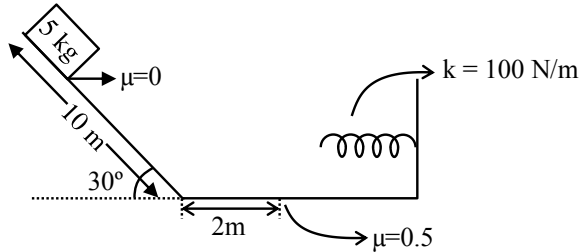# FINAL JEE–MAIN EXAMINATION – APRIL, 2024

(Held On Monday 08th April, 2024)   **TIME : 3 : 00 PM to 6 : 00 PM**

SECTION-A

31.

A block is simply released from the top of an inclined plane as shown in the figure above. The maximum compression in the spring when the block hits the spring is :

(1) $\sqrt{6}$m (2) 2 m

(3) 1 m (4) $\sqrt{5}$m
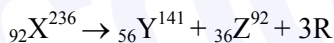
Ans. (2)

Sol. $w_g + w_{Fr} + w_s = \Delta KE$

$5 \times 10 \times 5 - 0.5 \times 5 \times 10 \times x - \dfrac{1}{2}Kx^2 = 0 - 0$

$250 = 25x + 50x^2$

$2x^2 + x - 10 = 0$

$x = 2$

32. In a hypothetical fission reaction

$_{92}X^{236} \rightarrow \, _{56}Y^{141} + \, _{36}Z^{92} + 3R$

The identity of emitted particles (R) is :

(1) Proton (2) Electron

(3) Neutron (4) γ-radiations

Ans. (3)

Sol. Z in LHS = 92

Z in RHS = 56 + 36 = 92

A in LHS = 236

A in RHS = 141 + 92 = 233

So 3 neutrons are released.

33. If $\in_0$ is the permittivity of free space and E is the electric field, then $\in_0 E^2$ has the dimensions :

(1) $[M^o L^{-2} T A]$ (2) $[M L^{-1} T^{-2}]$
(3) $[M^{-1} L^{-3} T^4 A^2]$ (4) $[M L^2 T^{-2}]$

Ans. (2)

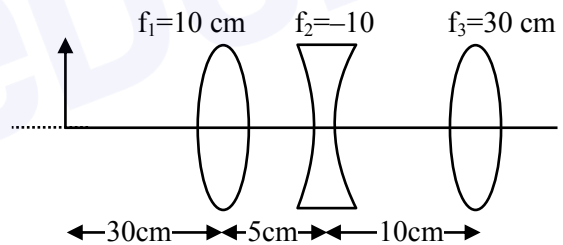**Sol.** $E = \dfrac{KQ}{R^2}$

$E = \dfrac{Q}{4\pi\varepsilon_o R^2}$

$\varepsilon_o = \dfrac{Q}{4\pi R^2 E}$

Now, $\varepsilon_o E^2 = \dfrac{Q}{4\pi R^2 E} \cdot E^2 = \dfrac{Q}{4\pi R^2} \cdot E$

$[\varepsilon_o E^2] = \left[\dfrac{QE}{R^2}\right] = \dfrac{[Q][E]}{[R^2]} = \dfrac{[Q]}{[R^2]}\dfrac{[W]}{[Q][R]}$

$= \dfrac{[W]}{[R^3]} = \dfrac{ML^2 T^{-2}}{L^3} = ML^{-1}T^{-2}$

34. The position of the image formed by the combination of lenses is :

(1) 30 cm (right of third lens)
(2) 15 cm (left of second lens)
(3) 30 cm (left of third lens)
(4) 15 cm (right of second lens)

Ans. (1)

Sol. **For lens 1 :** $f_1 = 10$, $u = -30$, $v = ?$

$$v = \dfrac{uf}{u+f} = \dfrac{-30 \times 10}{-30+10} = 15$$

For lens 2 : $f_1 = -10$, $u = 10$, $v = ?$

$$v = \dfrac{uf}{u+f} = \dfrac{10 \times -10}{10-10} = \infty$$

For lens 3 : $f = 30$, $u = -\infty$, $v = ?$
So v will be 30.

35. A plane progressive wave is given by $y = 2 \cos 2\pi(330\,t - x)$ m. The frequency of the wave is :

(1) 165 Hz   (2) 330 Hz

(3) 660 Hz   (4) 340 Hz

Ans. (2)

Sol. $y = 2 \cos 2\pi(330\,t - x)$ m

$y = A\cos(\omega t - kx)$

by comparing $\omega = 2\pi \times 330$

$2\pi f = 2\pi \times 330$

$f = 330$

36. A thin circular disc of mass M and radius R is rotating in a horizontal plane about an axis passing through its centre and perpendicular to its plane with angular velocity ω. If another disc of same dimensions but of mass $M/2$ is placed gently on the first disc co-axially, then the new angular velocity of the system is :

(1) $\dfrac{4}{5}\omega$ (2) $\dfrac{5}{4}\omega$

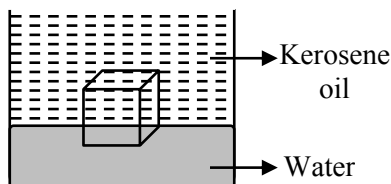(3) $\dfrac{2}{3}\omega$ (4) $\dfrac{3}{2}\omega$

Ans. (3)

Sol. $I_1\omega = I_2\omega_2$

$\dfrac{MR^2}{2}\omega = \dfrac{3}{2}\left(\dfrac{MR^2}{2}\right)\omega_2$

$\omega_2 = \dfrac{2}{3}\omega$

37. A cube of ice floats partly in water and partly in kerosene oil. The radio of volume of ice immersed in water to that in kerosene oil (specific gravity of Kerosene oil = 0.8, specific gravity of ice = 0.9)

(1) 8 : 9   (2) 5 : 4

(3) 9 : 10   (4) 1 : 1

Ans. (4)

Sol. v_1 = volume immersed in water.

v_2 = volume immersed in oil.

$v_1\,\rho_w\,g + v_2\,\rho_o\,g = (v_1 + v_2)\,\rho_c\,g$

$v_1 + \dfrac{v_2\rho_o}{\rho_w} = (v_1 + v_2)\ \dfrac{\rho_c}{\rho_w}$

$= v_1 + 0.8\,v_2 = 0.9\,v_1 + 0.9\,v_2$

$= 0.1\,v_1 = 0.1\,v_2$

$v_1 : v_2 = 1 : 1$

38. Given below are two statements :

Statement (I) : The mean free path of gas molecules is inversely proportional to square of molecular diameter.

Statement (II) : Average kinetic energy of gas molecules is directly proportional to absolute temperature of gas.

In the light of the above statements, choose the correct answer from the option given below:

(1) **Statement I** is false but **Statement II** is true.

(2) **Statement I** is true but **Statement II** is false.

(3) Both **Statement I** and **Statement II** are false

(4) Both **Statement I** and **Statement II** are true.

Ans. (4)

Sol.

$\sqrt{2}\pi d^2 N_A P$

$KE = \dfrac{f}{2}nRT$

39. Two satellite A and B go round a planet in circular orbits having radii 4 R and R respectively. If the speed of A is $3v$, the speed of B will be :

(1) $\dfrac{4}{3}v$ (2) $3v$

(3) $6v$ (4) $12v$

Ans. (3)

Sol. $v = \sqrt{\dfrac{GM}{R}}$

$\dfrac{v_A}{v_B} = \sqrt{\dfrac{R_B}{R_A}} = \sqrt{\dfrac{R}{4R}} = \dfrac{1}{2}$

$v_B = 2v_A = 6v$

40. A long straight wire of radius a carries a steady current I. The current is uniformly distributed across its cross section. The ratio of the magnetic field at $\frac{a}{2}$ and 2a from axis of the wire is :

(1) 1 : 4   (2) 4 : 1

(3) 1 : 1   (4) 3 : 4

Ans. (3)

Sol. $B_1 2\pi \frac{a}{2} = \mu_o \frac{I}{4}$

$B_1 = \frac{\mu_o I}{4\pi a}$

$B_2 2\pi 2a = \mu_o I$

$B_2 = \frac{\mu_o I}{4\pi a}$

41. The angle of projection for a projectile to have same horizontal range and maximum height is :

(1) $\tan^{-1}(2)$ (2) $\tan^{-1}(4)$

(3) $\tan^{-1}\left(\frac{1}{4}\right)$ (4) $\tan^{-1}\left(\frac{1}{2}\right)$

Ans. (2)

Sol. $\frac{u^2 \sin 2\theta}{g} = \frac{u^2 \sin^2 \theta}{2g}$

$4\sin\theta \cos\theta = \sin^2\theta$

$4 = \tan\theta$

42. Water boils in an electric kettle in 20 minutes after being switched on. Using the same main supply, the length of the heating element should be ………….. to …………. times of its initial length if the water is to be boiled in 15 minutes.

(1) increased, $\frac{3}{4}$ (2) increased, $\frac{4}{3}$

(3) decreased, $\frac{3}{4}$ (4) decreased, $\frac{4}{3}$

Ans. (3)

Sol. $P = \frac{v^2}{R}$, $R = \frac{\rho\ell}{A}$

$P \propto \frac{1}{\ell}$

$\frac{P_1}{P_2} = \frac{t_2}{t_1} = \frac{15}{20} = \frac{\ell_2}{\ell_1}$

$\ell_2 = \frac{3}{4}\ell_1$

43. A capacitor has air as dielectric medium and two conducting plates of area 12 cm^2 and they are 0.6 cm apart. When a slab of dielectric having area 12 cm^2 and 0.6 cm thickness is inserted between the plates, one of the conducting plates has to be moved by 0.2 cm to keep the capacitance same as in previous case. The dielectric constant of the slab is : (Given $\epsilon_0 = 8.834 \times 10^{-12}$ F/m)

(1) 1.50   (2) 1.33

(3) 0.66   (4) 1

Ans. (1)

Sol. $\frac{A\varepsilon_o}{d} = \frac{A\varepsilon_o}{\left(0.2 + \frac{d}{k}\right)}$

$0.6 = 0.2 + \frac{0.6}{k}$

$k = \frac{3}{2}$

44. A given object takes n times the time to slide down 45° rough inclined plane as it takes the time to slide down an identical perfectly smooth 45° inclined plane. The coefficient of kinetic friction between the object and the surface of inclined plane is :

(1) $1 - \frac{1}{n^2}$ (2) $1 - n^2$

(3) $\sqrt{1 - \frac{1}{n^2}}$ (4) $\sqrt{1 - n^2}$

Ans. (1)

Sol.

Case-1 : No friction

$a = g\sin\theta$

$\ell = \frac{1}{2}(g\sin\theta)t_1^2$

$t_1 = \sqrt{\frac{2\ell}{g\sin\theta}}$

Case-2 : With friction

$$a = g\sin\theta - \mu g\cos\theta$$

$$\ell = \frac{1}{2}(g\sin\theta - \mu g\cos\theta)t_2^2$$

$$\sqrt{\frac{2\ell}{g\sin\theta - \mu g\cos\theta}} = n\sqrt{\frac{2\ell}{g\sin\theta}}$$
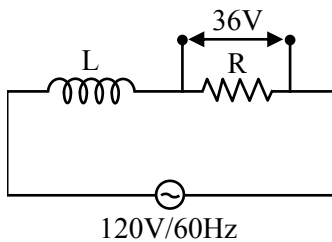
$$\mu = 1 - \frac{1}{n^2}$$

45. A coil of negligible resistance is connected in series with 90 Ω resistor across 120 V, 60 Hz supply. A voltmeter reads 36 V across resistance. Inductance of the coil is :

(1) 0.76 H   (2) 2.86 H

(3) 0.286 H   (4) 0.91 H

Ans. (1)

Sol.

$$36 = I_{rms}\, R$$

$$36 = \frac{120}{\sqrt{X_L^2 + R^2}} \times R$$

$$R = 90\,\Omega \Rightarrow 36 = \frac{120 \times 90}{\sqrt{X_L^2 + 90^2}}$$

$$\sqrt{X_L^2 + 90^2} = 300$$

$$X_L^2 = 81900$$

$$X_L = 286.18$$

$$\omega L = 286.18$$

$$L = \frac{286.18}{376.8}$$

$$L = 0.76\,H$$

46. There are 100 divisions on the circular scale of a screw gauge of pitch 1 mm. With no measuring quantity in between the jaws, the zero of the circular scale lies 5 divisions below the reference line. The diameter of a wire is then measured using this screw gauge. It is found the 4 linear scale divisions are clearly visible while 60 divisions on circular scale coincide with the reference line. The diameter of the wire is :

(1) 4.65 mm   (2) 4.55 mm

(3) 4.60 mm   (4) 3.35 mm

Ans. (2)

Sol. Least count = $\frac{1}{100}$ mm = 0.01mm

zero error = +0.05 mm

Reading = 4 × 1 mm + 60 × 0.01 mm – 0.05 mm

= 4.55 mm

47. A proton and an electron have the same de Broglie wavelength. If K_p and K_e be the kinetic energies of proton and electron respectively. Then choose the correct relation :

(1) $K_p > K_e$ (2) $K_p = K_e$

(3) $K_p = K_e^2$ (4) $K_p < K_e$

Ans. (4)

Sol. De Broglie wavelength of proton & electron = λ

$$\because \lambda = \frac{h}{p}$$

$$\therefore p_{proton} = p_{electron}$$

$$\because KE = \frac{p^2}{2m}$$

$$\therefore KE_{proton} < KE_{electron}$$

$$[K_p < K_e]$$

48. Least count of a vernier caliper is $\frac{1}{20N}$ cm. The value of one division on the main scale is 1 mm. Then the number of divisions of main scale that coincide with N divisions of vernier scale is :

(1) $\left(\frac{2N-1}{20N}\right)$ (2) $\left(\frac{2N-1}{2}\right)$

(3) $(2N-1)$ (4) $\left(\frac{2N-1}{2N}\right)$

Ans. (2)

Sol. Least count of vernier calipers $= \dfrac{1}{20N}$ cm

∵ Least count = 1 MSD – 1 VSD

let x no. of divisions of main scale coincides with N division of vernier scale, then

$1 \text{ VSD} = \dfrac{x \times 1mm}{N}$

$\therefore \dfrac{1}{20N} \text{cm} = 1 \text{ mm} - \dfrac{x \times 1mm}{N}$

$\dfrac{1}{2N} \text{mm} = 1\text{mm} - \dfrac{x}{N}\text{mm}$

$x = \left(1 - \dfrac{1}{2N}\right) N$

$x = \dfrac{2N-1}{2}$

49. If M_o is the mass of isotope $^{12}_{5}B$, M_p and M_n are the masses of proton and neutron, then nuclear binding energy of isotope is :
(1) $(5 M_p + 7M_n - M_o)C^2$
(2) $(M_o - 5M_p)C^2$
(3) $(M_o - 12M_n)C^2$
(4) $(M_o - 5M_p - 7M_n)C^2$

Ans. (1)

Sol. B.E. = $\Delta m C^2$

$(5 M_p + 7M_n - M_o)C^2$

50. A diatomic gas ($\gamma = 1.4$) does 100 J of work in an isobaric expansion. The heat given to the gas is :
(1) 350 J   (2) 490 J
(3) 150 J   (4) 250 J

Ans. (1)

For Isobaric process

$w = P\Delta v = nR\Delta T = 100$ J

$Q = \Delta u + w$

$\Delta Q = \dfrac{F}{2}nR\Delta T + nR\Delta T$

$\left(\dfrac{f}{2}+1\right)nR\Delta T$

$\left(\dfrac{5}{2}+1\right)100 = 350$ J

SECTION-B

51. The coercivity of a magnet is 5×10^3 A/m. The amount of current required to be passed in a solenoid of length 30 cm and the number of turns 150, so that the magnet gets demagnetised when inside the solenoid is …………A.

Ans. (10)

Sol.

$H_c = \dfrac{\mu_o ni}{\mu_o}$
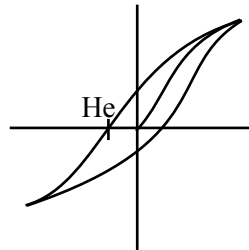
$5 \times 10^3 = \dfrac{150}{30} \times 100 \times i$

$\dfrac{50}{5} = i$

I = 10

52. Small water droplets of radius 0.01 mm are formed in the upper atmosphere and falling with a terminal velocity of 10 cm/s. Due to condensation, if 8 such droplets are coalesced and formed a larger drop, the new terminal velocity will be ………..cm/s.

Ans. (40)

Sol. m = mass of small drop

M = mass of bigger drop

$V_t = \dfrac{2}{9}\dfrac{R^2(\rho - \sigma)g}{\eta}$

$8 \propto m = M$
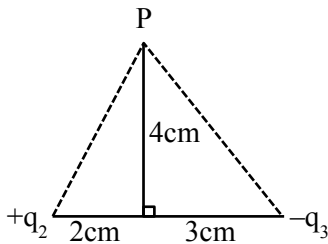
$8r^3 = R^3 \Rightarrow R = 2R$

as $V_t \times R^2$ ∵ Radius double so V_t becomes 4 time
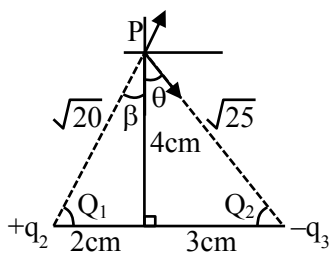
$\therefore 4 \times 10 = 40$ cm/s

53. If the net electric field at point P along Y axis is zero, then the ratio of $\left|\dfrac{q_2}{q_3}\right|$ is $\dfrac{8}{5\sqrt{x}}$,

where x = …………..

P

4cm

$+q_2$ 2cm   3cm $-q_3$

Ans. (5)

Sol.

P

$\sqrt{20}$ β θ $\sqrt{25}$

4cm

Q_1 Q_2

$+q_2$ 2cm   3cm $-q_3$

$\dfrac{Kq_2}{20}\cos\beta = \dfrac{Kq_3}{25}\cos\theta$

$\dfrac{Kq_2}{20}\dfrac{4}{\sqrt{20}} = \dfrac{Kq_3}{25}\dfrac{4}{\sqrt{25}}$

$\dfrac{q_2}{q_3} = \dfrac{25}{20}\sqrt{\dfrac{25}{20}} = \dfrac{8}{5\sqrt{x}}$

$\Rightarrow \sqrt{x} = \dfrac{8\times25\sqrt{25}}{5\times20\sqrt{20}}$

x = 5

54. A heater is designed to operate with a power of 1000 W in a 100 V line. It is connected in combination with a resistance of 10 Ω and a resistance R, to a 100 V mains as shown in figure. For the heater to operate at 62.5 W, the value of R should be ……………. Ω.

B   C
heater
10Ω
R
100 V
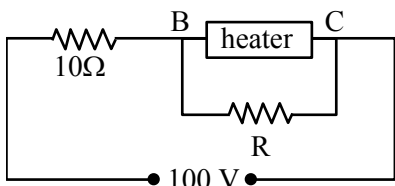
Ans. (5)

Sol. $R_{heater} = \dfrac{V^2}{P} = \dfrac{(100)^2}{1000} = 10\,\Omega$

For heater $P = \dfrac{V^2}{R} \Rightarrow V = \sqrt{PR}$

$V = \sqrt{62.5\times10}$

$V = 25\ v$

10Ω
i_1 i_H heater
10Ω
←75V→
i_R R
←25V→
100 V
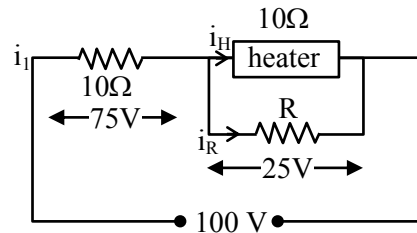
$i_1 = \dfrac{75}{10} = 7.5A,\quad i_H = \dfrac{25}{10} = 2.5\ A.$

$i_R = i_1 - i_H = 5$

$V = IR$

$R = \dfrac{25}{5} = 5\,\Omega$

55. An alternating emf $E = 110\sqrt{2}\sin 100t$ volt is applied to a capacitor of 2μF, the rms value of current in the circuit is ………. mA.

Ans. (22)

Sol. $C = 2\mu f;\quad E = 110\sqrt{2}\sin(100\,t)$

$X_C = \dfrac{1}{\omega c} = \dfrac{1}{100\times2\times10^6}$

$= \dfrac{10000}{2} = 5000\,\Omega$

$i_o = \dfrac{110\sqrt{2}}{5000}$

$i_{rms} = \dfrac{110\sqrt{2}}{5000\sqrt{2}}$

$= \dfrac{110}{5}\,mA$

$= 22\ mA$

56. Two slits are 1 mm apart and the screen is located 1 m away from the slits. A light wavelength 500 nm is used. The width of each slit to obtain 10 maxima of the double slit pattern within the central maximum of the single slit pattern is ……….. $\times 10^{-4}$ m.

Ans. (2)

Sol. $d = 1$ mm, $D = 1$m, $\lambda = 500$ nm

$$10\left(\frac{\lambda D}{d}\right) = \frac{2\lambda D}{a}$$

$$\mathbf{a} = \frac{d}{5}$$

$$= \frac{10 \times 10^{-4}\,\text{m}}{5}$$

$$= 2 \times 10^{-4}$$

57. An object of mass 0.2 kg executes simple harmonic motion along x axis with frequency of $\left(\frac{25}{\pi}\right)$ Hz. At the position $x = 0.04$ m the object has kinetic energy 0.5 J and potential energy 0.4 J. The amplitude of oscillation is …………. cm.

Ans. (6)

Sol. Total energy = K.E. + P.E.

at $x = 0.04$ m, T.E. $= 0.5 + 0.4 = 0.9$ J
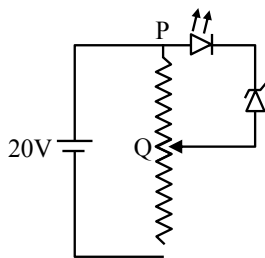
T.E $= 1\,m\omega^2 A^2 = 0.9$

$$= \frac{1}{2} \times 0.2 \left(2\pi \times \frac{25}{\pi}\right)^2 \times A^2 = 0.9$$

$\Rightarrow A = 0.06$ m
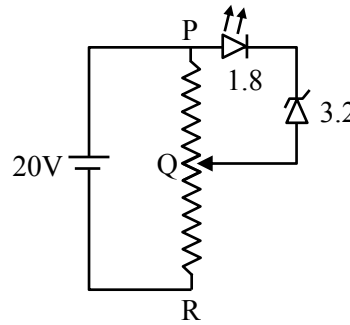
$A = 6$ cm

58. A potential divider circuit is connected with a dc source of 20 V, a light emitting diode of glow in voltage 1.8 V and a zener diode of breakdown voltage of 3.2 V. The length (PR) of the resistive wire is 20 cm. The minimum length of PQ to just glow the LED is …………. cm.

Ans. (5)

Sol.

PR = 20 cm

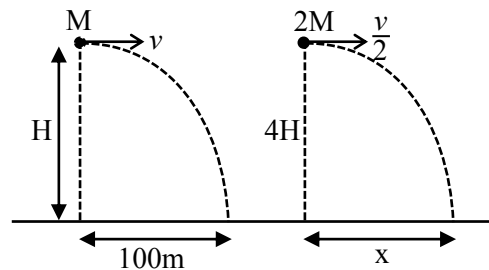$$V_{PQ} = \frac{1}{4} \times R_{PR}$$

$$\ell_{min}\,(PQ) = \frac{1}{4} \times 20$$

$$= 5 \text{ cm}$$

59. A body of mass M thrown horizontally with velocity v from the top of the tower of height H touches the ground at a distance of 100m from the foot of the tower. A body of mass 2M thrown at a velocity $\frac{v}{2}$ from the top of the tower of height 4H will touch the ground at a distance of ……….m.

Ans. (100)

Sol.

$$100 = v\sqrt{\frac{2H}{g}}; \quad x = \frac{v}{2}\sqrt{\frac{2(4H)}{g}} = v\sqrt{\frac{2H}{g}}$$

$\Rightarrow x = 100$

60. A circular table is rotating with an angular velocity of ω rad/s about its axis (see figure). There is a smooth groove along a radial direction on the table. A steel ball is gently placed at a distance of 1m on the groove. All the surface are smooth. If the radius of the table is 3 m, the radial velocity of the ball w.r.t. the table at the time ball leaves the table is $x\sqrt{2}\omega$ m/s, where the value of x is………..
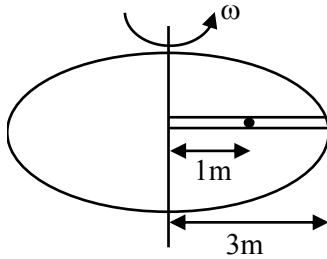
Ans. (2)

Sol. $a_c = \omega^2 x$

$$\frac{v\,dv}{dx} = \omega^2 x$$

$$\int_0^V v\,dv = \int_1^3 \omega^2 x\,dx$$

$$\frac{v^2}{2} = \omega^2 \left[\frac{x^2}{2}\right]$$

$$\quad 2 \quad 2 \qquad \left. 1^2 \right]$$

$v = 2\sqrt{2}\omega$

$x = 2$