

JEE Main Session 2 Mathematics Exam: Model 3

- 1. Find the eccentricity of an ellipse whose length of the minor axis is equal to half of the length between foci.
- 2. The domain of $y = \cos^{-1} |((2 |x|)/4)| + \log (3 x)^{-1}$ is $[\alpha, \beta] {\gamma}$, then find $\alpha + \beta + \gamma$.
- 3. A line passes through (9,0), making angle 30° with positive direction of x-axis. It is rotated by angle of 15° with respect to (9,0). Find the equation of the new line.
- 4. For a non-zero complex number z satisfying $z^2 + i\bar{z} = 0$, then value of $|z|^2$ is?
- 5. If |a| = 1, |b| = 4, $a \cdot b = 2$ and $c = 2(a \times b) 3b$, then what is the angle between b and c?
- 6. Set $S = \{0, 1, 2, 3, ..., 10\}$

If a random ordered pair (x, y) of elements of S is chosen, then find probability that |x - y| > 5.

- 7. Find the number of integral terms in the binomial expansion: $(7^{1/2} + 11^{1/6})^{824}$
- 8. In a class, there are 40 students.
 - 16 students passed in Chemistry.
 - 20 students passed in Physics.
 - 25 students passed in Maths.
 - 15 students passed in both Math and Physics.
 - 15 students passed in both Math and Chemistry
 - 10 students passed in both Physics and Chemistry.

Find the maximum number of students that passed in all the subjects.



If the number of functions from Set A to Power Set A can be expressed as m^n (where m is the least integer), the find m + n.

10.
$$[1/(1-3(1)^2+1^4)]+[2/(2-3(2)^2+2^4)]+[3/(3-3(3)^2+3^4)]+...$$
 (up to n = 10) = ?

- 11. If one of the diameters of the circle $x^2 + y^2 10x + 4y + 13 = 0$ is a chord of another circle and whose centre is the point of intersection of the lines 2x + 3y = 12 and 3x 2y = 5. then the radius of the circle is?
- 12. An urn contains 15 red, 10 white, 60 orange, and 15 green balls. If 2 balls are taken with replacement, find the probability 1 ball is red and the other ball is white.
- 13. $\lim_{x\to 0} (x\to 0) \left[(e^{|2\sin x|} 2|\sin x| 1) / x^2 \right] = ?$
- 14. If three vectors are:

$$a = 3i + j - 2k$$

$$b = 4i + j + 7k$$

$$c = i - 3i + 4k$$

If p is a vector such that p x b = c x b and $p \cdot a = 0$, then find $p \cdot (i - j - k)$.

15. Find the value of 20M, if M is the median of the following data:

X_i	$\mathbf{f_i}$	C.F.
0 - 4	2	2
4 - 8	4	6
8 - 12	7	13
12 - 16	8	21
16 - 20	6	27