Physics

SECTION 1 (Maximum Marks: 12)

- This section contains THREE (03) questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).

Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;

Partial Marks : +3 If all the four options are correct but **ONLY** three options are chosen;

Partial Marks : +2 If three or more options are correct but **ONLY** two options are chosen, both of

which are correct;

Partial Marks : +1 If two or more options are correct but **ONLY** one option is chosen and it is a

correct option;

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);

Negative Marks: -2 In all other cases.

• For example, in a question, if (A), (B) and (D) are the ONLY three options corresponding to correct

answers, then

choosing ONLY (A), (B) and (D) will get +4 marks;

choosing ONLY (A) and (B) will get +2 marks;

choosing ONLY (A) and (D) will get +2 marks;

choosing ONLY (B) and (D) will get +2 marks;

choosing ONLY (A) will get +1 mark;

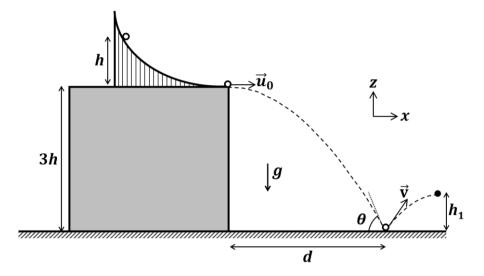
choosing ONLY (B) will get +1 mark;

choosing ONLY (D) will get +1 mark;

choosing no option (i.e. the question is unanswered) will get 0 marks; and

choosing any other combination of options will get -2 marks.

Q.1 A slide with a frictionless curved surface, which becomes horizontal at its lower end, is fixed on the terrace of a building of height 3h from the ground, as shown in the figure. A spherical ball of mass m is released on the slide from rest at a height h from the top of the terrace. The ball leaves the slide with a velocity $\vec{u}_0 = u_0 \hat{x}$ and falls on the ground at a distance d from the building making an angle θ with the horizontal. It bounces off with a velocity \vec{v} and reaches a maximum height h_1 . The acceleration due to gravity is g and the coefficient of restitution of the ground is $1/\sqrt{3}$. Which of the following statement(s) is(are) correct?



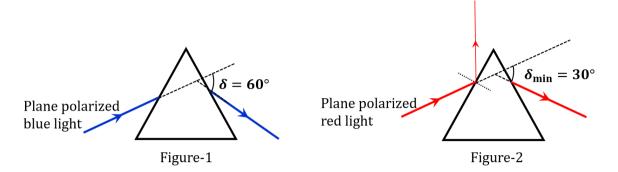
$$\begin{aligned} &(\mathrm{A})\,\vec{\mathrm{u}}_0 = \sqrt{2gh}\hat{x}\\ &(\mathrm{B})\,\vec{\mathrm{v}} = \sqrt{2gh}(\hat{x}-\hat{z})\\ &(\mathrm{C})\,\theta = 60^\circ \end{aligned}$$

(C)
$$\theta = 60^{\circ}$$

(D)
$$d/h_1 = 2\sqrt{3}$$

Answer: A, C, D

Q.2 A plane polarized blue light ray is incident on a prism such that there is no reflection from the surface of the prism. The angle of deviation of the emergent ray is $\delta = 60^{\circ}$ (see Figure-1). The angle of minimum deviation for red light from the same prism is $\delta_{min} = 30^{\circ}$ (see Figure-2). The refractive index of the prism material for blue light is $\sqrt{3}$. Which of the following statement(s) is(are) correct?

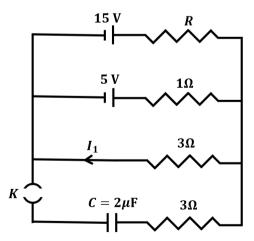


- (A) The blue light is polarized in the plane of incidence.
- (B) The angle of the prism is 45°.
- (C) The refractive index of the material of the prism for red light is $\sqrt{2}$.
- (D) The angle of refraction for blue light in air at the exit plane of the prism is 60°.

Answer: A, C, D

Q.3 In a circuit shown in the figure, the capacitor C is initially uncharged and the key K is open. In this condition, a current of 1 A flows through the 1 Ω resistor. The key is closed at time $t = t_0$. Which of the following statement(s) is(are) correct?

[Given: $e^{-1} = 0.36$]



- (A) The value of the resistance R is 3 Ω .
- (B) For $t < t_0$, the value of current I_1 is 2 A.
- (C) At $t = t_0 + 7.2 \,\mu\text{s}$, the current in the capacitor is 0.6 A.
- (D) For $t \to \infty$, the charge on the capacitor is 12 μ C.

Answer: A, B, C, D

SECTION 2 (Maximum Marks: 12)

- This section contains FOUR (04) questions.
- Each guestion has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +3 If **ONLY** the correct option is chosen;

: 0 If none of the options is chosen (i.e. the question is unanswered); Zero Marks

Negative Marks : -1 In all other cases.

0.4 A bar of mass M = 1.00 kg and length L = 0.20 m is lying on a horizontal frictionless surface. One end of the bar is pivoted at a point about which it is free to rotate. A small mass m = 0.10 kg is moving on the same horizontal surface with 5.00 m s⁻¹ speed on a path perpendicular to the bar. It hits the bar at a distance L/2 from the pivoted end and returns back on the same path with speed v. After this elastic collision, the bar rotates with an angular velocity ω . Which of the following statement is correct?

(A)
$$\omega = 6.98 \text{ rad s}^{-1} \text{ and } v = 4.30 \text{ m s}^{-1}$$
 (B) $\omega = 3.75 \text{ rad s}^{-1} \text{ and } v = 4.30 \text{ m s}^{-1}$ (C) $\omega = 3.75 \text{ rad s}^{-1} \text{ and } v = 4.30 \text{ m s}^{-1}$ (D) $\omega = 6.80 \text{ rad s}^{-1} \text{ and } v = 4.10 \text{ m s}^{-1}$

(B)
$$\omega = 3.75 \text{ rad s}^{-1} \text{ and v} = 4.30 \text{ m s}^{-1}$$

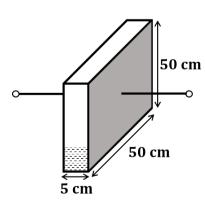
(C)
$$\omega = 3.75 \text{ rad s}^{-1} \text{ and v} = 10.0 \text{ m s}^{-1}$$

(D)
$$\omega = 6.80 \text{ rad s}^{-1} \text{ and v} = 4.10 \text{ m s}^{-1}$$

Answer: A

Q.5 A container has a base of 50 cm × 5 cm and height 50 cm, as shown in the figure. It has two parallel electrically conducting walls each of area 50 cm × 50 cm. The remaining walls of the container are thin and non-conducting. The container is being filled with a liquid of dielectric constant 3 at a uniform rate of 250 cm³ s⁻¹. What is the value of the capacitance of the container after 10 seconds?

[Given: Permittivity of free space $\epsilon_0 = 9 \times 10^{-12} \,\mathrm{C}^2\mathrm{N}^{-1}\mathrm{m}^{-2}$, the effects of the non-conducting walls on the capacitance are negligible]



- (A) 27 pF
- (B) 63 pF
- (C) 81 pF
- (D) 135 pF

Answer: B

Q.6 One mole of an ideal gas expands adiabatically from an initial state (T_A, V_0) to final state $(T_f, 5V_0)$. Another mole of the same gas expands isothermally from a different initial state (T_B, V_0) to the same final state $(T_f, 5V_0)$. The ratio of the specific heats at constant pressure and constant volume of this ideal gas is γ . What is the ratio T_A/T_B ?

(A) $5^{\gamma-1}$ (B) $5^{1-\gamma}$ (C) 5^{γ} Answer: A

Q.7 Two satellites P and Q are moving in different circular orbits around the Earth (radius R). The heights of P and Q from the Earth surface are h_P and h_Q , respectively, where $h_P = R/3$. The accelerations of P and Q due to Earth's gravity are g_P and g_Q , respectively. If $g_P/g_Q = 36/25$, what is the value of h_Q ?

(D) $5^{1+\gamma}$

(A) 3R/5 (B) R/6 (C) 6R/5 (D) 5R/6

Answer: A

SECTION 3 (Maximum Marks: 24)

- This section contains SIX (06) questions.
- The answer to each question is a **NON-NEGATIVE INTEGER**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the onscreen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:

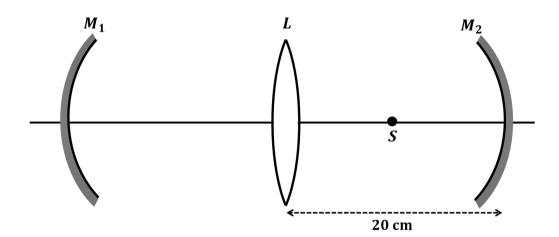
Full Marks : +4 If **ONLY** the correct integer is entered;

Zero Marks : 0 In all other cases.

Q.8 A Hydrogen-like atom has atomic number Z. Photons emitted in the electronic transitions from level n=4 to level n=3 in these atoms are used to perform photoelectric effect experiment on a target metal. The maximum kinetic energy of the photoelectrons generated is 1.95 eV. If the photoelectric threshold wavelength for the target metal is 310 nm, the value of Z is 3.

[Given: hc = 1240 eV-nm and Rhc = 13.6 eV, where R is the Rydberg constant, h is the Planck's constant and c is the speed of light in vacuum]

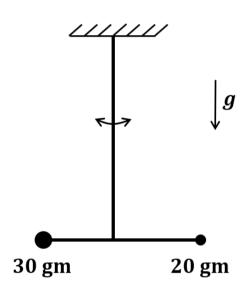
Q.9 An optical arrangement consists of two concave mirrors M_1 and M_2 , and a convex lens L with a common principal axis, as shown in the figure. The focal length of L is 10 cm. The radii of curvature of M_1 and M_2 are 20 cm and 24 cm, respectively. The distance between L and M_2 is 20 cm. A point object S is placed at the mid-point between L and M_2 on the axis. When the distance between L and M_1 is n/7 cm, one of the images coincides with S. The value of n is $\frac{80 \text{ or } 150 \text{ or } 220 \text{ or$



Q.10 In an experiment for determination of the focal length of a thin convex lens, the distance of the object from the lens is 10 ± 0.1 cm and the distance of its real image from the lens is 20 ± 0.2 cm. The error in the determination of focal length of the lens is n %. The value of n is ______.

Q.11 A closed container contains a homogeneous mixture of two moles of an ideal monatomic gas $(\gamma = 5/3)$ and one mole of an ideal diatomic gas $(\gamma = 7/5)$. Here, γ is the ratio of the specific heats at constant pressure and constant volume of an ideal gas. The gas mixture does a work of 66 Joule when heated at constant pressure. The change in its internal energy is ___121___ Joule.

- Q.12 A person of height 1.6 m is walking away from a lamp post of height 4 m along a straight path on the flat ground. The lamp post and the person are always perpendicular to the ground. If the speed of the person is 60 cm s⁻¹, the speed of the tip of the person's shadow on the ground with respect to the person is 40 cm s⁻¹.
- Q.13 Two point-like objects of masses 20 gm and 30 gm are fixed at the two ends of a rigid massless rod of length 10 cm. This system is suspended vertically from a rigid ceiling using a thin wire attached to its center of mass, as shown in the figure. The resulting torsional pendulum undergoes small oscillations. The torsional constant of the wire is 1.2×10^{-8} N m rad⁻¹. The angular frequency of the oscillations in $n \times 10^{-3}$ rad s⁻¹. The value of n is __10__.



SECTION 4 (Maximum Marks: 12)

- This section contains FOUR (04) Matching List Sets.
- Each set has **ONE** Multiple Choice Question.
- Each set has TWO lists: List-I and List-II.
- List-I has Four entries (P), (Q), (R) and (S) and List-II has Five entries (1), (2), (3), (4) and (5).
- **FOUR** options are given in each Multiple Choice Question based on **List-I** and **List-II** and **ONLY ONE** of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +3 ONLY if the option corresponding to the correct combination is chosen;

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);

Negative Marks: -1 In all other cases.

Q.14 List-I shows different radioactive decay processes and List-II provides possible emitted particles. Match each entry in List-I with an appropriate entry from List-II, and choose the correct option.

List-I

(P)
$$^{238}_{92}U \rightarrow ^{234}_{91}Pa$$

(O)
$$^{214}_{92}Pb \rightarrow ^{210}_{92}Pb$$

$$(R)^{210}_{81}Tl \rightarrow {}^{206}_{82}Pb$$

(S)
$$^{228}_{91}Pa \rightarrow ^{224}_{88}Ra$$

List-II

- (1) one α particle and one β^+ particle
- (2) three β^- particles and one α particle
- (3) two β^- particles and one α particle
- (4) one α particle and one β^- particle
- (5) one α particle and two β^+ particles

(A)
$$P \rightarrow 4$$
, $Q \rightarrow 3$, $R \rightarrow 2$, $S \rightarrow 1$

(C)
$$P \rightarrow 5$$
, $Q \rightarrow 3$, $R \rightarrow 1$, $S \rightarrow 4$

(B)
$$P \rightarrow 4$$
, $Q \rightarrow 1$, $R \rightarrow 2$, $S \rightarrow 5$

(D)
$$P \rightarrow 5$$
, $Q \rightarrow 1$, $R \rightarrow 3$, $S \rightarrow 2$

Answer: A

Q.15 Match the temperature of a black body given in List-I with an appropriate statement in List-II, and choose the correct option.

[Given: Wien's constant as 2.9×10^{-3} m-K and $\frac{hc}{e} = 1.24 \times 10^{-6}$ V-m]

List-I

(P) 2000 K

(Q) 3000 K

List-II

- (1) The radiation at peak wavelength can lead to emission of photoelectrons from a metal of work function 4 eV.
- (2) The radiation at peak wavelength is visible to human eye.
- (3) The radiation at peak emission wavelength will result in the widest central maximum of a single slit diffraction.
- (4) The power emitted per unit area is 1/16 of that emitted by a blackbody at temperature 6000 K.
- (5) The radiation at peak emission wavelength can be used to image human bones.

(A)
$$P \rightarrow 3$$
, $Q \rightarrow 5$, $R \rightarrow 2$, $S \rightarrow 3$

(C)
$$P \rightarrow 3, Q \rightarrow 4, R \rightarrow 2, S \rightarrow 1$$

Answer: C

(B)
$$P \rightarrow 3$$
, $Q \rightarrow 2$, $R \rightarrow 4$, $S \rightarrow 1$

(D)
$$P \rightarrow 1, Q \rightarrow 2, R \rightarrow 5, S \rightarrow 3$$

A series LCR circuit is connected to a 45 $\sin(\omega t)$ Volt source. The resonant angular frequency of Q.16 the circuit is 10^5 rad s⁻¹ and current amplitude at resonance is I_0 . When the angular frequency of the source is $\omega = 8 \times 10^4 \text{ rad s}^{-1}$, the current amplitude in the circuit is 0.05 I_0 . If L = 50 mH, match each entry in List-I with an appropriate value from List-II and choose the correct option.

List-I		List-II
(P) I_0 in mA		(1) 44.4
(Q) The quality factor of the circuit		(2) 18
(R) The bandwidth of the circuit in rad s^{-1}		(3) 400
(S) The peak power dissipated at resonance in Watt		(4) 2250
		(5) 500
(A) $P \rightarrow 2$, $Q \rightarrow 3$, $R \rightarrow 5$, $S \rightarrow 1$		$3, Q \rightarrow 1, R \rightarrow 4, S$

$$(A) P \rightarrow 2, Q \rightarrow 3, R \rightarrow 5, S \rightarrow 1$$

(B)
$$P \to 3, 0 \to 1, R \to 4, S \to 2$$

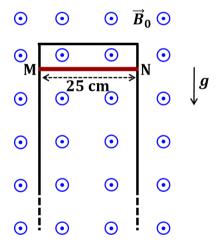
(C)
$$P \rightarrow 4$$
, $Q \rightarrow 5$, $R \rightarrow 3$, $S \rightarrow 1$

(D)
$$P \rightarrow 4$$
, $Q \rightarrow 2$, $R \rightarrow 1$, $S \rightarrow 5$

Answer: B

Q.17 A thin conducting rod MN of mass 20 gm, length 25 cm and resistance 10 Ω is held on frictionless, long, perfectly conducting vertical rails as shown in the figure. There is a uniform magnetic field $B_0 = 4$ T directed perpendicular to the plane of the rod-rail arrangement. The rod is released from rest at time t = 0 and it moves down along the rails. Assume air drag is negligible. Match each quantity in List-I with an appropriate value from List-II, and choose the correct option.

[Given: The acceleration due to gravity $g = 10 \text{ m s}^{-2}$ and $e^{-1} = 0.4$]



List-I List-II

(P) At t = 0.2 s, the magnitude of the induced emf in Volt (1) 0.07

(Q) At t = 0.2 s, the magnitude of the magnetic force in Newton (2) 0.14

(R) At t = 0.2 s, the power dissipated as heat in Watt (3) 1.20

(S) The magnitude of terminal velocity of the rod in m s^{-1} (4) 0.12

(5) 2.00

(A)
$$P \rightarrow 5$$
, $Q \rightarrow 2$, $R \rightarrow 3$, $S \rightarrow 1$

(B)
$$P \rightarrow 3$$
, $Q \rightarrow 1$, $R \rightarrow 4$, $S \rightarrow 5$

(C)
$$P \rightarrow 4$$
, $Q \rightarrow 3$, $R \rightarrow 1$, $S \rightarrow 2$

(D)
$$P \rightarrow 3$$
, $Q \rightarrow 4$, $R \rightarrow 2$, $S \rightarrow 5$

Answer: D