</sup>, heat of liquid fusion and vapourisation of water are 334 kJ kg<sup>-1</sup> and 2491 kJ kg<sup>-1</sup>, respectively) (log 273 = 2.436, log 373 = 2.572, log 383 = 2.583)
  - (A) 7.90 kJ K<sup>-1</sup> kg<sup>-1</sup>

(B) 2.64 kJ K<sup>-1</sup> kg<sup>-1</sup>

(C) 8.49 kJ K<sup>-1</sup> kg<sup>-1</sup>

- (D) 9.26 kJ K<sup>-1</sup> kg<sup>-1</sup>
- 32. For the following reaction the mass of water produced from 445 g of  $C_{57}H_{110}O_6$  is  $2C_{57}H_{110}O_6(s)+163O_2(g)-\longrightarrow 114CO_2(g)+110H_2O(I)$ 
  - (A) 490 g

(B) 445 g

(C) 495 g

- (D) 890 g
- 33. The major product formed in the following reaction is:

(A)  $H_3C$  H

- (B) H O OH H<sub>3</sub>C
- (C) H<sub>3</sub>C
- $(D) \qquad O \qquad OH \qquad \\ H_3C \qquad \\$
- 34. Which of the following conditions in drinking water causes methemoglobinemia?
  - (A) > 50 ppm of lead

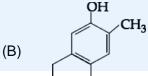
(B) > 50 ppm of chloride

(C) > 50 ppm of nitrate

- (D) > 100 ppm of sulphate
- 35. The major product of the following reaction is:

O + CH<sub>3</sub>AlCl<sub>3</sub>, 
$$\Delta$$

(A) CH<sub>3</sub>

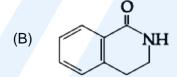


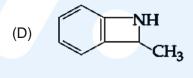
36. The major product obtained in the following reaction is:

OH 
$$(CH_3CO)_2O$$
/pyridine (1 eqv.) room temp.  $NH_2$ 

37. The major product of the following reaction is:

$$\begin{array}{c|c}
O \\
C \\
NH_2 \\
CH_2CH_3
\end{array}$$
(i) Br<sub>2</sub>/hv
(ii) KOH (dil)





38. The correct match between item I and item II is

#### Item II

- Benzaldehyde (a)
- Mobile phase (p) Adsorbent (q)
- Alumina (b) Acetonitrile (c)
- (r) Adsorbate
- (A)  $a \rightarrow q$ ,  $b \rightarrow p$ ,  $c \rightarrow r$

(B)  $a \rightarrow r$ ,  $b \rightarrow q$ ,  $c \rightarrow p$ 

(C)  $a \rightarrow q, b \rightarrow r, c \rightarrow p$ 

(D)  $a \rightarrow p, b \rightarrow r, c \rightarrow q$ 

- 39. The metal that forms nitride by reacting directly with N<sub>2</sub> of air is
  - (A) K

(B) Li

(C) Rb

- (D) Cs
- 40. For coagulation of arsenious sulphide sol, which one of the following salt solution will be most effective?
  - (A) BaCl<sub>2</sub>

(B) AICI<sub>3</sub>

(C) NaCl

(D) Na<sub>3</sub>PO<sub>4</sub>

- 41. The complex that has highest crystal field splitting energy( $\Delta$ ) is
  - (A)  $[Co(NH_3)_5(H_2O)]CI_3$

(B)  $K_2[CoCl_4]$ 

(C) [Co(NH<sub>3</sub>)<sub>5</sub>Cl]Cl<sub>2</sub>

- (D)  $K_3[Co(CN)_6]$
- 42. The pH of rain water is approximately
  - (A) 5.6

(B) 7.5

(C) 7.0

- (D) 6.5
- 43. Consider the following reversible chemical reactions:

$$A_2(g) + B_2(g) \xrightarrow{K_1} 2 AB(g)$$
 ......

$$6 AB(g) \stackrel{\kappa_2}{\rightleftharpoons} 3 A_2(g) + 3 B_2(g) \dots (2)$$

The relation between K<sub>1</sub> and K<sub>2</sub> is

(A) 
$$K_1K_2 = \frac{1}{3}$$

(B) 
$$K_2 = K_1^3$$

(C) 
$$K_2 = K_1^{-3}$$

(D) 
$$K_1K_2 = 3$$

44. The correct sequence of amino acids present in the tripeptide given below is

$$\begin{array}{c|c} Me & Me & OH \\ H_2N & N & OH \\ OH & OH \\ OH & OH \\ \end{array}$$

(A) Val – Ser – Thr

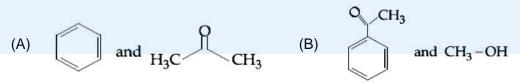
(B) Thr – Ser – Val

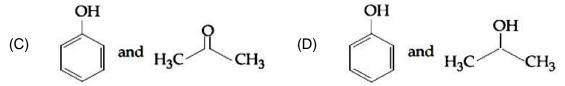
(C) Leu - Ser - Thr

- (D) Thr Ser Leu
- 45. For the reaction,  $2A+B\longrightarrow$  products , when the concentrations of A and B both were doubled, the rate of the reaction increased from 0.3 mol L<sup>-1</sup> s<sup>-1</sup> to 2.4 mol L<sup>-1</sup> s<sup>-1</sup>. When the concentration of A alone is doubled, the rate increased from 0.3 mol L<sup>-1</sup> s<sup>-1</sup> to 0.6 mol L<sup>-1</sup> s<sup>-1</sup>.

Which one of the following statements is correct?

- (A) Total order of the reaction is 4
- (B) Order of the reaction with respect to B is 2
- (C) Order of the reaction with respect to B is 1
- (D) Order of the reaction with respect to A is 2
- 46. The products formed in the reaction of cumene with O<sub>2</sub> followed by treatment with dil. HCl are:





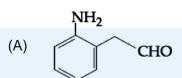
47. The tests performed on compound X and their inferences are:

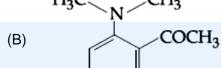
#### Test

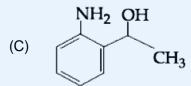
#### Interference

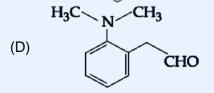
- (a) 2, 4-DNP test
- Colorued precipitate
- (b) lodoform test
- Yellow precipitate
- Azo-dye test (c)
- No dye formation

Compound 'X' is









48. If the standard electrode potential for a cell is 2 V at 300 K, the equilibrium constant (K) for the reaction

$$Zn(s) + Cu^{2+}(aq) \Longrightarrow Zn^{2+}(aq) + Cu(s)$$

At 300 K is approximately

$$(R = 8 \text{ JK}^{-1} \text{ mol}^{-1}, F = 96000 \text{ C mol}^{-1})$$

(A)  $e^{-80}$ 

(B)  $e^{-160}$ 

(C)  $e^{320}$ 

- (D)  $e^{160}$
- 49. The temporary hardness of water is due to
  - (A) Na<sub>2</sub>SO<sub>4</sub>

(B) NaCl

(C) Ca(HCO<sub>3</sub>)<sub>2</sub>

- (D) CaCl<sub>2</sub>
- 50. In which of the following processes, the bond order has increased and paramagnetic character has changed to diamagnetic?
  - (A)  $NO \longrightarrow NO^+$

(B)  $N_2 \longrightarrow N_2^+$ 

(C)  $O_2 \longrightarrow O_2^+$ 

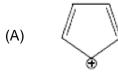
- (D)  $O_2 \longrightarrow O_2^{2-}$
- 51. Which of the following combination of statements is true regarding the interpretation of the atomic orbitals?
  - (1) An electron in an orbital of high angular momentum stays away from the nucleus than an electron in the orbital of lower angular momentum.
  - (2) For a given value of the principal quantum number, the size of the orbit is inversely proportional to the azimuthal quantum number
  - (3) According to wave mechanics, the ground state angular momentum is equal to  $\frac{h}{2\pi}$
  - (4) The plot of ψ Vs r for various azimuthal quantum numbers, shows peak shifting towards higher r value
  - (A) (1), (4)

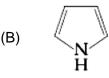
(B) (1), (2)

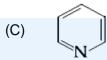
(C) (1), (3)

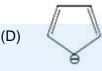
(D) (2), (3)

52. Which of the following compounds is not aromatic?









53. Good reducing nature of H<sub>3</sub>PO<sub>2</sub> is attributed to the presence of

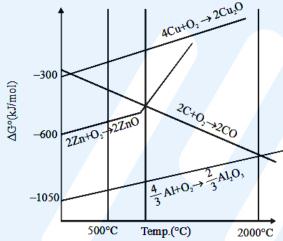
(A) Two P – OH bonds

(B) One P – H bond

(C) Two P – H bonds

(D) One P – OH bond

54. The correct statement regarding the given Ellingham diagram is



(A) At 1400°C, Al can be used for the extraction of Zn from ZnO

(B) At 500°C, coke can be used for the extraction of Zn from ZnO

(C) Coke cannot be used for the extraction of Cu from Cu<sub>2</sub>O

(D) At 800°C Cu can be used for the extraction of Zn from ZnO

55. The transition element that has lowest enthalpy of atomisation is

(A) Fe

(B) Cu

(C) V

(D) Zn

56. The increasing basicity order of the following compounds is

(1) CH<sub>3</sub>CH<sub>2</sub>NH<sub>2</sub>

(2) CH<sub>3</sub>CH<sub>2</sub>NH

(3)  $\begin{array}{c} CH_3 \\ H_3C-N-CH_3 \end{array}$ 

(4)  $CH_3$  Ph-N-H

(A) (4) < (3) < (2) < (1)

(B) (4) < (3) < (1) < (2)

(C) (1) < (2) < (3) < (4)

(D) (1) < (2) < (4) < (3)

- 57. When the first electron gain enthalpy ( $\Delta_{eg}H$ ) of oxygen is -141 kJ/mol, its second electron gain enthalpy is
  - (A) a more negative value than the first (B)
    - (B) almost the same as that of the first
  - (C) negative, but less negative than the first (D) a positive value
- 58. At  $100^{\circ}$ C, copper(Cu) has FCC unit cell structure with cell edge length x  $\overset{\circ}{A}$ . What is the approximate density of Cu(in g cm<sup>-3</sup>) at this temperature?

[Atomic mass of Cu = 63.55 u]

(A)  $\frac{205}{x^3}$ 

 $(B)\frac{105}{x^3}$ 

(C)  $\frac{211}{x^3}$ 

- (D)  $\frac{422}{x^3}$
- 59. A solution containing 62 g ethylene glycol in 250 g water is cooled to -10°C. If K<sub>f</sub> for water is 1.86 K kg mol<sup>-1</sup>, the amount of water(in g) separated as ice is
  - (A) 48

(B) 32

(C) 64

- (D) 16
- 60. Homoleptic octahedral complexes of a metal ion ' $M^{3+}$ ' with three monodentate ligands  $L_1$ ,  $L_2$  and  $L_3$  absorb wavelengths in the region of green, blue and red respectively. The increasing order of the ligand strength is
  - (A)  $L_3 < L_1 < L_2$

(B)  $L_3 < L_2 < L_1$ 

(C)  $L_1 < L_2 < L_3$ 

(D)  $L_2 < L_1 < L_3$ 

# **PART-C (MATHEMATICS)**

61. The sum of the following series

 $1+6+\frac{9 \left(1^2+2^2+3^2\right)}{7}+\frac{12 \left(1^2+2^2+3^2+4^2\right)}{9}+\frac{15 \left(1^2+2^2+....+5^2\right)}{11}+... \text{ up to 15 terms, is:}$ 

(A) 7820

(C) 7520

- For each  $x \in R$ , let [x] be the greatest integer less than or equal to x. Then 62.  $\lim_{x\to 0^+}\frac{x\left(\left[x\right]+\left|x\right|\right)\sin\left[x\right]}{\left|x\right|} \text{ is equal to}$ 
  - (A) -sin1

(B) 0

(C) 1

- (D) sin 1
- Let  $f:[0,1] \to R$  be such that f(xy) = f(x) f(y) for all  $x,y \in [0,1]$ , and  $f(0) \neq 0$ . If 63. y = y(x) satisfies the differential equation,  $\frac{dy}{dx} = f(x)$  with y(0) = 1, then  $y(\frac{1}{4}) + y(\frac{3}{4})$  is equal to
  - (A) 4

(C) 5

- (B) 3 (D) 2
- If  $x = \sin^{-1}(\sin 10)$  and  $y = \cos^{-1}(\cos 10)$ , then y x is equal to: 64.
  - (A) π

(B)  $7\pi$ 

(C) 0

- (D) 10
- If  $0 \le x < \frac{\pi}{2}$ , then the number of values of x for which  $\sin x \sin 2x + \sin 3x = 0$ , is 65.
  - (A) 2

(C) 3

- (D) 4
- Let  $z_0$  be a root of the quadratic equation,  $x^2 + x + 1 = 0$ . If  $z = 3 + 6iz_0^{81} 3iz_0^{93}$ , then argz66. is equal to
  - (A)  $\frac{\pi}{4}$

(B)  $\frac{\pi}{3}$ 

(C) 0

- (D)  $\frac{\pi}{6}$
- The area of the region A  $\{(x,y): 0 \le y \le x |x| + 1 \text{ and } -1 \le x \le 1\}$  in sq. units, is: 67.
  - (A)  $\frac{2}{3}$

(C)2

(D)  $\frac{4}{3}$ 

68.	If the system of linear equation $x$ consistent, then: (A) $g+h+k=0$ (C) $g+h+2k=0$	-4y + 7z = g, $3y - 5z = h$ , $-2x + 5y - 9z = k$ is (B) $2g + h + k = 0$ (D) $g + 2h + k = 0$	
69.	The coefficient of $t^4$ in the expansion of $\left(\right.$	$\left(\frac{1-t^6}{1-t}\right)^3$ is	
	(A) 12 (C) 10	(B) 15 (D) 14	
70.	If both the roots of the quadratic equation lie in the interval [1, 5], then m lies in the (A) (4, 5) (C) (5, 6)	on $x^2 - 5x + 4 = 0$ are real and distinct and they interval. (B) $(3, 4)$ (D) $(-5, -4)$	
71.	Let S be the set of all triangle in the xy – plane, each having one vertex at the origin and the other two vertices lie on coordinate axes with integral coordinates. If each triangle in S has area 50 sq. units, then the number of elements in the set S is:  (A) 9  (B) 18  (C) 32  (D) 36		
72.	Let a, b and c be the 7 <sup>th</sup> , 11 <sup>th</sup> and 13 <sup>th</sup> terms respectively of a non - constant A.P. If		
	these are also the three consecutive terms of a G.P. then $\frac{a}{c}$ is equal to:		
	(A) $\frac{1}{2}$	(B) 4	
	(C) 2	(D) $\frac{7}{13}$	
73.	The logical statement $\left[ \sim (\sim p \lor q) \lor (p \land r) \land (\sim q \land r) \right]$ is equivalent to:		
	(A) $(p \wedge r) \wedge \sim q$	(B) $(\sim p \land \sim q) \land r$	
	(C) ~p∨r	(D) $(p \land \sim q) \lor r$	
74.	The equation of the plane containing the straight line $\frac{x}{2} = \frac{y}{3} = \frac{z}{4}$ and perpendicular to the		
	plane containing the straight lines $\frac{x}{3} = \frac{y}{4} = \frac{z}{2}$ and $\frac{x}{4} = \frac{y}{2} = \frac{z}{3}$ is:		
	(A) $x + 2y - 2z = 0$	(B) $x - 2y + z = 0$	
	(C) $5x + 2y - 4z = 0$	(D) $3x + 2y - 3z = 0$	
75.	A data consists of n observations:		
	$x_1, x_2, \dots, x_n$ . If $\sum_{i=1}^{n} (x_i + 1)^2 = 9n$ and $\sum_{i=1}^{n} (x_i + 1)^2 = 9n$	$(x_i - 1)^2 = 5n$ , then the standard deviation of this	
	data is:	_	
	(A) 5	(B) √5	
	(C) $\sqrt{7}$	(D) 2	

76. If 
$$A = \begin{bmatrix} e^{t} & e^{-t} \cos t & e^{-t} \sin t \\ e^{t} & -e^{-t} \cos t - e^{-t} \sin t & -e^{-t} \sin t + e^{-t} \cos t \\ e^{t} & 2e^{-t} \sin t & -2e^{-t} \cos t \end{bmatrix}$$
 Then A is

(A) Invertible only if  $t = \frac{\pi}{2}$ 

(B) not invertible for any  $t \in R$ 

(C) invertible for all  $t \in R$ 

(D) invertible only if  $t = \pi$ 

77. If 
$$f(x) = \int \frac{5x^8 + 7x^6}{(x^2 + 1 + 2x^7)^2} dx$$
,  $(x \ge 0)$  and  $f(0) = 0$ , then the value of  $f(1)$  is:

(A)  $-\frac{1}{2}$ 

(B)  $\frac{1}{2}$ 

(C)  $-\frac{1}{4}$ 

(D)  $\frac{1}{4}$ 

78. Let f be a differentiable function R to R such that 
$$|f(x)-f(y)| \le 2|x-y|^{\frac{3}{2}}$$
, for all  $x,y \in R$ . If  $f(0)=1$  then  $\int_{0}^{1} f^{2}(x) dx$  is equal to

(A) 0

(B)  $\frac{1}{2}$ 

(C) 2

(D) 1

79. If 
$$x = 3 \tan t$$
 and  $y = 3 \sec t$ , then the value of  $\frac{d^2y}{dx^2}$  at  $t = \frac{\pi}{4}$ , is:

(A)  $\frac{3}{2\sqrt{2}}$ 

(B)  $\frac{1}{3\sqrt{2}}$ 

(C)  $\frac{1}{6}$ 

(D)  $\frac{1}{6\sqrt{2}}$ 

80. The number of natural numbers less than 7,000 which can be formed by using the digits 0, 1, 3, 7, 9 (repetition of digits allowed) is equal to:

(A) 250

(B) 374

(C) 372

(D) 375

81. If the circles  $x^2 + y^2 - 16x - 20y + 164 = r^2$  and  $(x - 4)^2 + (y - 7)^2 = 36$  intersect at two distinct points, then:

(A) 0 < r < 1

(B) 1<r<11

(C) r > 11

(D) r = 11

82. A hyperbola has its centre at the origin, passes through the point (4, 2) and has transverse axis of length 4 along the x – axis. Then the eccentricity of the hyperbola is:

(A)  $\frac{2}{\sqrt{3}}$ 

(B)  $\frac{3}{2}$ 

(C) √3

(D) 2

83.	Let A(4, -4) and B(9,6) be points on the parabola $y^2=4x$ . Let C be chosen on the arc AOB of the parabola, where O is the origin, such that the area of $\triangle$ ACB is maximum. Then, the area (in sq. units) of $\triangle$ ACB, is:		
	(A) $31\frac{3}{4}$	(B) 32	
	(C) $30\frac{1}{2}$	(D) $31\frac{1}{4}$	
84.	Let the equation of two sides of a triangle orthocentre of this triangle is at $(1, 1)$ , then $(A) 122y - 26x - 1675 = 0$ $(C) 122y + 26x + 1675 = 0$	the equation of its third side is: (B) $26x + 61y + 1675 = 0$ (D) $26x - 122y - 1675 = 0$	
85.	drawn ball is green, then a red ball is adde	A ball is drawn at random from the urn. If the d to the urn and if the drawn ball is red, then a ball is not returned to the urn. Now, a second billity that the second ball is red, is:  (B) $\frac{32}{49}$ (D) $\frac{21}{49}$	
86.	If the lines $x = ay + b$ , $z = cy + d$ and $x = a'$ (A) $cc' + a + a' = 0$ (C) $ab' + bc' + 1 = 0$	z+b', $y=c'z+d'$ are perpendicular, then: (B) $aa'+c+c'=0$ (D) $bb'+cc'+1=0$	
87.	Let $\vec{a} = \hat{i} + \hat{j} + \sqrt{2}\hat{k}$ , $\vec{b} = b_1\hat{i} + b_2\hat{j} + \sqrt{2}\hat{k}$ and $\vec{c}$ projection vector of $\vec{b}$ on $\vec{a}$ is $\vec{a}$ . If $\vec{a} + \vec{b}$ is (A) $\sqrt{22}$ (C) $\sqrt{32}$	$\vec{c} = 5\hat{i} + \hat{j} + \sqrt{2}\hat{k}$ be three vectors such that the sperpendicular to $\vec{c}$ , then $ \vec{b} $ is equal to: (B) 4 (D) 6	
88.	The number of all possible positive integration and possible positive integration of $a^2 - 11x + \alpha = 0$ are respectively. (A) 2 (C) 3	gral values of $\alpha$ for which the roots of the ational numbers is: (B) 5 (D) 4	
89.	Let $A = \{x \in R : x \text{ is not a positive integer}\}$	Define a function $f:A \to R$ as $f(x) = \frac{2x}{x-1}$	
	then f is (A) injective but nor surjective (C) surjective but not injective	(B) not injective (D) neither injective nor surjective	
90.	If $\int_{0}^{\frac{\pi}{3}} \frac{\tan \theta}{\sqrt{2k \sec \theta}} d\theta = 1 - \frac{1}{\sqrt{2}}, (k > 0), \text{ then the value of k is:}$		
	(A) 2	(B) $\frac{1}{2}$	
	(C) 4	(D) 1	

## HINTS AND SOLUTIONS

### PART A - PHYSICS

1. 
$$R = R_0 e^{-\lambda t}$$

$$\therefore \qquad \frac{R_{_B}}{R_{_A}} = \frac{R_{_O}e^{-\lambda_{_B}t}}{R_{_O}e^{-\lambda_{_B}t}} = e^{-(\lambda_{_B}-\lambda_{_A})t} = e^{-3t}$$

$$\Rightarrow \lambda_B - \lambda_A = 3$$

$$\Rightarrow \frac{\ell n^2}{T_R} - \frac{\ell n2}{\ell n2} = 3.$$

$$\Rightarrow$$
  $T_B = \frac{\ell n2}{4}$ 

2. 
$$P_s = \eta P_P$$

$$\Rightarrow$$
  $E_s i_s = \eta E_i i_p$ 

$$\Rightarrow$$
  $i_s = \frac{(0.9)(2300)(5)}{(230)} = 45 \text{ A}.$ 

3. 
$$B = \frac{E}{C}$$

$$\Rightarrow$$
  $U_E = \frac{1}{2} \epsilon_o E^2$ 

$$U_{B} = \frac{B^{2}}{2u_{o}} = \frac{E^{2}}{2u_{o}C^{2}} = \frac{E^{2}}{2u_{o}}(\mu_{o}\varepsilon_{o}) = U_{E}$$

4. 
$$x = 3t^2 + 5$$

$$\Rightarrow$$
 v = 6t

$$\Rightarrow \quad v = 6t$$

$$\Rightarrow \quad \Delta W = \Delta k$$

$$= \frac{1}{2}(2)(30)^2 - \frac{1}{2}2(0)^2$$

5. 
$$eE = evB$$

$$\Rightarrow$$
  $E = \left(\frac{eBr}{m}\right)B$ 

$$\Rightarrow$$
 m =  $\frac{eB^2r}{r}$ 

$$\Rightarrow m = \frac{(1.6 \times 10^{-19}) (0.5)^2 (0.5 \times 10^{-2})}{100} = 2 \times 10^{-24} \text{ kg}.$$

6. 
$$\vec{E} = \frac{kq_1}{r_1^3} \vec{r_1} + \frac{kq_2}{r_2^3} \vec{r_2} = k \times 10^{-6} \left[ \frac{\sqrt{10}}{10\sqrt{10}} (-\hat{i} + 3\hat{j}) + \frac{(-25)}{125} (-4\hat{i} + 3\hat{j}) \right]$$
$$= (9 \times 10^3) \left[ \frac{1}{10} (-\hat{i} + 3\hat{j}) - \frac{1}{5} (-4\hat{i} + 3\hat{j}) \right]$$

$$= (9 \times 10^{3}) \left[ \left( -\frac{1}{10} + \frac{4}{5} \right) \hat{\mathbf{i}} + \left( \frac{3}{10} - \frac{3}{5} \right) \hat{\mathbf{i}} \right] = 9000 \left( \frac{7}{10} \hat{\mathbf{i}} - \frac{3}{10} \hat{\mathbf{j}} \right)$$
$$= (63\hat{\mathbf{i}} - 27\hat{\mathbf{j}}) (100)$$

7. 
$$t = G^{a} h^{b} c^{c}$$

$$\Rightarrow M^{o} L^{o} T' = (M^{-1} L^{3} T^{-2})^{a} (ML^{2}T^{-1})^{b} (LT^{-1})^{c}$$

$$\Rightarrow -a + b = 0 \Rightarrow a = b$$

$$\Rightarrow 3a + 2b + c = 0$$

$$\Rightarrow c = -5a$$

$$\Rightarrow -2a - b - c = 1$$

$$\Rightarrow a = \frac{1}{2}; b = \frac{1}{2}; c = -\frac{5}{2}$$

8. 
$$V_{O_i} = 12 - 0.3 = 11.7 \text{ V}$$
  
 $V_{O_i} = 12 - 0.7 = 11.3 \text{ V}$   
 $\Rightarrow \Delta V_{O} = -0.4 \text{ V}$ 

9. 
$$\frac{dV}{dt} = Av \implies \frac{dV}{dt} = A\sqrt{2gh}$$

$$\Rightarrow \frac{0.74}{60} = (3.14) \left(\frac{2}{100}\right)^2 \sqrt{2(9.8)h}$$

$$\Rightarrow h = 4.92 \text{ m}$$

$$10. \qquad E_1 = -\frac{GMm}{R+h} - \left(-\frac{GMm}{R}\right)$$
 
$$E_2 = \frac{1}{2}m\left(\sqrt{\frac{GM}{R+h}}\right)^2 = \frac{GMm}{2(R+h)}$$
 
$$E_1 = E_2 \quad ; \quad h = \frac{R}{2}$$

11. 
$$W_1 = W_2$$
  
 $\Rightarrow 600 - T_2 = T_2 - 400$   
 $\Rightarrow T_2 = 500 \text{ K}$ 

12. 
$$E = Pt = \frac{E^2}{Z^2}Rt = \frac{(24)^2}{60^2 + (8.33\pi - 2\pi)^2}(60)(60) = 518 \text{ J}.$$

13. PE = KE  

$$\Rightarrow \frac{1}{2}m\omega^{2}(A^{2} - x^{2}) = \frac{1}{2}m\omega^{2}x^{2}$$

$$\Rightarrow x = \frac{A}{\sqrt{2}}$$

- 14.  $T \cos 45^\circ = mg$   $T \sin 45^\circ = F$  $\Rightarrow F = mg = 100 \text{ N}.$
- 15.  $\Delta Q = \frac{f}{2} nR\Delta T$  $= \frac{5}{2} \left(\frac{15}{28}\right) (8.3) (1200 300) = 10000 \text{ J}.$
- 16.  $\Delta X_{\text{max}} = d \sin \theta = 0.32 \sin 30 = 0.16 \text{ mm}$

$$\therefore n = \frac{\Delta X_{\text{max}}}{\lambda} = \frac{0.16 \times 10^{-3}}{500 \times 10^{-9}}$$
$$= \frac{0.16 \times 10^{6}}{500} = \frac{1600}{5} = 320$$

 $\therefore$  Number of BFs = (2n + 1) = 641

17. 
$$\theta = 60^{\circ}$$

18. 
$$mg \frac{\ell}{2} \left( \frac{1}{2} \right) = \frac{1}{2} \left( \frac{m\ell^2}{3} \right) \omega^2$$

$$\Rightarrow \omega = \sqrt{\frac{3g}{2\ell}} = \sqrt{30}$$

19.  $R = 530 \text{ k}\Omega \pm 5\%$ 

20. 
$$B_{L} = \frac{\mu_{o}i}{2R}$$

$$B_{C} = \frac{\mu_{o}Ni}{2(R/N)}$$

$$\therefore \frac{B_{L}}{B_{C}} = \frac{1}{N^{2}}$$

21. 
$$f = \frac{1}{2\pi} \sqrt{\frac{C}{\left(\frac{ML^{2}}{3}\right)}} & 0.8 \text{ f} = \frac{1}{2\pi} \sqrt{\frac{C}{\left(\frac{ML^{2}}{3} + \frac{mL^{2}}{2}\right)}}$$

$$\Rightarrow \frac{25}{16} = \frac{\frac{ML^{2}}{3} + \frac{mL^{2}}{2}}{\frac{ML^{2}}{3}}$$

$$\Rightarrow \frac{25}{16} = 1 + \frac{3 \text{ m}}{2 \text{ M}}$$

$$\Rightarrow \frac{9}{16} = \frac{3 \text{ m}}{2 \text{ M}}$$

$$\Rightarrow \frac{m}{M} = \frac{3}{8} = 0.37$$

22. 
$$Q = \int \rho 4\pi r^2 dr = \int_0^R \left(\frac{A}{r^2} e^{-\frac{2r}{a}}\right) (4\pi r^2) dr$$
$$= 4\pi A \frac{a}{2} \left(1 - e^{\frac{-2R}{a}}\right)$$
$$\Rightarrow R = \frac{-a}{2} log \left(1 - \frac{Q}{2\pi Aa}\right)$$

23. 
$$C_{1} = \frac{\varepsilon_{0}K_{1}\frac{L^{2}}{2}}{\frac{d}{2}} + \frac{\varepsilon_{0}K_{3}\frac{L^{2}}{2}}{\left(\frac{d}{2}\right)} = \frac{\varepsilon_{0}L^{2}}{d}(K_{1} + K_{3})$$

$$C_{2} = \frac{\varepsilon_{0}K_{2}\frac{L^{2}}{2}}{\frac{d}{2}} + \frac{\varepsilon_{0}K_{4}\frac{L^{2}}{2}}{\frac{d}{2}} = \frac{\varepsilon_{0}L^{2}}{d}(K_{2} + K_{4})$$

$$\therefore \frac{1}{c} = \frac{1}{c_{1}} + \frac{1}{c_{2}}$$

$$\Rightarrow \frac{d}{\varepsilon_{0}KL^{2}} = \frac{d}{\varepsilon_{0}L^{2}(K_{1} + K_{3})} + \frac{d}{\varepsilon_{0}L^{2}(K_{2} + K_{4})}$$

24. Zero error = 
$$0 + 3 \times \frac{0.5 \text{ mm}}{100} = 0.015 \text{ mm}$$
  
MSR =  $5.5 + 48 \times \frac{0.5}{100}$   
=  $5.74 \text{ mm}$ .  
 $\therefore$  Thickness =  $5.74 - 0.015 = 5.725 \text{ mm}$ 

25. 
$$f = \frac{2}{2\ell} v_s = \frac{330}{0.5} = 660 \text{ Hz}$$

$$f' = f\left(\frac{v_s + v}{v_s}\right) = (660) \left(\frac{330 + \frac{50}{18}}{330}\right) = 660 \left(1 + \frac{50}{18 \times 330}\right)$$
$$= 666 \text{ Hz.}$$

$$\begin{aligned} 26. \qquad & \sqrt{\frac{2\ell}{a_2}} - \sqrt{\frac{2\ell}{a_1}} = t & \qquad \Rightarrow \qquad & \frac{\sqrt{2\ell}}{t} = \frac{\sqrt{a_1 a_2}}{\sqrt{a_1} - \sqrt{a_2}} \\ & \sqrt{2a_1\ell} - \sqrt{2a_2\ell} = v & \qquad \Rightarrow \qquad & \frac{\sqrt{2\ell}}{v} = \frac{1}{\sqrt{a_1} - \sqrt{a_2}} \\ & \Rightarrow \quad & \frac{v}{t} = \sqrt{a_1 a_2} & \qquad \Rightarrow \qquad v = (\sqrt{a_1 a_2}) t \end{aligned}$$

27. 
$$\begin{aligned} \text{KE}_{\text{max}} &= h\nu_{\text{max}} - \phi \\ &= \frac{\left(6.6 \times 10^{-34}\right) \left(6.28 \times 10^{7}\right) \left(3 \times 10^{8}\right)}{1.6 \times 10^{-19} \times 2 \times 3.14} - 4.7 \\ &= 12.37 - 4.7 = 7.67 \text{ eV} \end{aligned}$$

28. 
$$\frac{12}{400} = \frac{6}{600} + \frac{6}{R_{2}}$$

$$\Rightarrow \frac{1}{200} = \frac{1}{600} + \frac{1}{R_{2}}$$

$$\Rightarrow R_{2} = 300 \Omega$$

29. 
$$f = \frac{c}{\lambda} = \frac{3 \times 10^8}{8 \times 10^{-7}} = \frac{3}{8} \times 10^{15} \text{Hz}$$

$$\therefore \qquad n = \frac{(0.01) \text{ f}}{6 \times 10^6} = \frac{\frac{3}{8} \times 10^{13}}{6 \times 10^6}$$

$$= \frac{1}{16} \times 10^7 = 6.25 \times 10^5$$

30. 
$$v_{x} = \frac{dx}{dt} = -a\omega \sin \omega t$$

$$v_{y} = \frac{dy}{dt} = a\omega \cos \omega t$$

$$v_{z} = \frac{dz}{dt} = a\omega$$

$$\therefore v = \sqrt{v_{x}^{2} + v_{y}^{2} + v_{z}^{2}} = a\omega \sqrt{2}$$

### **PART B - CHEMISTRY**

31. 
$$H_2O(s) \longrightarrow H_2O(\ell) \longrightarrow H_2O(\ell) \longrightarrow H_2O(g) \longrightarrow H_2O(g)$$

1 kg 1 kg 1 kg
at 273 K at 273 K at 373 K at 373 K at 383 K
$$\Delta S = \Delta S_1 + \Delta S_2 + \Delta S_3 + \Delta S_4$$

$$= \frac{334}{273} + 4.2\ell n \frac{373}{273} + \frac{2491}{373} + 2\ell n \frac{383}{373} = 9.267 \text{ kJ Kg}^{-1} \text{ K}^{-1}$$

32. 
$$2C_{57}H_{110}O_{6}(s) + 163O_{2}(g) \longrightarrow 114CO_{2}(g) + 110H_{2}O(I)$$

$$\frac{\text{Moles of }C_{57}H_{110}O_{6}}{2} = \frac{\text{Moles of }H_{2}O}{110}$$

$$\frac{\frac{445}{890}}{2} = \frac{\frac{\text{Mass of }H_{2}O}{18}}{110}$$

$$\text{Mass of }H_{2}O = 495 \text{ g}$$

33. 
$$\begin{array}{c} O \\ || \\ Ph-C-CH_3 \xrightarrow{NaOH} \\ \end{array} \\ \begin{array}{c} O \\ || \\ \ominus \\ \end{array} \\ \begin{array}{c} O^- \\ || \\ \rightarrow \\ \end{array} \\ \begin{array}{c} Ph-C-CH_2 \\ \longleftarrow Ph-C=CH_2 \\ \end{array}$$
 enolate ion

34. Fact based

35.

36. Nucleophilicity of NH<sub>2</sub>> OH

37. 
$$\begin{array}{c} OH \\ NH_2 \\ \hline \\ Br_2/hv \\ \hline \\ Br \\ \hline \\ KOH \\ \hline \\ CH_3 \\ \end{array}$$

- 38. Acetonitrile is used as mobile phase for most of the reverse chromatography. Benzaldehyde is adsorbed on alumina.
- 39. The only alkali metal which forms nitride by reacting directly with N<sub>2</sub> is 'Li'.
- 40. As<sub>2</sub>S<sub>3</sub> is a negatively charged sol. so AlCl<sub>3</sub> will be most effective.
- 41. As CN<sup>-</sup> is a strong field ligand. K<sub>3</sub>[Co(CN)<sub>6</sub>] will have maximum 'Δ'.
- 42. Fact based.

43. 
$$A_{2}(g) + B_{2}(g) \xrightarrow{K_{1}} 2 AB(g) \qquad \dots \dots (1)$$

$$6 AB(g) \xrightarrow{K_{2}} 3 A_{2}(g) + 3 B_{2}(g) \qquad \dots \dots (2)$$

$$Reaction(2) = -3 \times reaction(1)$$

$$\therefore K_{2} = \left(\frac{1}{K_{1}}\right)^{3} \Rightarrow K_{2} = K_{1}^{-3}$$

$$\begin{array}{c|c} Me & Me & OH \\ H_2N & & & \\ OH & OH \\ OH & O \\ \end{array}$$

45.  $2A + B \longrightarrow products$ 

Rate = 
$$K[A]^x[B]^y$$

$$r = K[A]^x[B]^y - - - - (i)$$

$$0.3 = K[A]^{x}[B]^{y} - - - (1)$$

$$2.4 = K[2A]^{x}[2B]^{y} - - - (2)$$

$$0.6 = K[2A]^{x}[B]^{y} - - - (3)$$

$$x = 1, y = 2$$

Overall order = 
$$2 + 1 = 3$$

Order w.r.t 
$$A = 1$$

Order w.r.t 
$$B = 2$$

47. ∴ -COCH<sub>3</sub> is present it will show both 2, 4-DNP & iodoform test.

Due to steric inhibition of resonance. I.P of 'N' is not involved in delocalization so coupling reaction will not take place.

48. 
$$Zn(s) + Cu^{2+}(aq) \Longrightarrow Zn^{2+}(aq) + Cu(s)$$
  
 $-nFE_{cell} = -RT\ell nK$   
 $\ell nK = \frac{2 \times 96500 \times 2}{8 \times 300} = 160.83$   
 $K = e^{160}$ 

49. Fact based.

50. NO
$$\longrightarrow$$
NO $^+$  N $_2\longrightarrow$ N $_2^+$ 
B.O 0.5 3 B.O 3 2.5
Para Dia Dia Para
O $_2\longrightarrow$ O $_2^+$  O $_2\longrightarrow$ O $_2^{2-}$ 
B.O 2 2.5 B.O 2 1
Para Para Dia

- 51. Refer Theory
- 52. is anti aromatic
- 53. Refer theory
- 54.  $4 \text{ Al} + 6 \text{ ZnO} \longrightarrow 2 \text{ Al}_2 \text{O}_3 + 6 \text{ Zn}$  $\Delta \text{H}$  for the above reaction is -ve.
- 55. Due to weak metallic bonding.
- 56. Correct order of basic strength is  $NH_2(Et)_2 > EtNH_2 > NMC_3 > Ph NH CH_3$
- 57. 2<sup>nd</sup> electron gain enthalpy of oxygen is positive.

58. 
$$d = \frac{ZM}{N_a a^3}$$
$$= \frac{4 \times 63.55}{6.023 \times 10^{23} \times (x \times 10^{-8})^3} = \frac{422}{x^3} \text{gm/cm}^3$$

59. Let moles of H<sub>2</sub>O separated as ice = x gm  $\Delta T_f = iK_f m$ 

$$10 = 1 \times 1.86 \frac{\frac{62}{62}}{\frac{250 - x}{1000}}$$

x = 64 gm

- 60.  $L_1$   $L_2$   $L_3$  Green Blue Red absorbed wave length Order of  $\lambda$  Red > Green > Blue  $L_3 > L_1 > L_2$ 
  - $\therefore$  Strength of ligand  $\alpha \Delta \alpha 1/\lambda$
  - $\therefore \mbox{ Strength of ligand } L_2 > L_1 > L_3$

### **PART C - MATHEMATICS**

$$\begin{aligned} & 61. \qquad T_n = \frac{\left(3 + \left(n - 1\right) \times 3\right) \left(1^2 + 2^2 + \dots + n^2\right)}{\left(2n + 1\right)} \\ & T_n = \frac{3. \frac{n^2 \left(n + 1\right) \left(2n + 1\right)}{6}}{2n + 1} = \frac{n^2 \left(n + 1\right)}{2} \\ & S_{15} = \frac{1}{2} \sum_{n=1}^{15} \left(n^3 + n^2\right) = \frac{1}{2} \left[ \left(\frac{15 \left(15 + 1\right)}{2}\right)^2 + \frac{15 \times 16 \times 31}{6} \right] \\ & = 7820 \end{aligned}$$

62. 
$$\lim_{x \to 0^{+}} \frac{x([x] + |x|)\sin[x]}{|x|}$$

$$x \to 0^{-}$$

$$|x| = -1$$

$$|x| = -x$$

$$\Rightarrow \lim_{x \to 0^{-}} \frac{x(-x - 1)\sin(-1)}{-x} = -\sin 1$$

63. 
$$f(xy) = f(x).f(y)$$

$$f(0) = 1 \text{ as } f(0) \neq 0$$

$$\Rightarrow f(x) = 1$$

$$\frac{dy}{dx} = f(x) = 1$$

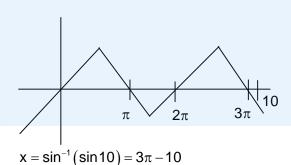
$$\Rightarrow y = x + c$$

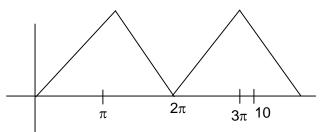
$$At, x = 0, y = 1 \Rightarrow c = 1$$

$$y = x + 1$$

$$\Rightarrow y\left(\frac{1}{4}\right) + y\left(\frac{3}{4}\right) = \frac{1}{4} + 1 + \frac{3}{4} + 1 = 3$$

64.





$$y = \cos^{-1}(\cos 10) = 4\pi - 10$$
  
 $y - x = \pi$ 

65. 
$$\sin x - \sin 2x + \sin 3x = 0$$

$$\Rightarrow (\sin x + \sin 3x) - \sin 2x = 0$$

$$\Rightarrow 2\sin x \cdot \cos x - \sin 2x = 0$$

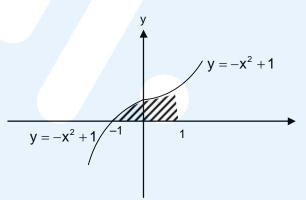
$$\Rightarrow \sin 2x (2\cos x - 1) = 0$$

$$\Rightarrow \sin 2x = 0 \text{ or } \cos x = \frac{1}{2} \Rightarrow x = 0, \frac{\pi}{3}$$

66. 
$$z_0 = \omega$$
 or  $\omega^2$  (where  $\omega$  is a non – real cube root of unity) 
$$z = 3 + 6i(\omega)^{81} - 3i(\omega)^{93}$$
$$z = 3 + 3i$$
$$\Rightarrow arg z = \frac{\pi}{4}$$

67. The graph is a follows

$$\int_{-1}^{0} \left(-x^{2}+1\right) dx + \int_{0}^{1} \left(x^{2}+1\right) dx = 2$$



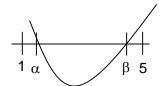
68. 
$$\begin{aligned} P_1 &= x - 4y + 7z - g = 0 \\ P_2 &= 3x - 5y - h = 0 \\ P_3 &= -2x + 5y - 9z - k = 0 \\ \text{Here } \Delta &= 0 \\ 2P_1 + P_2 + P_3 &= 0 \text{ when } 2g + h + k = 0 \end{aligned}$$

69. 
$$(1-t^6)^3 (1-t)^{-3}$$

$$(1-t^{18}-3t^6+3t^{12})(1-t)^{-3}$$

$$\Rightarrow \text{ coefficient of } t^4 \text{ in } (1-t)^{-3} \text{ is } {}^{3+4-1}C_4 = {}^6C_2 = 15$$

70. 
$$x^2 - mx + 4 = 0$$
$$\alpha, \beta \in \begin{bmatrix} 1,5 \end{bmatrix}$$



(1) 
$$D > 0 \Rightarrow m^2 - 16 > 0$$
$$\Rightarrow m \in (-\infty, -4) \cup (4, \infty)$$

(2) 
$$f(1) \ge 0 \Rightarrow 5 - m \ge 0 \Rightarrow m \in (-\infty, 5]$$

$$(3) \hspace{1cm} f\left(5\right) \geq 0 \Rightarrow 29 - 5m \geq 0 \Rightarrow m \in \left(-\infty, \frac{29}{5}\right]$$

$$(4) 1 < \frac{-b}{2a} < 5 \Rightarrow 1 < \frac{m}{2} < 5 \Rightarrow m \in (2,10)$$
$$\Rightarrow m \in (4,5)$$

No option correct: Bonus

71. Let  $A(\alpha,0)$  and  $B(0,\beta)$  be the vectors of the given triangle AOB

$$\Rightarrow |\alpha\beta| = 100$$

 $\Rightarrow$  Number of triangles

= 4 × (number of divisors of 100)

$$= 4 \times 9 = 36$$

72. 
$$a = A + 6d$$

$$b = A + 10d$$

$$c = A + 12d$$

a, b, c are in G.P.

$$\Rightarrow (A + 10d)^2 = (A + 6d)(a + 12d)$$

$$\Rightarrow \frac{A}{d} = -14$$

$$\frac{a}{c} = \frac{A + 6d}{A + 12d} = \frac{6 + \frac{A}{d}}{12 + \frac{A}{d}} = \frac{6 - 14}{12 - 14} = 4$$

<sup>\*</sup> If we consider  $\alpha, \beta \in (1, 5)$  then option (1) is correct.

74. Vector along the normal to the plane containing the lines  $\frac{x}{3} = \frac{y}{4} = \frac{z}{2}$  and  $\frac{x}{4} = \frac{y}{2} = \frac{z}{3}$  is  $\left(8\hat{i} - \hat{j} - 10\hat{k}\right)$ .

Vector perpendicular to the vectors  $2\hat{i} + 3\hat{j} + 4\hat{k}$  and  $8\hat{i} - \hat{j} - 10\hat{k}$  is  $26\hat{i} - 52\hat{j} + 26\hat{k}$ So, required plane is  $26x - 52y + 26z = 0 \implies x - 2y + z = 0$ 

- - $\Rightarrow \frac{\sum x_i}{n} = 1$
  - $\Rightarrow$  variance = 6 1 = 5
  - $\Rightarrow$  standard diviation =  $\sqrt{5}$
- 76.  $|A| = e^{-t} \begin{vmatrix} 1 & \cos t & \sin t \\ 1 & -\cos t \sin t & -\sin t + \cos t \\ 1 & 2\sin t & -2\cos t \end{vmatrix}$  $= e^{-t} \left[ 5\cos^2 t + 5\sin^2 t \right] \forall t \in R$  $= 5e^{-t} \neq 0 \ \forall t \in R$
- 77.  $\int \frac{5x^8 + 7x^6}{\left(x^2 + 1 + 2x^7\right)^2} dx$   $= \int \frac{5x^{-6} + 7x^{-8}}{\left(\frac{1}{x^7} + \frac{1}{x^5} + 2\right)^2} dx = \frac{1}{2 + \frac{1}{x^5} + \frac{1}{x^7}} + C$   $As f(0) = 0, f(x) = \frac{x^7}{2x^7 + x^2 + 1}$   $f(1) = \frac{1}{4}$
- 78.  $|f(x) f(y)| \le 2|x y|^{3/2}$  divide both side by |x y|  $|\frac{f(x) f(y)}{x y}| \le 2.|x y|^{1/2}$

Apply limit 
$$x \to y$$
  
 $|f'(y)| \le 0 \Rightarrow f'(y) = 0 \Rightarrow f(y) = c \Rightarrow f(x) = 1$   

$$\int_{0}^{1} 1. dx = 1$$

79. 
$$\frac{dx}{dt} = 3\sec^2 t$$

$$\frac{dy}{dt} = 3\sec t \tan t$$

$$\frac{dy}{dx} = \frac{\tan t}{\sec t} = \sin t$$

$$\frac{d^2y}{dx^2} = \cos t \frac{dt}{dx}$$

$$= \frac{\cos t}{3\sec^2 t} = \frac{\cos^3 t}{3} = \frac{1}{3.2\sqrt{2}} = \frac{1}{6\sqrt{2}}$$

80. 
$$a_1 a_2 a_3$$

Number of numbers  $= 5^3 - 1$ 

$$\begin{bmatrix} a_4 & a_1 & a_2 & a_3 \end{bmatrix}$$

2 ways for a<sub>4</sub>

Numbers of numbers =  $2 \times 5^3$ 

Required number  $0020 = 5^3 + 2 \times 5^3 - 1 = 374$ 

81. 
$$x^{2} + y^{2} - 16x - 20y + 164 = r^{2}$$

$$A(8,10), R_{1} = r$$

$$(x-4)^{2} + (y-7)^{2} = 36$$

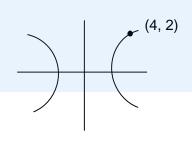
$$B(4,7), R_{2} = 6$$

$$|R_{1} - R_{2}| < AB < R_{1} + R_{2}$$

$$\Rightarrow 1 < r < 11$$

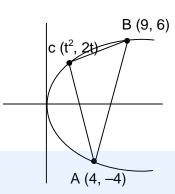
82. Given hyperbola is 
$$\frac{x^2}{4} - \frac{y^2}{b^2} = 1$$
Satisfying the point (4, 2) 
$$\Rightarrow b^2 = \frac{4}{3}$$

$$\Rightarrow e = \frac{2}{\sqrt{3}}$$



83. For maximum area, tangent at the point c must be parallel to chord BC.

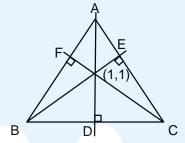
$$\therefore t = \frac{1}{2}$$



84. Equation of AB is 3x - 2y + 6 = 0Equation of AC is 4x + 5y - 20 = 0. Equation of BE is 2x + 3y - 5 = 0

Equation of CF is 5x - 4y - 1 = 0

 $\Rightarrow$  Equation of BC is 26x - 122y = 1675



85. E<sub>1</sub>: Event of drawing a Red ball and placing a green ball in the bag

E2: Event of drawing a green ball and placing a red ball in the bag

E : Event of drawing a red ball in second draw  $P(E) = P(E_1) \times P\left(\frac{E}{E_1}\right) + P(E_2) \times P\left(\frac{E}{E_2}\right)$ 

$$=\frac{5}{7}\times\frac{4}{7}+\frac{2}{7}\times\frac{6}{7}=\frac{32}{49}$$

86. Line x = ay + b, z = cy + d

$$\Rightarrow \frac{x-b}{a} = \frac{y}{1} = \frac{z-d}{c}$$

Line x = a'z + b', y = c'z + d'

$$\Rightarrow \frac{x-b'}{a'} = \frac{y-d'}{c'} = \frac{z}{1}$$

Given both the lines are perpendicular

$$\Rightarrow$$
 aa'+ c'+ c = 0

87. Projection of  $\vec{b}$  on  $\vec{a} = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}|} = |\vec{a}|$ 

$$\Rightarrow b_1 + b_2 = 2 \qquad (1)$$

and 
$$(\vec{a} + \vec{b}) \perp \vec{c} \Rightarrow (\vec{a} + \vec{b}) \cdot \vec{c} = 0$$

$$\Rightarrow 5b_1 + b_2 = -10 \qquad \dots (2)$$

from (1) and (2)  $\Rightarrow$  b<sub>1</sub> = -3 and b<sub>2</sub> = 5

then 
$$|\vec{b}| = \sqrt{b_1^2 + b_2^2 + 2} = 6$$

88. D must be perfect square

$$\Rightarrow$$
 121 – 24 $\alpha = \lambda^2$ 

 $\Rightarrow$  maximum value of  $\alpha$  is 5

$$\alpha = 1 \Longrightarrow \lambda \notin I$$

$$\alpha=2\Longrightarrow \lambda\not\in I$$

$$\alpha = 3 \Rightarrow \lambda \in I$$

⇒ 3 integral values

$$\alpha=4\Rightarrow\lambda\in I$$

$$\alpha = 5 \Rightarrow \lambda \in I$$

89.  $f(x) = 2\left(1 + \frac{1}{x-1}\right)$ 

$$f'(x) = -\frac{2}{(x-1)^2}$$

 $\Rightarrow$  f is one – one but not onto

90.  $\frac{1}{\sqrt{2k}} \int\limits_0^{\pi/3} \frac{\tan \theta}{\sqrt{\sec \theta}} \, d\theta = \frac{1}{\sqrt{2k}} \int\limits_0^{\pi/3} \frac{\sin \theta}{\sqrt{\cos \theta}} \, d\theta$ 

$$= -\frac{1}{\sqrt{2k}} 2 \sqrt{\cos \theta} \Big|_0^{\pi/3} = -\frac{\sqrt{2}}{\sqrt{k}} \left( \frac{1}{\sqrt{2}} - 1 \right)$$

$$\Rightarrow k = 2$$