Amrita VISHWA VIDYAPEETHAM

(University established u/s 3 of UGC Act 1956)

Amrita Entrance Examination – Engineering

PHYSICS, CHEMISTRY & MATHEMATICS

Question booklet Version Code	Question booklet no.		Time : 3 hrs
Number of pages	Number of questions	120	Max. Marks: 360
Registration number			
Name of the candidate			
Signature of the candidate			

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GENERAL

- 1. Any malpractice or attempt to commit malpractice in the examination hall will lead to disqualification of the candidate.
- 2. Candidates are not allowed to carry any textual material, printed or written bits of papers, Mathematical and Physical Tables, electronic gadgets like calculator, cell phone, etc. into the examination hall.
- 3. Candidates shall possess the University Hall Ticket which should be produced on demand.
- 4. Candidates shall occupy the respective seats bearing their registration numbers on time.
- 5. Candidates shall sign the attendance sheet available with the invigilator.
- 6. Candidates are not permitted to leave the hall before the end of the examination.
- 7. Candidates are required to handover the ANSWER SHEET and the QUESTION BOOKLET to the invigilator before leaving the hall.
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QUESTION BOOKLET

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- 12. Rough work may be done on the space provided in this booklet.

(Continued on the last page of this question booklet)

Rough Work	

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MODEL QUESTIONS

PHYSICS (S.No.1 to 35) 35 Questions

Ch	ta: celeration due to gravity = arge of electron = 1.6 x 10 V = 1.6 x 10 ⁻¹⁹ J	= 10m/s ² , Mass of elector of C, Velocity of ligh	tron = 9.1×10^{-31} kg t, c = 3×10^{8} m/s			
1.	Which of the following has $A^2s^4kg^{-1}m^{-2}$	•	of farad? c) kg m ² A ⁻¹ s ²	d) kg m^3 $A^{-2}s^2$		
2.	a) Earth (29.8); Saturn(9.65); Venus(35.0); Mars(24.2) b) Earth (9.65); Saturn(29.8); Venus(35.0); Mars(24.2) c) Earth (24.2); Saturn(9.65); Venus(35.0); Mars(29.8) d) Earth (29.8); Saturn(9.65); Venus(24.2); Mars(35.0)					
3.	At a point 3200 km vert of earth in SI units is	•				
	a) 6.66	b) 3.33	c) 5.55	d) 4.44		
4.	Two laser beams one of photons. Their powers as a) 64:40	_	nd the other 400 nm ha	eve same unit flux of d) 25:64		
5.	The relation, Work Done	a – Change in internal	energy holds for			
<i>J</i> .	a) isothermal process	. – Change in internal (b) adiabatic process			
	c) isobaric process		d) isochoric process			
6.	The rate of flow of volume length L due to pressure used and ΔP is doubled	e difference ΔP is $(\Delta V/$	Δt). If a pipe of radius			
	a) 2	b) 4	c) 8	d) 16		
7.	If the charge Q in a capa	citor is doubled, electri	ic field energy stored in	nside		
	a) doubles		b) increases by factor			
	c) remains unchanged		d) increases by factor	: 8		
8.	. A capacitor with C =0.144 μ F having charge Q is made to discharge through a resistance of 1.0 Ω . What is the time taken for the discharge of 50% of the initial charge?					
	a) 10 ⁻⁷ s	b) 0.144 x10 ⁻⁶ s	c) $2.1 \times 10^{-7} \text{s}$	d) 0.144 x 10 ⁻⁷ s		
Ro	ough Work					

9.	A slab having dielectric constant $\kappa = 3$ is placed in a region having constant electric field $E = 10 \text{ V m}^{-1}$. The electric field inside the slab volume is					
	a) 1.1 V m ⁻¹	b) 30 V m ⁻¹	c) zero	d) 3.33V m ⁻¹		
10.	0. A parallel plate capacitor is connected to a battery supplying constant voltage difference such that it accumulates charge <i>Q</i> . While being connected, if the separation <i>d</i> between the plates is increased a) both electric field inside the capacitor and Q decrease					
	b) electric field inside thec) electric field inside thed) both electric field inside	e capacitor increases ar	nd Q decreases			
11.	The sides (in meters) $\mathbf{a} = 4\mathbf{i}$, $\mathbf{b} = 2\mathbf{i} + 3\mathbf{j}$ and $\mathbf{c} = \mathbf{i}$			esented by vectors		
	a) 20 m ²	b) 26 m ²	c) 36 m2	d) 40 m^2		
12.	12. The slant side of a frictionless incline making an angle 60° with the vertical is 1 m Starting from rest the time taken by a mass to slide down the incline from top to the base is					
	a) 0.63 s	b) 0.23 s	c) 0.2 s	d) 0.4 s		
13.	A mass of 0.01 kg is huspring constants k_1 = 10 system is					
	a) 3 cm	b) 1.5 cm	c) 6 cm	d) 2.5 cm		
14.	A mass $m = 1 \text{ kg located}$ in the y direction. All nur		The angular acceleration	n is		
	a) 0.24 radians s ⁻² along a c) 0.12 radians s ⁻² along a		,			
15.	A circuit is operated by flowing in the circuit is (internal resistance is					
	a) 1.8 W	b) 1.74 W	c) 1.42 W	d) 1.62 W		
16.	16. A small magnet of magnetic moment m is placed inside a hollow sphere of radius R; the net magnetic flux emerging out of the sphere is					
	a) proportional to mb) proportional to the procc) zerod) a function of location a					
Ro	ugh Work					
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	netic induction flux crost + 4 j + 6 k ? All numbers		plane if magnetic induction
a) 2	b) 4	c) 6	d) √56
18. The direction of corresponding w		plane wave is along	unit vector $n = i + j$. The
a) parallel to z asc) perpendicular		b) parallel to a d) parallel to	
_	l in a region is given by at a point (-5,1,2) is	$4x^2+3$. All numbers	are in SI units. The Electric
a) 40	b) 20	c) 80	d) 10
	ism of refracting angle 6 The critical angle of glas		iquid, its angle of minimum liquid medium is
a) 45°	b) 30°	c) 60°	d) 55°
(i) The ammete(ii) An ammeter(iii) An ammeter	p of incorrect statement in used to measure current should have very low reshould have very high reammeter in series will	et in a circuit is to be consistance. Resistance.	e e
a) (i) and (ii)	b) (ii) and (iii)	c) (iii) and (iv	d) (iv) and (i)
	h $i=1,2$ denote respective secondary coils of an ide	=	of turns, and the current in
a) $E_1/E_2 = N_1/N_1$ c) $E_2/E_1 = N_1/N_2$		b) $E_1/E_2 = N_2$ d) $E_1/E_2 = N_1$	
23. Which of the fol	lowing are unrelated?		
	ciple and propagation of	light	
	nciple and speed of light ation and Kepler's laws		
,	and Coulomb force		
•	pole of dipole moment p nt (b,0,0) and (0,0,b) are	•	gin. The electric fields at
a)		equal in magr	nitude
b) equal c) equal in direc	tion only		
/ 1	ignitude and opposite in	direction	
Rough Work			

25.	 25. A compound telescope have two lenses A and B. Lens A is closer to object than lens B. Which statement is correct? a) Both A and B form real images. b) Both A and B form virtual images. c) A forms real image and B forms virtual image. d) A forms virtual image and B forms real image. 					
26.	Assume that the wave le 600 nm. Its frequency is		C			
	a) $0.5 \times 10^{15} \text{ Hz}$	b) 0.33 x10 ¹⁵ Hz	c) $1.5 \times 10^{15} \text{ Hz}$	d) $0.5 \times 10^{15} \text{ Hz}$		
27.	The energies of two phomenta is	notons are in the rational	to 1:4. The correspon	nding ratio of their		
	a) 1:2	b) 1:4	c) 2:1	d) 4:1		
28.	At a given kinetic energy	which of the followin	g has the highest speed	1?		
	a) neutrino	b) electron	c) muon	d) photon		
29.	The time taken by light to order of					
	a) 10^{-21} s	b) 10^{-23} s	c) 10^{-25} s	d) 10^{-19} s		
30.	Water in a porcelain con of the water rises, but the a) porcelain is a bad cond b) water is a liquid and ca conductor.c) preferential absorption d) microwaves are more	container temperature ductor of heat. an set up convection con a of microwaves of cer	does not rise much. Turrents but the container	his is because er is solid non		
				IN COMPLETE		
Roi	agh Work					

CHEMISTRY (S.No. 36 to 70) 35 Questions

36.	6. 20 g of a solute whose density is 2.0 g/cc is dissolved in water and the solution is made upto one litre. If the molecular weight of the solute is 100, what is the molality of the solution?					
	a) 0.2020	b) 0.4040	c) 0.2000	d) 0.0200		
37.	The velocity of infra red a) twice	radiation in vacuum co b) half	ompared to ultra violet c) equal	is d) four times		
38.	 8. Which one of the following statements is true? a) An orbit and orbital mean the same thing. b) An orbit and orbital contain the same number of electrons always. c) The energies of the orbit and the orbital are the same. d) The maximum number of electrons present in an orbit and an orbital will be different. 					
39.	Which one of the foll principle? a) calcium	lowing has electronic b) titanium	c configuration in vi	d) manganese		
40	,	,	,	u) manganese		
40.	 a) A matchstick on strike burns. b) Camphor packed in a container without over space catches fire on its own. c) Petrol kept in an open beaker reduces in quantity slowly. d) Water in a beaker surrounded by ice and salt freezes. 					
41.	41. For a substance A_2B the first dissociation constant is $5x10^{-5}$ and the second dissociation constant is $1x10^{-9}$ at $25^{\circ}C$. The value of the equilibrium constant for the following reaction $A_2B \leftrightarrow 2A^+ + B^{2-}$ at the same temperature is					
4.0	a) 5 x 10 ⁴	,	c) 4×10^{-4}	d) 5 x 10 ⁻¹⁴		
42.	In ice-liquid water equilib	_				
	a) increase in melting poic) no change in melting p		b) decrease in meltingd) disappearance of o	_		
43.	3. A silver rod dipped in a solution of silver nitrate of a particular concentration shows a potential of 0.75 V vs standard hydrogen electrode. If the standard potential for silver is 0.8V, at what molar concentration of the solution the potential will become zero?					
	a) 2.76×10^{-14}	b) 2.76×10^{14}	c) 7.6×10^{-28}	d) 7.6×10^{28}		
Ro	ough Work					

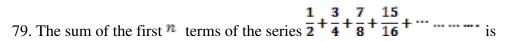
44.	4. What is the theoretical quantity of hydrogen required to generate 53.6Ah in a Proton Exchange Membrane Fuel Cell?				
	a) 1.0 g	b) 1.0 kg	c) 2.0 g	d) 2.0 litre	
45.	the concentration of X is reaction increases by for	our times. What is the	nat of Y and Z constant. T e order of the reaction?		
	a) 2	b) 4	c) 1	d) 0	
46.	Which one of the follow	wing exhibits Schottl	ky defect?		
	a) nickel oxidec) ferrous sulphide		b) potassium bromidd) silver chloride	e	
47.	Which one of the follow	wing is anti ferromag	gnetic?		
	a) titanium dioxide		b) nickel		
	c) oxygen		d) ferrous oxide		
48.	The gas that is produce	d through catalytic re	eforming of sewage is		
	a) producer gas		b) syngas		
	c) natural gas		d) carbon monoxide		
49.	Which one of the follow	wing hydrides is non-	-stoichiometric?		
	a) ammonia	b) nickel hydride	c) sodium hydride	d) diborane	
50.	The order of energy release 1 LPG > octane > lie b) liquid hydrogen > g c) octane > LPG > lie d) gaseous hydrogen >	quid hydrogen > gas gaseous hydrogen > quid hydrogen > ga	LPG > octane seous hydrogen	r litre is	
51.	Density of the following	g alkali metals is in t	the order of		
	c) sodium < potass	ium < sodium ium < lithium			
52.	The discontinuity in ior is due to	nization enthalpy val	ues of group 13 elements	in the periodic table	
	a) irregular variation inb) irregular variation inc) poor shielding effectd) poor shielding effect	electronegativity of 'p' and 'd' electro			
Roi	ıgh Work				

53.	3. The reduction of germanium tetrachloride with lithium aluminium hydride gives				
	a) digermanec) monogermane		b) di and tri germanesd) mixture of all germanes		
54.		following is used as cathode in		ery?	
	a) liquid sulphur oc) poly ethylene o		b) thionyl chlorided) methyl cyanide		
55.	• •	nerism is possible in pentaamn			
	a) linkage	b) optical	c) position	d) ionisation	
56.	A coordination co is the type of hybr	=	•		
	a) dsp ²	b) sp ³	c) sp^3d	d) d^2sp^3	
57.	pressure and 27°	nic compound gave 60 mL of PC. Aqueous tension at 27° trogen in the compound? b) 2.125			
58.	 58. Predict the products formed on passing acetylene through acetic acid followed by distillation in presence of mercuric sulphate. a) acetic anhydride and acetone b) acetic anhydride and ethanol c) propionic anhydride and methanol d) acetic anhydride and ethanal 				
59.	69. The order of reactivity of the following for an S _N ² reaction is a) alkyl fluoride > alkyl chloride > alkyl bromide > alkyl iodide b) alkyl fluoride > alkyl bromide > alkyl chloride > alkyl iodide c) alkyl iodide > alkyl bromide > alkyl chloride > alkyl fluoride d) alkyl bromide > alkyl fluoride > alkyl iodide > alkyl chloride				
60.	acid at 170°C to		sis, followed by hydr	olysis with lithium set of products from nol	

IN COMPLETE

MATHEMATICS (S.No. 71 to 120) 50 Questions

	6i and $z_2 = 4 + 6i$. If $z = \frac{\pi}{4}$, then $ z - 7 - 9i $ is ea	• •	such that the argument
or 2-2 ₂ 1 (a) 6	(b) 3√2	quai to (ɛ) 2√3	(d) √6
72. The complex	numbers z_1 and z_2 are	e such that $z_1 \neq z_2$ and	$ z_1 = z_2 $. If z_1 has
positive real j	part and Z ₂ has negati	ive imaginary part, then (b) real and	$\frac{z_1 + z_2}{z_1 - z_2} \text{may be}$ negative
(c) purely in	naginary	(d) real and p	ositive
73. The maximum (a) √3 – 1	value of $ z $ where ' z ', (b) $\sqrt{3}$	satisfies the condition $ z $	$\left +\frac{2}{z} \right = 2$ is $(d) \sqrt{3} + \sqrt{2}$
74. If ' 🥨 ' is a no	n real cube root of unity, th	nen (α + b)(α + bω)(α + l	<i>ω</i> ²) is
(a) $a^2 - b^2$	(b) $a^2 + b^2$		(d) $a^2 + b^2$
75. If a² +b² +c²	a = 1, then, $bc + ca + ab$	lies in the interval	
(a) $\left[-\frac{1}{2}\right]$	1] (b) $\left[-\frac{1}{2}\right]$	3] (c) [-1,	2] (d) [-1,
	e the number of triangles n of n sides. If $T_{n+1}-T_n$		
(a) 5	(b) 4	(c) 6	(d) 7
77. If (2 n + 1) P _{n-1}	$_{1}: (2n-1)P_{n} = 3:5$, the	en the value of ⁿ is	
(a) 3	(b) 6	(c) 4	(d) 8
78. The inverse of	the function $y = \frac{10^{x} - 10}{10^{x} + 10}$	is	
(a) log_{10} (2 –	x)	(b) $\frac{1}{2}log_{10}\left(\frac{1}{1}\right)$	$\left(\frac{x}{x}\right)$
(c) $\frac{1}{2}log_{10}(2x)$	–1)	(d) $\frac{1}{2} log_{10} \left(\frac{2x}{2-x} \right)$	$\left(\frac{c}{x}\right)$
Rough Work			



- (a) $2^{n} 1$
- (b) $1 2^{-n}$
- (c) $2^{-n} n + 1$
- (d) $2^{-n} + n 1$
- 80. If $\mathbf{5^{1+x} + 5^{1-x}}$, $\frac{\alpha}{2}$ and $2\mathbf{5^{x} + 25^{-x}}$ are three consecutive terms of an A.P., then the values of '\alpha' are given by
 - (a) $\alpha \geq 12$
- (b) a > 12
- (c) a < 12
- (d) $\alpha \leq 12$

81. If
$$a_a$$
 b_a c are in H.P., then the value of $\frac{b+a}{b-a} + \frac{b+c}{b-c}$ is

(a) 0

(b) 1

(c) 2

(d) 3

82. Let
$$\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix} = \mathbf{\Lambda}$$
, where a_s b_s c are positive. Then

- $(a) \Delta > 0$
- (b) ∆≥ 0
- (c) ∆≤ 0
- $(d) \Delta < 0$

83. If
$$\begin{bmatrix} 1 & x & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 \\ 0 & 4 & 5 \\ 0 & 6 & 7 \end{bmatrix} \begin{bmatrix} x \\ 1 \\ -2 \end{bmatrix} = 0$$
, then the value of x is

 $(a) - \frac{1}{2}$

 $(b)^{\frac{1}{2}}$

 $(c)^{\frac{12}{5}}$

 $(d) - \frac{12}{5}$

- 84. The quadratic expression $17 + 12x 4x^2$ takes
 - (a) the least value 6

(b) the highest value 26

(c) the highest value 17

- (d) the lowest value 17
- 85. Three vectors \overline{A}_s \overline{B} and \overline{C} are given by $\hat{\imath} + \hat{k}_s$ $\hat{\imath} + \hat{\jmath} + \hat{k}$ and $3\hat{\imath} 2\hat{\jmath} + 5\hat{k}$ respectively. Then the vector \overline{R} which satisfies the relation $\overline{R} \times \overline{B} = \overline{C} \times \overline{B}$ and $\overline{R} \cdot \overline{A} = \mathbf{0}$ is
 - (a) $-\hat{\imath} 6\hat{\jmath} + \hat{k}$

(b) $\hat{i} + 6\hat{j} - \hat{k}$

(c) $2\hat{i} - 3\hat{j} + \hat{k}$

(d) $-\hat{\imath} + 6\hat{\jmath} - \hat{k}$

86. If the magnitude of more through the point $\hat{i} + \hat{j}$ is			$\hat{i} + \alpha \hat{j} - \hat{k}$ acting
(a) 9	(b) 4	(c) ± 2	(d) ± 3
87. The arithmetic mean of ⁿ	odd natural numbers is	}	
(a) n	(b) $\frac{n(n+1)}{2}$	(c) n – 1	(d) n ²
88. A car completes the first have velocity *** The average velocity **	<i>y</i>	•	remaining half with
(a) $\sqrt{v_1 v_2}$	(b) $\frac{v_1 - v_2}{2}$	$(c) \frac{v_1 + v_2}{2}$	$(d) \frac{2v_1v_2}{v_1 + v_2}$
89. An integer x is chosen $x + \frac{192}{x} \le 30$ is	at random from the nu	mbers 1 to 28.	The probability that
(a) $\frac{7}{10}$	(b) $\frac{1}{15}$	(c) $\frac{2}{28}$	(d) $\frac{5}{28}$
90. Let ** be a nonzero determinants of order two the determinant is nonzero	with entries x and x		
(a) $\frac{1}{4}$	(b) $\frac{1}{2}$	(c) $\frac{3}{16}$	(d) $\frac{1}{8}$
91. Two candidates <i>A</i> and probability that <i>A</i> is select atmost 0.25 . Then the pro	ted is 0.5 and the proba	bility that both 🐴 a	and B are selected is
(a) 0.75	(b) 0.7	(c) 0.8	(d) 0.6
92. The curve satisfying the dithe point (1, -1) is	ifferential equation $\frac{dy}{dx}$ =	$= \frac{y^2 - 2xy - x^2}{y^2 + 2xy - x^2}$ and	nd passing through
(a) a circle		(b) a straight lin	ne
(c) an ellipse		(d) a parabola	
Rough Work			

93. The solution of the differential equation	log dy _ ox 6v 16		
93. The solution of the differential equation	$\frac{dx}{dx} = 3x - 6y + 6$, given $y = 1$	when
x = 0 is			

(a)
$$3e^{6y} = 2e^{9x-6} + 6e^x$$

(b)
$$3e^{6y} = 2e^{9x+6} - 6e^6$$

(c)
$$3e^{6y} = 2e^{9x+6} + e^6$$

(d)
$$e^{6y} = 2e^{9x-6} + e^{-6}$$

94.
$$\sqrt{2 + \sqrt{2 + 2\cos 8\theta}}$$
 is equal to

(d)
$$\cos 2\theta$$

95. The value of
$$\lim_{|x|\to\infty} [\cos(\tan^{-1})] (\sin(\tan^{-1}x))$$
 is equal to

$$(\alpha)-1$$

(c)
$$-\frac{1}{\sqrt{2}}$$

$$(d)\frac{1}{\sqrt{2}}$$

96. If the orthocentre H of a triangle ABC bisects the altitude AD of the triangle ABC, then the value of tanBtanC is

$$(c)$$
 3

97. The remainder got by dividing 2804 by 257 is

98. If
$$\lim_{x\to 0} f(x) = \frac{1}{2}$$
 and $\lim_{x\to 0} g(x) = 4$, then $\lim_{x\to 0} \frac{f(x)\cos x}{e^x \sqrt{g(x)}}$ is

(b)
$$-1$$

99. If
$$f(x)$$
 and $g(x)$ are two functions such that $f(2) = 3$, $g(2) = -4$, $f'(2) = -\frac{1}{2}$ and $g'(2) = -\frac{8}{3}$, then the derivative of $\log_{\epsilon}[f(x)g(x) + x]$ at $x = 2$ is

(a)
$$\frac{1}{3}$$

(b)
$$\frac{1}{2}$$

(c)
$$-\frac{1}{3}$$

(b)
$$\frac{1}{2}$$
 (c) $-\frac{1}{3}$ (d) $-\frac{1}{2}$

100. If
$$p(x)$$
 is a

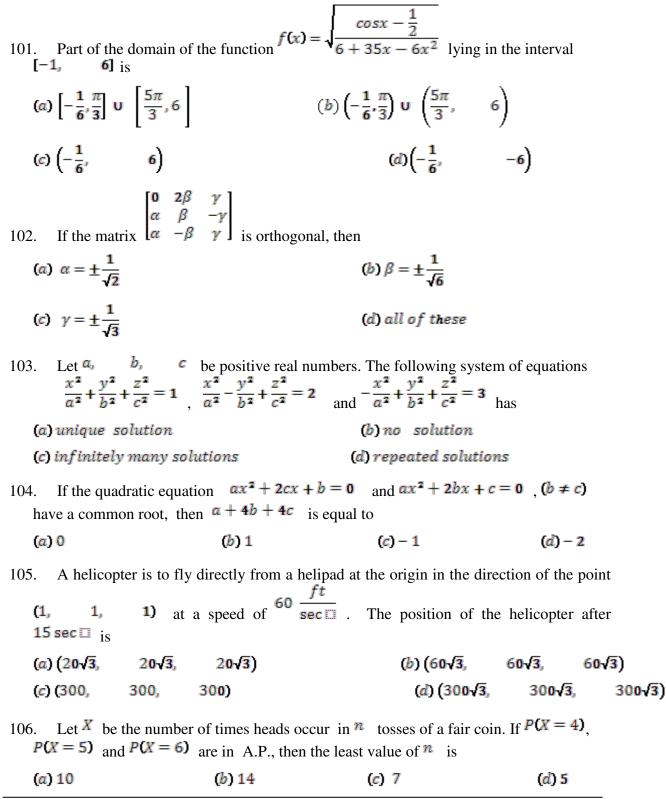
polynomial of degree three which attains its maximum value 60 at x = -3 and minimum value -84 at x = 3, then the polynomial is

(a)
$$\frac{x^3}{3} - 9x - 12$$

(b)
$$x^2 - 9x - 12$$

(c)
$$4\left(\frac{x^3}{3} - 9x\right) - 12$$

(d)
$$4\left(\frac{x^3}{3} - 9x\right) + 12$$



(a)
$$y = \frac{\varphi(x) + C}{x}$$

(c)
$$y = \varphi(x) + x + C$$

$$\frac{dy}{dx} = \frac{y\varphi(\square'(x) - y^2)}{\varphi(x)}$$
 is

(b)
$$y = \frac{\varphi(x)}{x + C}$$

(d)
$$y = \frac{\varphi(x)}{x} + C$$

108. The solution of the differential equation
$$\frac{dy}{dx} = \sin(x + y) + \cos(x + y)$$
 is

(a)
$$\log \left| 1 - \tan \left(\frac{x + y}{2} \right) \right| = y + C$$

(c)
$$\log \left| 1 + \tan \left(\frac{x+y}{2} \right) \right| = y + C$$

(b)
$$\log \left| 1 + \tan \left(\frac{x+y}{2} \right) \right| = x + C$$

(d)
$$log|1 + tan(x + y)| = x + C$$

109. The equation
$$sin^4x + cos^4x + sin2x + \beta = 0$$
 is solvable for

$$(\alpha) - \frac{5}{2} \le \beta \le \frac{1}{2}$$

$$(c) -\frac{3}{2} \le \beta \le \frac{1}{2}$$

(d)
$$-1 \le \beta \le 1$$

110. Given that
$$x=x(t)$$
 and $y=y(t)$ satisfy the equations $x+2x^{\frac{3}{2}}=t^2+t$ and $y\sqrt{1+t}+2t\sqrt{y}=4$, then $dy = dy$ at $t=0$ is

$$(a) - 6$$

$$(b) - 4$$

111. Two ships are steaming away from a point **O ' along routes that make an angle of 120°. Ship A moves at 14 knots and ship B at 21 knots. The ships are moving apart at a rate of $\Box'a \ knots'$ when OA = 5 nautical miles and OB = 3 nautical miles, where is

- (a)29.5
- (b) 28.5
- (c)29
- (d)28

112. If
$$U_n = \int_0^1 x^n tan^{-1} x dx$$
, then the value of $(n+1)U_n + (n-1)U_{n-2}$ is

- $(a)\frac{\pi}{4} \frac{1}{n}$ $(b)\frac{\pi}{4} + \frac{1}{n}$ $(c)\frac{\pi}{2} \frac{1}{n}$ $(d)\frac{\pi}{2} + \frac{1}{n}$

113. The value of
$$\int_{1}^{5} 2^{\sqrt{x-1}} dx$$
 is

$$(b)\frac{8}{\log 2} + \frac{16}{(\log 2)^2}$$

(c)
$$\frac{8}{log2} - \frac{4}{(log2)^2}$$

(d)
$$\frac{16}{\log 2} - \frac{8}{(\log 2)^2}$$

114. The pair of tangents drawn from the point $P = (h_1, k)$ to the two circles $x^2 + y^2 + 2x = 0$ and $x^2 + y^2 - 6x = 0$ coincide. Then the point P is

0)

115. Two circles pass through $(0, \pm \alpha)$ and touch the straight line x - 2y - 4 = 0. If the two circles are orthogonal, then the value of α is

$$(\alpha)\frac{3}{4}$$

$$(b)\frac{\sqrt{3}}{4}$$

(c)
$$\frac{4}{3}$$

(d)
$$\frac{3}{2}$$

116. A force $\bar{F} = 3\hat{\imath} + \hat{\jmath} - 2\hat{k}$ is applied to a spacecraft with velocity $\bar{v} = \hat{\imath} - 2\hat{\jmath}$. Then the force \bar{F} expressed as a vector which is both parallel and orthogonal to \bar{v} is

(a)
$$\frac{1}{5}(14\hat{\imath} + 7\hat{\jmath} - 2\hat{k})$$

(b)
$$\frac{1}{5} (14\hat{\imath} - 7\hat{\jmath} - 2\hat{k}) + \frac{\hat{\imath} - 2\hat{\jmath}}{\sqrt{5}}$$

$$(c)\frac{14\hat{i}}{5} + \frac{7\hat{j}}{5} - 2\hat{k} + \frac{\hat{i} - 2\hat{j}}{5}$$

(d)
$$\frac{1}{5}(14\hat{\imath} + 7\hat{\jmath} - 2\hat{k}) + \hat{\imath} - 2\hat{\jmath}$$

117. If x + 4y - 14 = 0 is the normal to the curve $y^2 = px^3 + q$ at the point $\{p_a = q\}$ is

7}

(d)
$$\{2, -7\}$$

118. $\int \frac{\log(x+1) - \log x}{x(x+1)} dx$

(a)
$$C - \frac{1}{2} \left(\log \left(1 + \frac{1}{x} \right)^2 \right)$$

(b)
$$\log\left(\frac{x+1}{x}\right) + C$$

$$(c) - \frac{1}{2} \left(\log \left(x - \frac{1}{x} \right) \right)^2 + C$$

(d)
$$2\log\left(x+\frac{1}{x}\right)+C$$

119. If $\int \frac{x^2+2}{(x^2+1)(x^2+4)} dx = p \tan \Box^{-1} \left(\frac{qx}{r+x^2}\right) + C$, then the values of p, q and r are respectively

(a) $\left\{ \frac{1}{3}, -3, -2 \right\}$ (c) $\left\{ -3, -\frac{2,1}{3} \right\}$

(b) $\left\{-\frac{1}{3}, 3, 2\right\}$ (d) $\left\{\frac{1}{3}, 3, 2\right\}$

120. The area enclosed between the two parabolas $y = 7 - 2x^2$ and $y = x^2 + 4$ is

- (a) 3
- **(b)** 4
- (c) 2
- (d)5

(Continued from the first page)

OMR ANSWER SHEET

- 1. Use the OMR answer sheet carefully; no spare sheet will be issued under any circumstance.
- 2. Do not fold or make any stray mark on the OMR sheet.
- 3. Use HB Pencil or Blue / Black ball point pen for shading the bubbles and black ball pen for writing.
- 4. In the OMR answer sheet, make the following entries
 - a. Write the Registration number, Question Booklet Number and Question Booklet Version code.
 - b. Fill the ovals corresponding to the Registration Number, Question Booklet Number and Question Booklet Version Code.
 - c. Write your Name and Signature.
- 5. Rough work should not be done on the answer sheet.

ANSWERING AND EVALUATION

- 6. For each question, four answers are suggested of which only one is correct / most appropriate. Mark the correct / most appropriate answer by darkening the corresponding bubble using HB pencil or Blue / Black ball point pen.
- 7. In case the candidate wishes to change the choice already shaded using HB pencil, he/she may erase the marking completely and thereafter shade the alternative bubble.
- 8. If more than one bubble is darkened against a question, it will be treated as an incorrect answer.
- 9. For each correct answer, three marks will be awarded.
- 10. For each incorrect answer, one mark will be deducted from the total score.
- 11. If any smudge is left on the OMR sheet, evaluation will become imperfect.