

Coordinate Geometry

Q. 1 A) MCQ

- 1) Point P is midpoint of segment AB where A(- 4,2) and B(6,2) then the coordinates of P are -----
- A) (-1, 2) B) (1, 2) C) (1, - 2) D) (-1, - 2)
- 2) The distance between Point P (2 , 2) and Q (5, x) is 5 cm then the value of x = -----
- A) 2 B) 6 C) 3 D) 1
- 3) The distance between points P (-1 , 1) and Q(5, -7) is -----..
- A) 11 cm B) 10 cm C) 5 cm D) 7 cm
- 4) If the length of the segment joining point L (x , 7) and point M(1, 15) is 10 cm then the value of x is -----
- A) 7 B) 7 or -5 C) - 1 D) 1
- 5) Find distance between point A (-3 , 4) and origin O.
- A) 7 cm B) 10 cm C) 5 cm D) -5 cm
- 6) If point P (1 , 1) divide segment joining point A and point B (-1 , -1) in the ratio 5 : 2 then the coordinates of A are -----
- A)(3 ,3) B)(6, 6) C)(2, 2) D)(1, 1)
- 7) If segment AB is parallel Y-axis and coordinates of A are (1, 3) then the coordinates of B are -----
- A)(3 ,1) B)(5, 3) C)(3, 0) D)(1, -3)
- 8) If point P is midpoint of segment joining point A (-4, 2) and point B(6, 2) then the coordinates of P are -----
- A)(-1, 2) B)(1 , 2) C)(1 , -2) D) (-1, - 2)

9) If point P divides segment AB in the ratio 1:3 where A(-5 , 3) and B(3 , -5) then the coordinates of P are -----

- A) $(-2, -2)$ B) $(-1, -1)$ C) $(-3, 1)$ D) $(1, -3)$

10) If the sum of x-coordinates of the vertices of a triangle is 12 and the sum of Y-coordinates is 9 then the coordinates of centroid are -----

- A)(12, 9) B)(9, 12) C)(4, 3) D)(3, 4)

Q. 1 B. Solve the following (1 mark each)

- 1) Find the coordinates of the point of intersection of the graph of the equation $X = 2$ and $y = -3$.
- 2) Find distance between point A (7, 5) and B (2, 5).
- 3) The coordinates of diameter AB of a circle are A (2, 7) and B (4, 5) then find the coordinates of the centre.
- 4) Write the X-coordinate and Y-coordinate of point P(-5, 4).
- 5) What are the coordinates of origin?
- 6) Find distance of point A(6, 8) from origin:
- 7) Find coordinates of midpoint joining (-2, 6) and (8, 2)
- 8) Find the coordinates of centroid of a triangle whose vertices are (4, 7), (8, 4) and (7, 11).
- 9) Find distance between point O(0, 0) and B (-5, 12).
- 10) Find coordinates of midpoint of point (0, 2) and (12, 14).

Q. 2 A) Complete the activity (each of 2 mark)

- 1) Find distance between point Q (3 , - 7) and point R (3, 3)

Solution: Suppose Q (x_1, y_1) and point R (x_2, y_2)

$$x_1 = 3, y_1 = -7 \quad \text{and} \quad x_2 = 3, y_2 = 3$$

Using distance formula,

$$d(Q, R) = \sqrt{\dots}$$

$$\therefore d(Q, R) = \sqrt{\boxed{}} 100$$

$$\therefore d(Q, R) = \sqrt{\boxed{}}$$

$$\therefore d(Q, R) = \boxed{}$$

2) Find distance between point A(-1, 1) and point B (5, -7) :

Solution : - Suppose A(x_1 , y_1) and B(x_2 , y_2)

$$X_1 = -1, y_1 = 1 \quad \text{and} \quad x_2 = 5, y_2 = -7$$

Using distance formula,

$$d(A, B) = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\therefore d(A, B) = \sqrt{\boxed{} + ((-7) - \boxed{})^2}$$

$$\therefore d(A, B) = \sqrt{\boxed{}}$$

$$\therefore d(A, B) = \boxed{}$$

3) Find coordinates of the midpoint of a segment joining point A(-1, 1) and point B(5, -7).

Solution: - Suppose A(x_1 , y_1) and B(x_2 , y_2)

$$X_1 = -1, y_1 = 1 \quad \text{and} \quad x_2 = 5, y_2 = -7$$

Using midpoint formula,

$$\therefore \text{Coordinates of midpoint of segment AB} = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right) = \left(\frac{\boxed{}}{2}, \frac{\boxed{}}{2} \right)$$

$$\therefore \text{Coordinates of the midpoint} = \left(\frac{4}{2}, \frac{\boxed{}}{2} \right)$$

$$\therefore \text{Coordinates of the midpoint} = (2, \boxed{})$$

- 4) The coordinates of the vertices of a triangle ABC are A (-7, 6), B(2, -2) and C(8, 5) find coordinates of its centroid.

Solution : - Suppose A(x_1 , y_1) and B(x_2 , y_2) and C (x_3 , y_3)

$$X_1 = -7, y_1 = 6 \text{ and } x_2 = 2, y_2 = -2 \text{ and } x_3 = 8, y_3 = 5$$

Using Centroid formula

\therefore Coordinates of the centroid of a triangle

$$ABC = \left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3} \right) = \left(\frac{\boxed{}}{3}, \frac{\boxed{}}{3} \right)$$

\therefore Coordinates of the centroid of a triangle ABC = $\left(\frac{3}{3}, \boxed{} \right)$

\therefore Coordinates of the centroid of a triangle ABC = $\left(1, \boxed{} \right)$

Q. 2 Solve (Each of 2 marks)

- 1) The point Q divides segment joining A (3, 5) and B (7, 9) in the ratio 2 : 3. Find the X-coordinate of Q.
- 2) If the distance between point L (x, 7) and point M (1, 15) is 10 then find the value of X.
- 3) Find the coordinates of midpoint of segment joining (22, 20) and (0, 16)
- 4) Find distance CD where C(-3a, a), D(a, -2a).
- 5) Show that the point(11, -2) is equidistant from (4, -3) and (6, 3).

Q. 3 A) Complete the activity (Each of 3 marks)

- 1) If the point P (6,7) divides the segment joining A (8, 9) and B(1, 2) in some ratio. Find that ratio.

Solution : Point P divides segment AB in the ratio m : n.

$$A (8, 9) = (x_1, y_1), B (1, 2) = (x_2, y_2) \text{ and } P (6, 7) = (x, y)$$

Using Section formula of internal division,

$$\therefore 7 = \frac{m(\text{ }) + n(9)}{m+n}$$

$$\therefore 7m + 7n = \text{ } + 9n$$

$$\therefore 7m - \text{ } = 9n - \text{ }$$

$$\therefore \text{ } = 2n$$

$$\therefore \frac{m}{n} = \text{ }$$

1) From the figure given alongside find the length of the median AD of triangle ABC .

Complete the activity.

Solution :- Here A (-1 , 1), B(5, -3), C (3, 5) and suppose D (x,y) are coordinates of point D.

Using midpoint formula,

$$X = \frac{5+3}{2}$$

$$y = \frac{-3+5}{2}$$

$$\therefore x = \text{ }$$

$$\therefore y = \text{ }$$

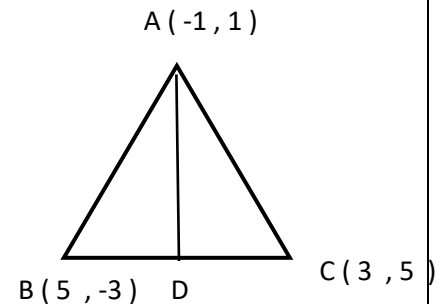
Using distance formula,

$$\therefore AD = \sqrt{(4 - \text{ })^2 + (1 - 1)^2}$$

$$\therefore AD = \sqrt{(\text{ })^2 + (0)^2}$$

$$\therefore AD = \sqrt{\text{ }}$$

$$\therefore \text{The length of median AD} = \text{ }$$



Q. 3 B) Solve the following (Each of 3 marks)

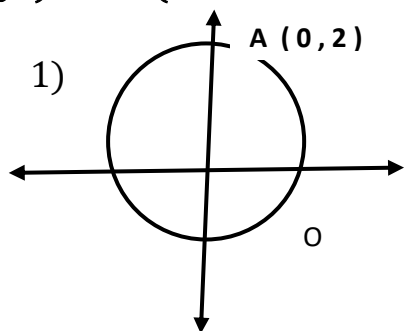
- 1) Show that P(-2 , 2), Q (2, 2) and R (2, 7) are vertices of a right angled triangle.
- 2) Show that the point (0 , 9) is equidistant from the points (-4,1) and (4 , 1).

- 3) Point $P(-4, 6)$ divides point $A(-6, 10)$ and $B(m, n)$ in the ratio $2:1$ then find the coordinates of point B .

Q. 4 Solve (Each of 4 marks)

- 1) Show that points $A(-4, -7)$, $B(-1, 2)$, $C(8, 5)$ and $D(5, -4)$ are the vertices of a parallelogram $ABCD$.
- 2) Show that the points $(0, -1)$, $(8, 3)$, $(6, 7)$ and $(-2, 3)$ are vertices of a rectangle.
- 3) Show that the points $(2, 0)$, $(-2, 0)$ and $(0, 2)$ are vertices of a triangle. State the type of triangle with reason.
- 4) If $A(5, 4)$, $B(-3, -2)$ and $C(1, -8)$ are the vertices of a ΔABC . Segment AD is median. Find the length of seg AD :
- 5) Show that $A(1, 2)$, $(1, 6)$, $C(1 + 2\sqrt{3}, 4)$ are vertices of an equilateral triangle.

Q.5) Solve (Each of 3 marks)



Seg OA is the radius of a circle with centre O .

The coordinates of point A is $(0, 2)$ then

decide whether the point $B(1, 2)$ is on the circle?

- 2) Find the ratio in which Y -axis divides the point $A(3, 5)$ and point $B(-6, 7)$. Find the coordinates of that point.
- 3) The points $(7, -6)$, $(2, K)$ and $(h, 18)$ are the vertices of triangle. If $(1, 5)$ are the coordinates of centroid. Find the value of h and k .
- 4) Using distance formula decide whether the points $(4, 3)$, $(5, 1)$ and $(1, 9)$ are collinear or not?