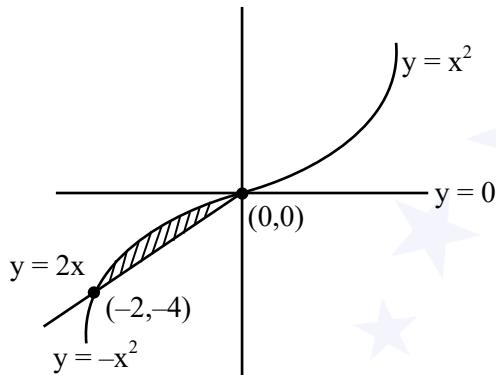


4. The area enclosed between the curves  $y = x|x|$  and  $y = x - |x|$  is :

(1)  $\frac{8}{3}$       (2)  $\frac{2}{3}$   
 (3) 1      (4)  $\frac{4}{3}$

**Ans. (4)**

**Sol.**



$$A = \int_{-2}^0 -x^2 - 2x = \frac{4}{3}$$

5. 60 words can be made using all the letters of the word BHBJO, with or without meaning. If these words are written as in a dictionary, then the 50<sup>th</sup> word is :

(1) OBBHJ      (2) HBBJO  
 (3) OBBJH      (4) JBBOH

**Ans. (3)**

**Sol.** B B H J O

$$\boxed{B} \quad 4! = 24$$

$$\boxed{H} \quad \frac{4!}{2!} = 12$$

$$\boxed{J} \quad \frac{4!}{2!} = 12$$

O B B H J

O B B J H  $\rightarrow$  50<sup>th</sup> rank

6. Let  $\vec{a} = 2\hat{i} + 5\hat{j} - \hat{k}$ ,  $\vec{b} = 2\hat{i} - 2\hat{j} + 2\hat{k}$  and  $\vec{c}$  be three vectors such that  $(\vec{c} + \hat{i}) \times (\vec{a} + \vec{b} + \hat{i}) = \vec{a} \times (\vec{c} + \hat{i})$ .  $\vec{a} \cdot \vec{c} = -29$ , then  $\vec{c} \cdot (-2\hat{i} + \hat{j} + \hat{k})$  is equal to :

(1) 10      (2) 5  
 (3) 15      (4) 12

**Ans. (2)**

**Sol.** Let's assume  $\vec{v} = \vec{a} + \vec{b} + \hat{i}$   
 $= 5\hat{i} + 3\hat{j} + \hat{k}$

and  $\vec{c} + \hat{i} = \vec{p}$

So,

$$\vec{p} \times \vec{v} = \vec{a} \times \vec{p}$$

$$\vec{p} \times \vec{v} + \vec{p} \times \vec{a} = \vec{0}$$

$$\vec{p} \times (\vec{v} + \vec{a}) = \vec{0}$$

$$\Rightarrow \vec{p} = \lambda(\vec{v} + \vec{a})$$

$$\vec{c} + \hat{i} = \lambda(7\hat{i} + 8\hat{j})$$

$$\vec{a} \cdot \vec{c} + \vec{a} \cdot \hat{i} = \lambda \vec{a} \cdot (7\hat{i} + 8\hat{j})$$

$$-29 + 2 = \lambda(14 + 40)$$

$$\lambda = -\frac{1}{2}$$

$$\vec{c} \cdot (-2\hat{i} + \hat{j} + \hat{k}) + \hat{i} \cdot (-2\hat{i} + \hat{j} + \hat{k}) = \lambda(7\hat{i} + 8\hat{j}) \cdot (-2\hat{i} + \hat{j} + \hat{k})$$

$$= -\frac{1}{2}(-14 + 8) + 2 = 5$$

7. Consider three vectors  $\vec{a}, \vec{b}, \vec{c}$ . Let  $|\vec{a}| = 2, |\vec{b}| = 3$

and  $\vec{a} = \vec{b} \times \vec{c}$ . If  $\alpha \in \left[0, \frac{\pi}{3}\right]$  is the angle between

the vectors  $\vec{b}$  and  $\vec{c}$ , then the minimum value of  $27|\vec{c} - \vec{a}|^2$  is equal to :

(1) 110      (2) 105  
 (3) 124      (4) 121

**Ans. (3)**

$$\begin{aligned}
 \text{Sol. } |\vec{c} - \vec{a}| &= |\vec{c}|^2 + |\vec{a}|^2 - 2\vec{a} \cdot \vec{c} \\
 &= |\vec{c}|^2 + 4 - 0 \\
 \therefore \vec{a} &= \vec{b} \times \vec{c} \\
 |\vec{a}| &= |\vec{b} \times \vec{c}|
 \end{aligned}$$

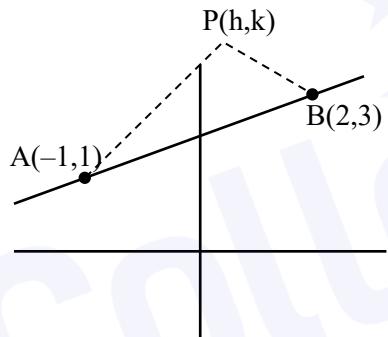
$$\begin{aligned} |\vec{c}| &= \frac{2}{3} \cosec \alpha & \alpha \in \left[ 0, \frac{\pi}{3} \right] \\ |\vec{c}|_{\min} &= \frac{2}{3} \times \frac{2}{\sqrt{3}} & \cosec \alpha \in \left[ \frac{2}{\sqrt{3}}, \infty \right) \\ \Rightarrow 27|\vec{c} - \vec{a}|_{\min}^2 &= 27 \left( \frac{16}{27} + 4 \right) = 124 \end{aligned}$$

8. Let A(-1, 1) and B(2, 3) be two points and P be a variable point above the line AB such that the area of  $\Delta PAB$  is 10. If the locus of P is  $ax + by = 15$ , then  $5a + 2b$  is :

(1)  $-\frac{12}{5}$       (2)  $-\frac{6}{5}$   
 (3) 4      (4) 6

**Ans. (1)**

Sol.



$$\frac{1}{2} \begin{vmatrix} h & k & 1 \\ -1 & 1 & 1 \\ 2 & 3 & 1 \end{vmatrix} = 10$$

$$-2x + 3y = 25$$

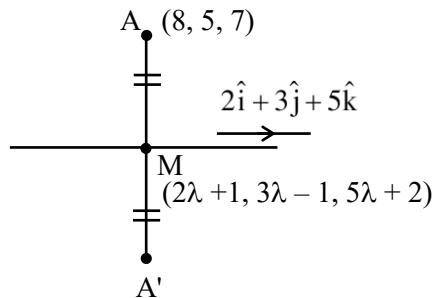
$$-\frac{6}{5}x + \frac{9}{5}y = 15$$

$$a = -\frac{6}{5}, b = \frac{9}{5}$$

$$5a = -6, 2b = \frac{18}{5}$$



Sol.



$$\overrightarrow{AM} \cdot (2\hat{i} + 3\hat{j} + 5\hat{k}) = 0$$

$$(2\lambda - 7)(2) + (3\lambda - 6)(3) + (5\lambda - 5)(5) = 0$$

$$38\lambda = 57$$

$$\lambda = \frac{3}{2}$$

$$A'(0,2,12)$$

- 10.** If the constant term in the expansion of  $\left(\frac{\sqrt[5]{3}}{x} + \frac{2x}{\sqrt[3]{5}}\right)^{12}$ ,  $x \neq 0$ , is  $\alpha \times 2^8 \times \sqrt[5]{3}$ , then  $25\alpha$  is

(3) 655

$$\text{Sol. } T_{r+1} = {}^{12}C_r \left( \frac{3^{1/5}}{x} \right)^{12-r} \left( \frac{2x}{5^{1/3}} \right)^r$$

$$\text{Sol. } T_{r+1} = {}^{12}C_r \left( \frac{3^{1/5}}{x} \right)^{12-r} \left( \frac{2x}{5^{1/3}} \right)^r$$

$$T_{r+1} = \frac{^{12}C_r (3)^{\frac{12-r}{5}} (2)^r (x)^{2r-12}}{(5)^{r/3}}$$

r = 6

$$T_7 = \frac{^{12}C_6(3)^{6/5}(2)^6}{5^2} = \left(\frac{9 \times 11 \times 7}{25}\right) 2^8 \cdot 3^{1/5}$$

$$25\alpha = 693$$

11. Let  $f, g : \mathbb{R} \rightarrow \mathbb{R}$  be defined as :  $f(x) = |x - 1|$  and  $g(x) = \begin{cases} e^x, & x \geq 0 \\ x + 1, & x \leq 0 \end{cases}$ . Then the function  $f(g(x))$  is

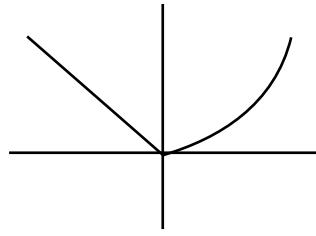
- neither one-one nor onto.
- one-one but not onto.
- both one-one and onto.
- onto but not one-one.

**Ans. (1)**

**Sol.**  $f(g(x)) = |g(x) - 1|$

$$f \circ g = \begin{cases} |e^x - 1| & x \geq 0 \\ |x+1-1| & x \leq 0 \end{cases}$$

$$f \circ g = \begin{cases} e^x - 1 & x \geq 0 \\ -x & x \leq 0 \end{cases}$$



12. Let the circle  $C_1 : x^2 + y^2 - 2(x + y) + 1 = 0$  and  $C_2$  be a circle having centre at  $(-1, 0)$  and radius 2. If the line of the common chord of  $C_1$  and  $C_2$  intersects the y-axis at the point P, then the square of the distance of P from the centre of  $C_1$  is :
- 2
  - 1
  - 6
  - 4

**Ans. (1)**

**Sol.**  $S_1 : x^2 + y^2 - 2x - 2y + 1 = 0$

$$S_2 : x^2 + y^2 + 2x - 3 = 0$$

$$\text{Common chord} = S_1 - S_2 = 0$$

$$-4x - 2y + 4 = 0$$

$$2x + y = 2 \Rightarrow P(0, 2)$$

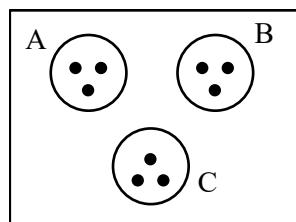
$$d_{(c,p)}^2 = (1 - 0)^2 + (2 - 1)^2 = 2$$

13. Let the set  $S = \{2, 4, 8, 16, \dots, 512\}$  be partitioned into 3 sets A, B, C with equal number of elements such that  $A \cup B \cup C = S$  and  $A \cap B = B \cap C = A \cap C = \emptyset$ . The maximum number of such possible partitions of S is equal to :

- 1680
- 1520
- 1710
- 1640

**Ans. (1)**

**Sol.**



$$\frac{9!}{(3!3!3!)^3} \times 3!$$

14. The values of m, n, for which the system of equations

$$\begin{aligned} x + y + z &= 4, \\ 2x + 5y + 5z &= 17, \\ x + 2y + mz &= n \end{aligned}$$

has infinitely many solutions, satisfy the equation :

- $m^2 + n^2 - m - n = 46$
- $m^2 + n^2 + m + n = 64$
- $m^2 + n^2 + mn = 68$
- $m^2 + n^2 - mn = 39$

**Ans. (4)**

**Sol.**  $D = \begin{vmatrix} 1 & 1 & 1 \\ 2 & 5 & 5 \\ 1 & 2 & m \end{vmatrix} = 0 \Rightarrow m = 2$

$$D_3 = \begin{vmatrix} 1 & 1 & 4 \\ 2 & 5 & 17 \\ 1 & 2 & n \end{vmatrix} = 0 \Rightarrow n = 7$$

15. The coefficients a, b, c in the quadratic equation  $ax^2 + bx + c = 0$  are from the set  $\{1, 2, 3, 4, 5, 6\}$ . If the probability of this equation having one real root bigger than the other is p, then  $216p$  equals :

- 57
- 38
- 19
- 76

**Ans. (2)**

**Sol.**  $D > 0$

$$b^2 > 4ac$$

$$b = 3 : (a, c) = (1, 1)(1, 2)(2, 1)$$

$$b = 4 : (a, c) = (1, 1)(1, 2)(2, 1)(1, 3)(3, 1)$$

$$b = 5 : (a, c) = (1, 1)(1, 2)(2, 1)(1, 3)(3, 1)(1, 4)(4, 1)$$

$$(1, 5)(5, 1)(1, 6)(6, 1)(2, 3)(3, 2)(2, 2)$$

$$b = 6 : (a, c) = (1, 1)(1, 2)(2, 1)(1, 3)(3, 1)(1, 4)(4, 1)$$

$$(1, 5)(5, 1)(1, 6)(6, 1)(2, 3)(3, 2)(2, 4)(4, 2)(2, 2)$$

fav. cases = 38

$$\text{Prob.} : \frac{38}{6 \times 6 \times 6}$$

- 16.** Let ABCD and AEFG be squares of side 4 and 2 units, respectively. The point E is on the line segment AB and the point F is on the diagonal AC. Then the radius r of the circle passing through the point F and touching the line segments BC and CD satisfies :

$$(1) r = 1$$

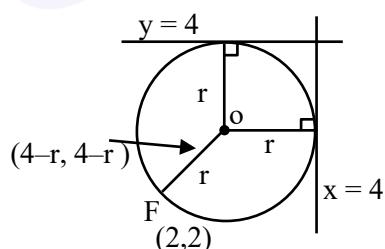
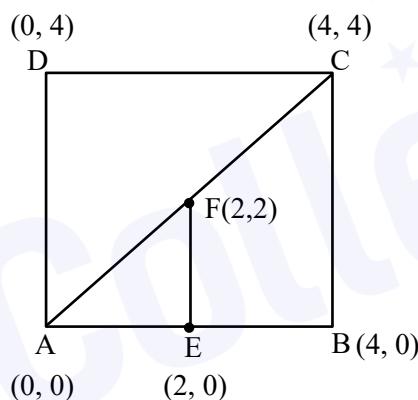
$$(2) r^2 - 8r + 8 = 0$$

$$(3) 2r^2 - 4r + 1 = 0$$

$$(4) 2r^2 - 8r + 7 = 0$$

**Ans. (2)**

**Sol.**



$$OF^2 = r^2$$

$$(2-r)^2 + (2-r)^2 = r^2$$

$$r^2 - 8r + 8 = 0$$

- 17.** Let  $\beta(m, n) = \int_0^1 x^{m-1}(1-x)^{n-1} dx$ ,  $m, n > 0$ . If  $\int_0^1 (1-x^{10})^{20} dx = a \times \beta(b, c)$ , then  $100(a + b + c)$  equals \_\_\_\_\_.

$$(1) 1021$$

$$(2) 1120$$

$$(3) 2012$$

$$(4) 2120$$

**Ans. (4)**

$$\text{Sol. } I = \int_0^1 1 \cdot (1-x^{10})^{20} dx$$

$$x^{10} = t$$

$$x = t^{1/10}$$

$$dx = \frac{1}{10} t^{-9/10} dt$$

$$I = \int_0^1 (1-t)^{20} \frac{1}{10} t^{-9/10} dt$$

$$I = \frac{1}{10} \int_0^1 t^{-9/10} (1-t)^{20} dt$$

$$a = \frac{1}{10} \quad b = \frac{1}{10} \quad c = 21$$

- 18.** Let  $\alpha\beta \neq 0$  and  $A = \begin{bmatrix} \beta & \alpha & 3 \\ \alpha & \alpha & \beta \\ -\beta & \alpha & 2\alpha \end{bmatrix}$ .

$$\text{If } B = \begin{bmatrix} 3\alpha & -9 & 3\alpha \\ -\alpha & 7 & -2\alpha \\ -2\alpha & 5 & -2\beta \end{bmatrix}$$

is the matrix of cofactors of the elements of A, then  $\det(AB)$  is equal to :

$$(1) 343$$

$$(2) 125$$

$$(3) 64$$

$$(4) 216$$

**Ans. (4)**

**Sol.** Equating co-factor fo  $A_{21}$

$$(2\alpha^2 - 3\alpha) = \alpha$$

$$\alpha = 0, 2 \text{ (accept)}$$

$$\text{Now, } 2\alpha^2 - \alpha\beta = 3\alpha$$

$$\alpha = 2 \quad \beta = 1$$

$$|AB| = |A \text{ cof}(A)| = |A|^3$$

$$A = \begin{vmatrix} 1 & 2 & 3 \\ 2 & 2 & 1 \\ -1 & 2 & 4 \end{vmatrix} = 6 - 2(9) + 3(6) = 6$$



**Sol.** IF =  $e^{\int \frac{2x}{(1+x^2)^2} dx} = e^{\frac{-1}{1+x^2}}$

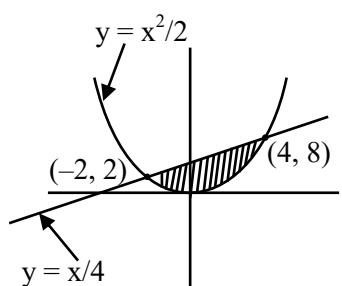
$$y \cdot e^{\frac{-1}{1+x^2}} = \int x \cdot e^{\frac{-1}{1+x^2}} \cdot e^{\frac{-1}{1+x^2} dx}$$

$$y \cdot e^{\frac{-1}{1+x^2}} = \frac{x^2}{2} + c$$

$$(0, 0) \Rightarrow C = 0$$

$$y(x) = \frac{x^2}{2} e^{\frac{-1}{1+x^2}}$$

$$f(x) = \frac{x^2}{2}$$



$$A = \int_{-2}^4 (x+4) - \frac{x^2}{2} dx = 18$$

- 23.** The number of solutions of  $\sin^2 x + (2 + 2x - x^2)\sin x - 3(x - 1)^2 = 0$ , where  $-\pi \leq x \leq \pi$ , is

**Ans. (2)**

**Sol.**  $\sin^2 x - (x^2 - 2x - 2)\sin x - 3(x - 1)^2 = 0$

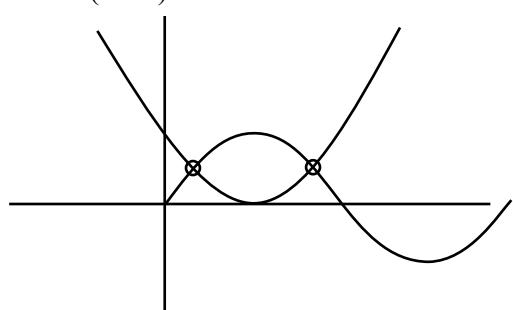
$$\sin^2 x - (x - 1)^2 \sin x - 3(x - 1)^2 = 0$$

roots :

$$-3 \quad (x-1)^2$$

$$\sin x = -3 \text{ (reject) or } (x-1)^2$$

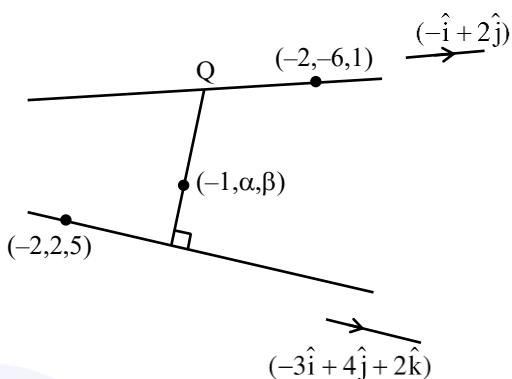
$$\sin x = (x-1)^2$$



- 24.** Let the point  $(-1, \alpha, \beta)$  lie on the line of the shortest distance between the lines  $\frac{x+2}{-3} = \frac{y-2}{4} = \frac{z-5}{2}$  and  $\frac{x+2}{-1} = \frac{y+6}{2} = \frac{z-1}{0}$ . Then  $(\alpha - \beta)^2$  is equal to \_\_\_\_\_.

**Ans. (25)**

**Sol.**



$$P(-3\lambda - 2, 4\lambda + 2, 2\lambda + 5)$$

$$Q(-\mu - 2, 2\mu - 6, 1)$$

$$\text{DRS of } PQ = (3\lambda - \mu, 2\mu - 4\lambda - 8, -2\lambda - 4)$$

$$\text{DRS of } PQ = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -1 & 2 & 0 \\ -3 & 4 & 2 \end{vmatrix}$$

$$= (4\hat{i} + 2\hat{j} + 2\hat{k})$$

OR

$$(2, 1, 1)$$

$$\frac{3\lambda - \mu}{2} = \frac{2\mu - 4\lambda - 8}{1} = \frac{-2\lambda - 4}{1}$$

$$\Rightarrow \mu = \lambda + 2 \text{ & } 7\lambda = \mu - 8$$

$$\boxed{\lambda = -1} \quad \boxed{\mu = 1}$$

$$Q : (-3, -4, 1)$$

$$L_{PQ} = \frac{x+3}{2} = \frac{y+4}{1} = \frac{z-1}{1}$$

$$(-1, \alpha, \beta) \Rightarrow 1 = \frac{\alpha + 4}{1} = \frac{\beta - 1}{1}$$

$$\Rightarrow \alpha = -3, \beta = 2$$

$$(\alpha - \beta)^2 = 25$$

**25.** If

$$1 + \frac{\sqrt{3} - \sqrt{2}}{2\sqrt{3}} + \frac{5 - 2\sqrt{6}}{18} + \frac{9\sqrt{3} - 11\sqrt{2}}{36\sqrt{3}} + \frac{49 - 20\sqrt{6}}{180} + \dots$$

upto  $\infty$  =  $2 \left( \sqrt{\frac{b}{a}} + 1 \right) \log_e \left( \frac{a}{b} \right)$ , where a and b are

integers with  $\gcd(a, b) = 1$ , then  $11a + 18b$  is equal to \_\_\_\_\_.

**Ans. (76)**

**Sol.**  $S = 1 + \frac{x}{2\sqrt{3}} + \frac{x^2}{18} + \frac{x^3}{36\sqrt{3}} + \frac{x^4}{180} + \dots \infty$

Put  $\frac{x}{\sqrt{3}} = t$ , where  $x = \sqrt{3} - \sqrt{2}$

$$S = 1 + \frac{t}{2} + \frac{t^2}{6} + \frac{t^3}{12} + \frac{t^4}{20} + \dots$$

$$S = 1 + t \left( 1 - \frac{1}{2} \right) + t^2 \left( \frac{1}{2} - \frac{1}{3} \right) + t^3 \left( \frac{1}{3} - \frac{1}{4} \right) + t^4 \left( \frac{1}{4} - \frac{1}{5} \right)$$

$$S = \left( 1 + t + \frac{t^2}{2} + \frac{t^3}{3} + \frac{t^4}{4} + \dots \right) - \left( \frac{t}{2} + \frac{t^2}{3} + \frac{t^3}{4} + \frac{t^4}{5} + \dots \right)$$

$$S = \left( t + \frac{t^2}{2} + \dots \right) - \frac{1}{t} \left( t + \frac{t^2}{2} + \frac{t^3}{3} + \dots \right) + 2$$

$$S = 2 + \left( 1 - \frac{1}{t} \right) (-\log(1-t)) = \left( \frac{1}{t} - 1 \right) \log(1-t) + 2$$

$$S = 2 + \left( \frac{\sqrt{3}}{\sqrt{3} - \sqrt{2}} - 1 \right) \log \left( 1 - \frac{\sqrt{3} - \sqrt{2}}{\sqrt{3}} \right)$$

$$S = 2 + \left( \frac{\sqrt{2}}{\sqrt{3} - \sqrt{2}} \right) \log e \frac{\sqrt{2}}{\sqrt{3}}$$

$$S = 2 + \frac{(\sqrt{6} + 2)}{2} \log e \frac{2}{3} = 2 + \left( \sqrt{\frac{3}{2}} + 1 \right) \log e \frac{2}{3}$$

$$a = 2, b = 3$$

$$11a + 18b = 11 \times 2 + 18 \times 3 = 76$$

**26.** Let  $a > 0$  be a root of the equation  $2x^2 + x - 2 = 0$ .

If  $\lim_{x \rightarrow \frac{1}{a}} \frac{16(1 - \cos(2 + x - 2x^2))}{(1 - ax^2)} = \alpha + \beta\sqrt{17}$ , where

$\alpha, \beta \in \mathbb{Z}$  then  $\alpha + \beta$  is equal to \_\_\_\_\_.

**Ans. (170)**

**Sol.**  $2x^2 + x - 2 = 0$

$$2x^2 - x - 2 = 0$$

$$\lim_{x \rightarrow \frac{1}{a}} 16 \cdot \frac{\left(1 - \cos 2\left(x - \frac{1}{a}\right)\left(x - \frac{1}{b}\right)\right)}{4\left(x - \frac{1}{b}\right)^2} \times \frac{4\left(x - \frac{1}{b}\right)^2}{a^2\left(x - \frac{1}{a}\right)^2}$$

$$= 16 \times \frac{2}{a^2} \left( \frac{1}{a} - \frac{1}{b} \right)^2$$

$$= \frac{32}{a^2} \left( \frac{17}{4} \right) = \frac{17.8}{a^2} = \frac{17 \times 8 \times 16}{(-1 + \sqrt{117})^2}$$

$$= \frac{136.16}{18.2\sqrt{7}} \times \frac{18 + 2\sqrt{7}}{18 + 2\sqrt{7}}$$

$$= \frac{136}{256} (18 + 2\sqrt{7}) \cdot 16$$

$$= 153 + 17\sqrt{17} = \alpha + \beta\sqrt{17}$$

$$\alpha + \beta = 153 + 17 = 170$$

**27.** If  $f(t) = \int_0^\pi \frac{2x dx}{1 - \cos^2 t \sin^2 x}$ ,  $0 < t < \pi$ , then the value

of  $\int_0^{\frac{\pi}{2}} \frac{\pi^2 dt}{f(t)}$  equals \_\_\_\_\_.

**Ans. (1)**

**Sol.**  $f(t) = \int_0^\pi \frac{2x}{1 - \cos^2 t \sin^2 x} dx \quad \dots(1)$

$$= 2 \int_0^{\pi} \frac{(\pi - x) dx}{1 - \cos^2 t \sin^2 x} \quad \dots(2)$$

$$2f(t) = 2 \int_0^{\pi} \frac{\pi}{1 - \cos^2 t \sin^2 x} dx$$

$$f(t) = \int_0^{\pi} \frac{\pi}{1 - \cos^2 t \sin^2 x} dx$$

divide & by  $\cos^2 x$

$$f(t) = \pi \int_0^{\pi} \frac{\sec^2 x dx}{\sec^2 x - \cos^2 t \tan^2 x}$$

$$f(t) = 2\pi \int_0^{\pi/2} \frac{\sec^2 x dx}{\sec^2 x - \cos^2 t \tan^2 x}$$

$\tan x = z$

$$\sec^2 x dx = dz$$

$$f(t) = 2\pi \int_0^{\infty} \frac{dz}{1 + \sin^2 t \cdot z^2}$$

$$= \frac{\pi^2}{\sin t}$$

$$\text{Then } \int_0^{\pi/2} \frac{\pi^2}{f(t)} dt$$

$$= \int_0^{\pi/2} \sin t dt$$

$$= 1$$

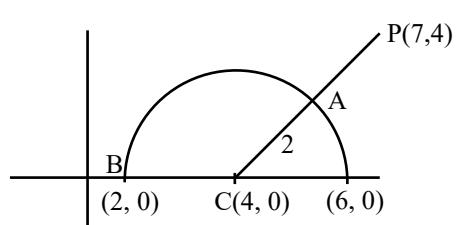
28. Let the maximum and minimum values of  $(\sqrt{8x - x^2 - 12} - 4)^2 + (x - 7)^2$ ,  $x \in \mathbb{R}$  be M and m respectively. Then  $M^2 - m^2$  is equal to \_\_\_\_\_.  
**Ans. (1600)**

**Sol.**  $(x - 7)^2 + (y - 4)^2$

$$y = \sqrt{8x - x^2 - 12}$$

$$y^2 = -(x - 4)^2 + 16 - 12$$

$$(x - 4)^2 + y^2 = 4$$



$$m = 9$$

$$M = 41$$

$$M^2 - m^2 = 41^2 - 9^2 = 1600$$

29. Let a line perpendicular to the line  $2x - y = 10$  touch the parabola  $y^2 = 4(x - 9)$  at the point P. The distance of the point P from the centre of the circle  $x^2 + y^2 - 14x - 8y + 56 = 0$  is \_\_\_\_\_.  
**Ans. (10)**

**Sol.**  $y^2 = 4(x - 9)$

$$\text{slope of tangent} = \frac{-1}{2}$$

$$\text{Point of contact } P\left(9 + \frac{1}{(-\frac{1}{2})^2}, \frac{2 \times 1}{-\frac{1}{2}}\right)$$

$$P(13, -4)$$

$$\text{center of circle } C(7, 4)$$

$$\text{distance } CP = \sqrt{(13 - 7)^2 + (-4 - 4)^2} \\ = 10$$

30. The number of real solutions of the equation  $x|x + 5| + 2|x + 7| - 2 = 0$  is \_\_\_\_\_.  
**Ans. (3)**

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**Allen Ans. (3)**

- Sol.** **Case I :**  $x \geq -5$

$$x^2 + 5x + 2x + 12 = 0$$

$$x^2 + 7x + 12 = 0$$

$$x = -3, -4$$

- Case II :**  $-7 < x < -5$

$$-x^2 - 5x + 2x + 14 - 2 = 0$$

$$-x^2 - 3x + 12 = 0$$

$$x = \frac{-3 \pm \sqrt{9 + 48}}{2}$$

$$= \frac{-3 \pm \sqrt{57}}{2}$$

$$x = \frac{-3 - \sqrt{57}}{2}, \frac{-3 + \sqrt{57}}{2} \text{ (rejected)}$$

**Case III :**  $x \leq -7$

$$-x^2 - 5x - 2x - 14 - 2 = 0$$

$$x^2 + 7x + 16 = 0$$

$$D = 49 - 64 < 0$$

No solutions

No. of solutions = 3