of four marks each and two questions of two marks each, two questions

Section B: Internal choice has been provided in one question of two ma. ... and one question of four marks.

Section C: Internal choice has been provided in one question of two marks and one question of four marks.

All working, including rough work, should be done on the same sheet as, and adjacent to the rest of the answer.

The intended marks for questions or parts of questions are given in brackets [].

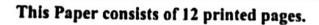
Mathematical tables and graph papers are provided.

SECTION A - 65 MARKS

Question 1

In subparts (i) to (x) choose the correct options and in subparts (xi) to (xv), answer the questions as instructed.

- (i) Let L be a set of all straight lines in a plane. The relation R on L defined as [1] 'perpendicular to' is:
 - (a) Symmetric and Transitive
 - (b) Transitive
 - (c) Symmetric
 - (d) Equivalence
- (ii) The order and the degree of differential equation $1 + \left(\frac{dy}{dx}\right)^2 = \frac{d^2y}{dx^2}$ are: [1]
 - (a) 2 and $\frac{3}{2}$
 - (b) 2 and 3
 - (c) 3 and 4
 - (d) 2 and 1



1224-860 © Copyright reserved.

Turn over

(iii) Let A be a non-empty set.
$$A > \{a, b\}$$
 $J = \{(a, a), (b, b), (b, b)\}$ [1]

Statement 1: Identity relation on A is Reflexive.

Statement 2: Every Reflexive relation on A is an Identity relation.

- (a) Both the statements are true.
- (b) Both the statements are false.

Statement 1 is true and Statement 2 is false.

- (d) Statement 1 is false and Statement 2 is true.
- (iv) The graph of the function f is shown below.

Of the following options, at what values of x is the function f NOT differentiable?

(a) At
$$x = 0$$
 and $x = 2$

- (b) At x = 1 and x = 3
- (c) At x = -1 and x = 1
- (d) At x = -1.5 and x = 1.5

(v) The value of cosec
$$\left(\sin^{-1}\left(\frac{-1}{2}\right)\right) - \sec\left(\cos^{-1}\left(\frac{-1}{2}\right)\right)$$
 is equal to:

(a) -4 (osee $\left(\cos^{-1}\left(-2\right)\right) - \sec\left(\sec^{-1}\left(-2\right)\right)$

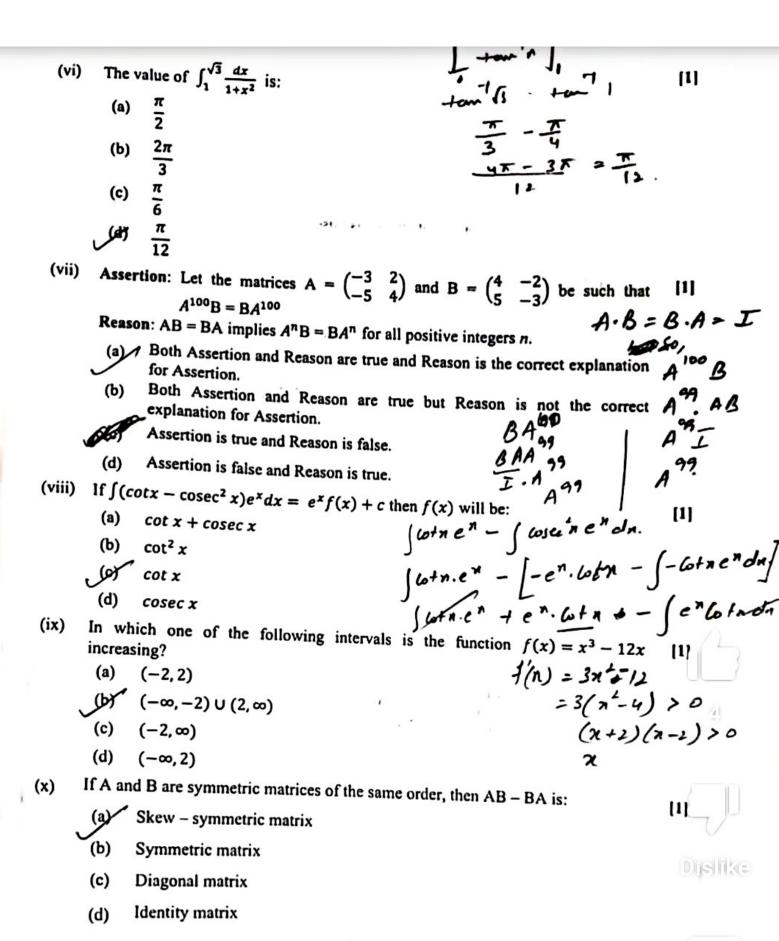
(b) 0

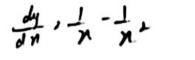
= $-2 - (-2)$

(c) -1

= $-2 + 2$

[1]



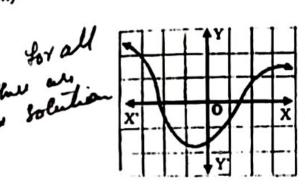


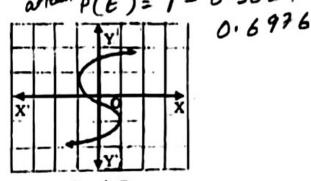
Find the derivative of $y = \log x + \frac{1}{x}$ with respect to x. (xi)

[1]

[1]

- Teena is practising for an upcoming Rifle Shooting tournament. The probability of her shooting the target in the 1st, 2nd, 3rd and 4th shots are 0.4, 0.3, 0.2 and 0.1 (xii) respectively. Find the probability of at least one shot of Teena hitting the target.
- Which one of the following graphs is a function of x? (xiii)
- alleast P(E)= 1-0.3024





(xiv) Evaluate:
$$\int_0^6 |x+3| dx$$

$$[x^2 + 3n]_0^6 = 54$$

- (xv)
 - Given that $\frac{1}{y} + \frac{1}{x} = \frac{1}{12}$ and y decreases at a rate of 1 cms^{-1} , find the rate of change of x when x = 5 cm and y = 1 cm

Question 2 domain Range
$$f(x) = \frac{5}{3x+1}$$
 is invertible. Find $f^{-1}(x)$

(i) Let $f: R - \left\{-\frac{1}{3}\right\} \to R - \{0\}$ be defined as $f(x) = \frac{5}{3x+1}$ is invertible. Find $f^{-1}(x)$

OR $y = \frac{5}{3x+1}$ $\begin{vmatrix} 3ny+y=5\\ 3ny \end{vmatrix} = 5$

(ii) If $f: R \to R$ is defined by $f(x) = \frac{2x-7}{4}$, show that $f(x)$ is one - one and onto.

- - put at b ER.

$$\begin{array}{c|c}
 & 4 & b & ER. \\
 & 4(a) = f(b) \\
 & 3a - 7 = 3b - 7 \\
 & 3a = 3b
\end{array}$$

$$\begin{array}{c|c}
 & 3a - 7 = 3b - 7 \\
 & 3a = 3b
\end{array}$$

Question 3
$$\frac{3a-7}{4} = \frac{3b-7}{4}$$
 $\frac{3a-3b}{a \cdot b \cdot c}$

Find the value of the determinant given below, without expanding it at any stage.

given below, without expanding it at any stage
$$\begin{vmatrix} \beta \gamma & 1 & \alpha(\beta + \gamma) \\ \gamma \alpha & 1 & \beta(\gamma + \alpha) \end{vmatrix}$$



Find the derivative of $y = \log x + \frac{1}{x}$ with respect to x. (xi)

[1]

[1]

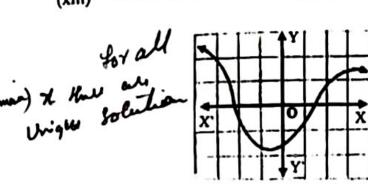
Teena is practising for an upcoming Rifle Shooting tournament. The probability of her shooting the target in the 1st, 2nd, 3rd and 4th shots are 0.4, 0.3, 0.2 and 0.1 (xii) respectively. Find the probability of at least one shot of Teena hitting the target.

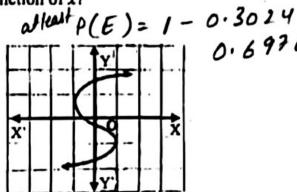
P(A BC D) = 0.6 × 0.716

Which one of the following graphs is a function of x? (xiii)

Graph A

[1]





Graph B $[\chi^2 + 3\pi]_0^6 = 54$

- (xiv) Evaluate: $\int_0^6 |x+3| dx$
- Given that $\frac{1}{y} + \frac{1}{x} = \frac{1}{12}$ and y decreases at a rate of 1 cms^{-1} , find the rate of change [1] of x when x = 5 cm and y = 1 cm $\frac{y}{y} \frac{dy}{dx} = -\frac{1}{x} \frac{dy}{dx} = 0$ $\frac{-1}{x} \frac{dy}{dx} = \frac{1}{x} \frac{dy}{dx} = 0$ $\frac{-1}{x} \frac{dy}{dx} = \frac{1}{x} \frac{dy}{dx} = 0$ $\frac{-1}{x} \frac{dy}{dx} = \frac{1}{x} \frac{dy}{dx} = 0$

OR $y = \frac{5}{3n+1} \begin{vmatrix} 3ny+y=5 \\ 3ny \cdot 5-3 \\ 7 = \frac{5-y}{4} \end{vmatrix}$ (ii) If $f: R \to R$ is defined by $f(x) = \frac{2x-7}{4}$, show that f(x) is one - one and onto.

(ii) If
$$f: R \to R$$
 is defined by $f(x) = \frac{2x-7}{4}$, show that $f(x)$ is one - one and onto.

put $a + b \notin R$.

$$f(a) = f(b)$$

$$3a - 7 = 3b - 7$$
Question 3

Find the value of the determinant given below, without expanding it at any stage.

$$\begin{vmatrix} \beta \gamma & 1 & \alpha(\beta + \gamma) \\ \gamma \alpha & 1 & \beta(\gamma + \alpha) \end{vmatrix}$$

$$\begin{vmatrix} \beta \gamma & 1 & \alpha(\beta + \gamma) \\ \gamma \alpha & 1 & \beta(\gamma + \alpha) \\ \alpha \beta & 1 & \gamma(\alpha + \beta) \end{vmatrix}$$

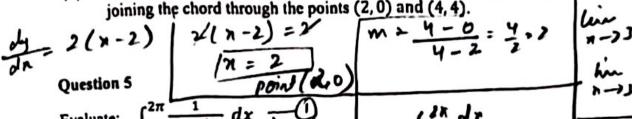
(i) Determine the value of k for which the following function is continuous at x = 3.

$$f(x) = \begin{cases} \frac{(x+3)^2 - 36}{x-3} & ; & x \neq 3 \\ k & ; & x = 3 \end{cases}$$

$$K = \lim_{n \to 3} \frac{(n+1)^2 - 36}{n-2}$$

$$\lim_{n \to 3} \frac{(n+1)^2 - 6}{n-3}$$

(ii) Find a point on the curve $y = (x-2)^2$ at which the tangent is parallel to the line joining the chord through the points (2,0) and (4,4).



Evaluate:
$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}} dx \frac{1}{1 + e^{\sin x}} dx$$

$$P(A \cup B) = P(A) \cdot P(B) - P(A \cap B)$$

$$= \frac{1}{13} \cdot \frac{1}{13} - \frac{2}{13} \cdot \frac{1}{13}$$
Question 7

If y = 3 cos(log x) + 4 sin(log x), show that
$$x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + y = 0$$

Question 8
$$4'' - 3 \frac{\log n}{2} = \frac{1}{2} \left[-3 \frac{\sin \log n}{2} + 4 \frac{\cos \log n}{2} \right]$$

(i) Solve for x: $\sin^{-1}(\frac{x}{2}) + \cos^{-1}x = \frac{\pi}{6}$ $y'' = -5i \frac{\log x}{2} - 7 \frac{\log x}{2}$

(ii) If
$$\sin^{-1}x + \sin^{-1}y + \sin^{-1}z = \pi$$
, show that $x^2 - y^2 - z^2 + 2yz\sqrt{1 - x^2} = 0$
Example in Schaul Book

Question 9

(i) Evaluate: $\int x^2 \cos x \, dx$

$$\frac{\text{Turn over}}{\lambda^2 = 1 - (n = 2)}$$

Sinta + Sinty + Sintx = T Sin x = A , siny = 0 , sin x = C 22 SinA + y = bin 8, z = she B+ A = x - 6 Sm(A+B) = Sh (x-E) SIN BY CONTRACT SAND y. Vietzyisa SINA COIB + COIA SINB = SIN C 2 VI-y2 +yVI-2 = 2. 2 JI-y2 , 2 - y JI-x2 sq. both Gal. x+(1-y2) = (x - y/1-x2)2 nt-xy = x++y-(1-n+)-2y x VI-n+ x- xig-x-y+ xig+2yz 1-x= 0. Qqui I= (x'Cosndn. لل کیا I = nt sinn - \int 2n. Sinn dn.

I = nt sinn - 2 \int n hin dn. I = n' fin n - 2 [- n win + swindn] \(\lambda + 2\right) = 2. I- n2 Sinx - 2[-x6sx + hix] + c I = 7 Sinx + 27 COSH - 2 Finn + C 13 +an / (x==)+c. I = 1 \(\frac{2(2+7)}{2\frac{1}{2}44442} \) dr. $\mathcal{I} \leftarrow \mathcal{I} \left(\frac{3x+4}{2^{2}+3x+4} \right)$ Subscribe I= 1 wg (n+4x++) + " 1 dn

(ii) Evaluate: $\int \frac{x+7}{x^2+4x+7} dx$

Question 10

[4]

A jewellery seller has precious gems in white and red colour which he has put in three boxes. The distribution of these gems is shown in the table given below:

Box	Number of Gems		
	White	Red	
1	1	2	
II	2	3	
Ш	3	1	

He wants to gift two gems to his mother. So, he asks her to select one box at random and pick out any two gems one after the other without replacement from the selected box. The mother selects one white and one red gem.

Calculate the probability that the gems drawn are from Box II.

Question 11

[6]

A furniture factory uses three types of wood namely, teakwood, rosewood and satinwood for manufacturing three types of furniture, that are, table, chair and cot. The wood requirements (in tonnes) for each type of furniture are given below:

	Table 2	Chair Y	Cot Z
Teakwood 🏚	2 12	3	4
Rosewood 🕏	1	1	2
Satinwood #	3	2	1

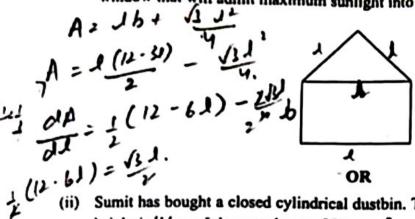
It is found that 29 tonnes of teakwood, 13 tonnes of rosewood and 16 tonnes of satinwood are available to make all three types of furniture.

Using the above information, answer the following questions:

- the above information, answer the following questions:

 Express the data given in the table above in the form of a set of simultaneous (i) equations.
- Solve the set of simultaneous equations formed in subpart (i) by matrix method. (ii)
- Hence, find the number of table(s), chair(s) and cot(s) produced. (iii)

(i) Mrs. Roy designs a window in her son's study room so that the room gets maximum sunlight. She designs the window in the shape of a rectangle surmounted by an equilateral triangle. If the perimeter of the window is 12 m, find the dimensions of the window that will admit maximum sunlight into the room.



- P= 31 + 26

 12:31 + 16

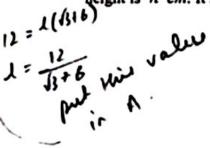
 12:31 + 16

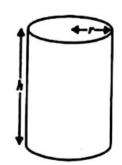
 12:31 + 16

 21/A = -6 12.

 01/2 = 2

 21/4 = -6 12.
- (ii) Sumit has bought a closed cylindrical dustbin. The radius of the dustbin is 'r'cm and height is 'h' cm. It has a volume of 20π cm³.





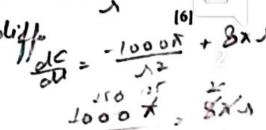
- V=7.12h 20 72 7.12h 12 20 7.5.A. 271 27 1.2
- (a) Express 'h' in terms of 'r', using the given volume.
- (b) Prove that the total surface area of the dustbin is $2\pi r^2 + \frac{40\pi}{r}$
- (c) Sumit wants to paint the dustbin. The cost of painting the base and top of the dustbin is ₹ 2 per cm² and the cost of painting the curved side is ₹ 25 per cm². Find the total cost in terms of 'r', for painting the outer surface of the dustbin including the base and top.

<u>.</u>

Question 13

Solve the following differential equation: $2ye^{\frac{x}{y}} dx + \left(y - 2xe^{\frac{x}{y}}\right) dy = 0, \text{ given } x = 0 \text{ and } y = 1$

(L)(a) = 1000 x



OR

Solve the following differential equation:

$$x(x^2-1)\frac{dy}{dx}=1, y=0, \text{ given } x=2$$

$$\frac{1}{x(x+1)(x-1)}$$
, $\frac{A}{x} + \frac{B}{x+1} + \frac{C}{x}$

Class II.

Question 14

A primary school teacher wants to teach the concept of 'larger number' to the students of Class II.

To teach this concept, he conducts an activity in his class. He asks the children to select two numbers from a set of numbers given as 2, 3, 4, 5 one after the other without replacement.

All the outcomes of this activity are tabulated in the form of ordered pairs given below:

	2	3	4,	5 /
2	(2,2)	(2,3)	. (2,4)	(2,5)
3	(3,2)	(3,3)	(3,4)	(3,5)
4	(4,2)	(4,3)	(4,4)	(4,5)
5	(5,2)	(5,3)	(5,4)	(5,5)



- Complete the table given above. (i)
- (ii) Find the total number of ordered pairs having one larger number. 12
- Let the random variable X denote the larger of two numbers in the ordered pair.



x	Subsc	ribe 🌡	(2,7), (3, (52), (5 5	f),(%f) ;3),(%Y)
P(X=x)	2/12	4/12	6/12.	

- Find the value of P (λ < 5)
- Calculate the expected value of the probability distribution.

(iii) Let A be a non-empty set.

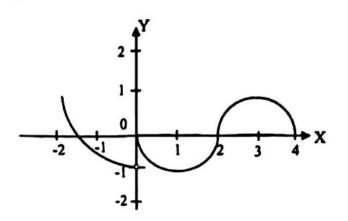
Statement 1: Identity relation on A is Reflexive.

Statement 2: Every Reflexive relation on A is an Identity relation.

- Both the statements are true. (a)
- Both the statements are false. **(b)**

Statement 1 is true and Statement 2 is false.

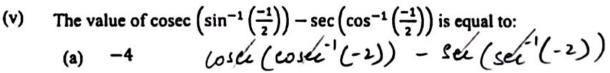
- (d) Statement 1 is false and Statement 2 is true.
- The graph of the function f is shown below. (iv)



Of the following options, at what values of x is the function f NOT differentiable?

(a) At
$$x = 0$$
 and $x = 2$

- (Ъ) At x = 1 and x = 3
- (c) At x = -1 and x = 1
- (d) At x = -1.5 and x = 1.5



(a)
$$-4$$



Subscribe

DIST