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BOARD QUESTION PAPER : MARCH 2023 MATHEMATICS AND STATISTICS

Time: 3 Hrs.

General instructions:

The question paper is divided into FOUR sections.

Max. Marks: 80

| (1) | Section A: Q. 1 contains Eight multiple choice type of questions, each carrying Two marks. | | | | | | | | |
|---------|--|---|---|-----------------------|---|----------------------|-------------------------|--|--|
| (2) | Section B: | Q. 2 contains PQ . 3 to Q . 1 | 14 contain Twe | swer type we short | answer type qu | urrying iestions, | each carrying | | |
| (3) | Section C: | Two marks. (At O. 15 to O. | tempt any Eight) 26 contain Twe | lve short | answer type au | uestions | each carrving | | |
| (-) | ~ | Three marks. (1 | Attempt any Eigh | <i>t</i>) | | | | | |
| (4) | Section D: | Q. 27 to Q. 34 ((Attempt any F i | contain Eight lon ive) | g answer t | ype questions, eac | ch carry | ving Four marks. | | |
| (5) | Use of log table is allowed. Use of calculator is not allowed. | | | | | | | | |
| (6) (7) | Figures to the right indicate full marks. | | | | | | | | |
| (7) | For each multiple choice type of question, it is mandatory to write the correct answer along with its | | | | | | | | |
| | alphabet, e.g. (a)/(b)/(c)/(d), etc. No marks shall be given, if $ONLY$ the correct answer or the alphabet of correct answer is written. Only the first attempt will be considered for evaluation. | | | | | | | | |
| (9) | Start answer | to each section of | n a new page. | | | | | | |
| | SECTION – A | | | | | | | | |
| Q.1. | Select and write the correct answer for the following multiple choice type of questions: | | | | | | | | |
| i. | If $p \land q$ is F, $p \rightarrow q$ is F then the truth values of p and q are respectively. | | | | | | | | |
| | (a) T, T | (b) | T, F | (c) | F, T | (d) | F, F | | |
| ii. | In $\triangle ABC$, if $c^2 + a^2 - b^2 = ac$, then $\angle B = _$. | | | | | | | | |
| | (a) $\frac{\pi}{4}$ | (b) | $\frac{\pi}{3}$ | (c) | $\frac{\pi}{2}$ | (d) | $\frac{\pi}{6}$ | | |
| iii. | The area of the | he triangle with v | ertices (1, 2, 0), (1 | 1, 0, 2) and | l (0, 3, 1) in sq. ur | nit is | | | |
| | (a) $\sqrt{5}$ | (b) | $\sqrt{7}$ | (c) | $\sqrt{6}$ | (d) | $\sqrt{3}$ | | |
| iv. | If the corner points of the feasible solution are (0, 10), (2, 2) and (4, 0) then the point of minimum | | | | | | | | |
| | z = 3x + 2y is | ; | (0, 10) | (c) | (4, 0) | (d) | (3, 4) | | |
| | (a) (2, 2) | | (0, 10) | (0) | (4, 0) | (u) | (3, 4) | | |
| v. | If y is a funct | 10n of x and log (. | (x + y) = 2xy, then | the value (| of $y'(0) = $ | _(4) | 1 | | |
| | (a) 2 | (0) | 0 | (0) | -1 | (u) | 1 | | |
| vi. | $\int \cos^3 x \mathrm{d}x = \underline{\ }$ | · | | | | | | | |
| | (a) $\frac{1}{12}\sin 3$ | $3x + \frac{3}{4}\sin x + c$ | | (b) | $\frac{1}{12}\sin 3x + \frac{1}{4}\sin x$ | + c | | | |
| | (c) $\frac{1}{12}\sin^3$ | $3x - \frac{3}{4}\sin x + c$ | | (d) | $\frac{1}{12}\sin 3x - \frac{1}{4}\sin x$ | + c | | | |
| vii. | The solution | of the differential | equation $\frac{dx}{dt} = \frac{xl}{x}$ | $\frac{\log x}{t}$ is | | | | | |
| | (a) $x = e^{ct}$ | | | (b) | $x + e^{ct} = 0$ | | | | |
| | (c) $x = e^t +$ | ⊦ t | | (d) | $xe^{ct} = 0$ | | | | |
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Mathematics and Statistics

| Math | ematics and Statistics | | | | | | | | |
|-------------------|--|----------------|--|--|--|--|--|--|--|
| viii. | Let the probability mass function (p.m.f.) of a random variable X be $P(X = x) = {}^{4}C_{x} \left(\frac{5}{9}\right)^{x} \times \left(\frac{4}{9}\right)^{4-x}$, | | | | | | | | |
| | (a) $\frac{20}{9}$ (b) $\frac{9}{20}$ (c) $\frac{12}{9}$ (d) $\frac{9}{25}$ | (2) | | | | | | | |
| Q.2. i. | Answer the following questions: Write the joint equation of co-ordinate axes. | [4] (1) | | | | | | | |
| ii. | Find the values of c which satisfy $ c\overline{u} = 3$ where $\overline{u} = \hat{i} + 2\hat{j} + 3\hat{k}$. | | | | | | | | |
| iii. | Write $\int \cot x dx$. | (1) | | | | | | | |
| iv. | Write the degree of the differential equation $e^{\frac{dy}{dx}} + \frac{dy}{dx} = x$ | (1) | | | | | | | |
| | SECTION – B | | | | | | | | |
| Atten O.3. | Approximate Provide Approximate Provide Appro | [16] | | | | | | | |
| C | If $x < y$ then $x^2 < y^2$ | (2) | | | | | | | |
| Q.4. | If $A = \begin{bmatrix} x & 0 & 0 \\ 0 & y & 0 \\ 0 & 0 & z \end{bmatrix}$ is a non singular matrix, then find A^{-1} by elementary row transformations. | | | | | | | | |
| | Hence write the inverse of $\begin{bmatrix} 2 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$ | (2) | | | | | | | |
| Q.5. | Find the cartesian co-ordinates of the point whose polar co-ordinates are $\left(\sqrt{2}, \frac{\pi}{4}\right)$. | (2) | | | | | | | |
| Q.6. | If $ax^2 + 2hxy + by^2 = 0$ represents a pair of lines and $h^2 = ab \neq 0$ then find the ratio of their slopes. | | | | | | | | |
| Q.7. | If \overline{a} , \overline{b} , \overline{c} are the position vectors of the points A, B, C respectively and $5\overline{a} + 3\overline{b} - 8\overline{c} = \overline{0}$ then find the ratio in which the point C divides the line segment AB. | | | | | | | | |
| Q.8. | Solve the following inequations graphically and write the corner points of the feasible region: $2x + 3y \le 6, x + y \ge 2, x \ge 0, y \ge 0$ | (2) | | | | | | | |
| Q.9. | Show that the function $f(x) = x^3 + 10x + 7$, $x \in R$ is strictly increasing. | (2) | | | | | | | |
| Q.10. | Evaluate: $\int_{0}^{\frac{\pi}{2}} \sqrt{1 - \cos 4x} \mathrm{d}x$ | (2) | | | | | | | |
| Q.11. | Find the area of the region bounded by the curve $y^2 = 4x$, the X-axis and the lines $x = 1$, $x = 4$ for $y \ge 0$. | (2) | | | | | | | |
| Q.12. | Solve the differential equation $\cos x \cos y dy - \sin x \sin y dx = 0$ | (2) | | | | | | | |
| Q.13. | Find the mean of number randomly selected from 1 to 15. | (2) | | | | | | | |
| Q.14. | Find the area of the region bounded by the curve $y = x^2$ and the line $y = 4$. | (2) | | | | | | | |

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SECTION - C

Q.23. Evaluate
$$\int x \tan^{-1} x dx$$

Q.24. Find the particular solution of the differential equation $\frac{dy}{dx} = e^{2y} \cos x$, when $x = \frac{\pi}{6}$, y = 0(3)

Q.25. For the following probability density function of a random variable X, find (a) P(X < 1) and (b) P(|X| < 1).

$$f(x) = \frac{x+2}{18} \quad ; \text{ for } -2 < x < 4$$

= 0 , otherwise (3)

Q.26. A die is thrown 6 times. If 'getting an odd number' is a success, find the probability of at least 5 successes. (3)

Attempt any FIVE of the following questions:

Q.27. Simplify the given circuit by writing its logical expression. Also write your conclusion.

Q.28. If
$$A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$
 verify that $A(adjA) = (adjA)A = |A|I$ (4)

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Mathematics and Statistics

Q.29. Prove that the volume of a tetrahedron with coterminus edges \bar{a} , \bar{b} and \bar{c} is $\frac{1}{6} \begin{bmatrix} \bar{a} & \bar{b} & \bar{c} \end{bmatrix}$. Hence, find the volume of tetrahedron whose coterminus edges are $\bar{a} = \hat{i} + 2\hat{j} + 3\hat{k}$, $\bar{b} = -\hat{i} + \hat{j} + 2\hat{k}$ and $\bar{c} = 2\hat{i} + \hat{j} + 4\hat{k}$.

Q.30. Find the length of the perpendicular drawn from the point P(3, 2, 1) to the line $\bar{\mathbf{r}} = (7\hat{\mathbf{i}} + 7\hat{\mathbf{j}} + 6\hat{\mathbf{k}}) + \lambda(-2\hat{\mathbf{i}} + 2\hat{\mathbf{j}} + 3\hat{\mathbf{k}})$ (4)

Q.31. If
$$y = \cos(m \cos^{-1} x)$$
 then show that $(1 - x^2)\frac{d^2 y}{dx^2} - x\frac{dy}{dx} + m^2 y = 0$ (4)

Q.32. Verify Lagrange's mean value theorem for the function $f(x) = \sqrt{x+4}$ on the interval [0, 5]. (4)

Q.33. Evaluate:
$$\int \frac{2x^2 - 3}{(x^2 - 5)(x^2 + 4)} dx$$

Q.34. Prove that:
$$\int_{0}^{2a} f(x) dx = \int_{0}^{a} f(x) dx + \int_{0}^{a} f(2a - x) dx$$

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