<u>...</u> <u>Colleg</u>eDekho

> FINAL JEE-MAIN EXAMINATION - SEPTEMBER, 2020 (Held On Friday 04th SEPTEMBER, 2020) TIME : 3 PM to 6 PM TEST PAPER WITH SOLUTION MATHEMATICS **DIFFERENTIABILITY-XII** R.H.L. = $\frac{\pi}{4} + \frac{\pi}{4} = \frac{\pi}{2}$ The function f(x) = $\begin{cases} \frac{\pi}{4} + \tan^{-1} x, |x| \le 1\\ \frac{1}{2}(|x|-1), |x| > 1 \end{cases}$ is : so, not continuous at x = 1For differentiability at x = -11. L.H.D. = $\frac{1}{1+1} = \frac{1}{2}$ R.H.D. = $-\frac{1}{2}$ (1) continuous on $R-\{1\}$ and differentiable on $R - \{-1, 1\}.$ so, non differentiable at x = -1(2) both continuous and differentiable on **SET-XI** $R - \{-1\}.$ 2. Let $\bigcup_{i=1}^{50} X_i = \bigcup_{i=1}^{n} Y_i = T$, where each X_i contains (3) continuous on $R - \{-1\}$ and differentiable on $R - \{-1, 1\}.$ (4) both continuous and differentiable on 10 elements and each Y_i contains 5 elements. If each $R - \{1\}$ element of the set T is an element of exactly 20 of sets X_i 's and exactly 6 of sets Y_i 's, then n is equal to : फलन f(x) = $\begin{cases} \frac{\pi}{4} + \tan^{-1} x, |x| \le 1\\ \frac{1}{2}(|x|-1), |x| > 1 \end{cases}$ (1) 45(2) 15(3) 50 (4) 301. माना $\bigcup_{i=1}^{50} X_i = \bigcup_{i=1}^n Y_i = T$ है, जहाँ प्रत्येक X_i में 10 अवयव 2. (1) R-{1} में संतत तथा R - {-1, 1} में अवकलनीय है। हैं तथा प्रत्येक \mathbf{Y}_{i} में 5 अवयव में है। यदि T का प्रत्येक अवयव (2) R - {-1} में संतत और अवकलनीय, दोनों, है। ठीक 20, X, समुच्चयों का एक अवयव है तथा ठीक 6, Y, (3) R - {-1} में संतत तथा R - {-1, 1} में अवकलनीय है। समुच्चयों का एक अवयव है, तो n का मान है : (4) R -{1}में संतत और अवलकनीय, दोनों, है। (1) 45(2) 15Official Ans. by NTA (1) (3) 50(4) 30Official Ans. by NTA (4) Sol. $f(x) = \begin{cases} \frac{\pi}{4} + \tan^{-1} x & , & x \in (-\infty, -1] \cup [1, \infty) \\ -\frac{(x+1)}{2} & , & x \in (-1, 0] \end{cases}$ **Sol.** $n(X_i) = 10$. $\bigcup_{i=1}^{50} X_i = T, \Rightarrow n (T) = 500$ each element of T belongs to exactly 20 elements of $X_i \Rightarrow \frac{500}{20} = 25$ distinct elements so $\frac{5n}{6} = 25$ $\frac{x-1}{2} , \qquad x \in (0,1)$ \Rightarrow n = 30 **Q.E.-XI** for continuity at x = -13. Let $\lambda \neq 0$ be in R. If α and β are the roots of the equation, L.H.L. = $\frac{\pi}{4} - \frac{\pi}{4} = 0$ $x^2 - x + 2\lambda = 0$ and α and γ are the roots of the equation, $3x^2-10x+27\lambda = 0$, then $\frac{\beta\gamma}{\lambda}$ is equal to : R.H.L. = 0so, continuous at x = -1for continuity at x = 1

CollegeDekho

 $\lambda \neq 0, R$ 4. 3. $x^2 - x + 2\lambda = 0$ के मूल हैं और α तथा γ , समीकरण $\frac{dy}{dx} - \frac{y + 3x}{\log_2(y + 3x)} + 3 = 0$ का हल है: $3x^2-10x+27\lambda = 0$ के मूल हैं, तो $\frac{\beta\gamma}{\lambda}$ बराबर है : (जहाँ C एक समाकलन अचर है।) (1) 36(2) 27(1) $x - 2 \log_{e}(y + 3x) = C$ (3)9(4) 18(2) $x-\log_e(y+3x)=C$ Official Ans. by NTA (4) **Sol.** $\alpha + \beta = 1$, $\alpha\beta = 2\lambda$ (3) $x - \frac{1}{2} (\log_e(y+3x))^2 = C$ $\alpha + \beta = \frac{10}{3}, \qquad \alpha \gamma = \frac{27\lambda}{3} = 9\lambda$ (4) $y + 3x - \frac{1}{2} (\log_e x)^2 = C$ $\gamma - \beta = \frac{7}{3},$ Official Ans. by NTA (3) **Sol.** ln(y + 3x) = z (let) $\frac{\gamma}{\beta} = \frac{9}{2} \Rightarrow \gamma = \frac{9}{2}\beta = \frac{9}{2} \times \frac{2}{3} \Rightarrow \gamma = 3$ $\frac{1}{v+3x} \cdot \left(\frac{dy}{dx} + 3\right) = \frac{dz}{dx}$ $\frac{9}{2}\beta - \beta = \frac{7}{3}$ $\frac{dy}{dx} + 3 = \frac{y + 3x}{\ell n(y + 3x)}$ (given) $\frac{9}{2}\beta = \frac{7}{3} \Longrightarrow \beta = \frac{2}{3}$ $\frac{dz}{dx} = \frac{1}{z}$ $\alpha = 1 - \frac{2}{3} = \frac{1}{3}$ \Rightarrow z dz = dx $\Rightarrow \frac{z^2}{2} = x + C$ $2\lambda = \frac{2}{9} \Longrightarrow \lambda = \frac{1}{9}$ $\Rightarrow \frac{1}{2}\ell n^2(y+3x) = x+C$ $\frac{\beta\gamma}{\lambda} = \frac{\frac{2}{3} \times 3}{1} = 18$ $\Rightarrow x - \frac{1}{2} (\ell n(y + 3 x))^2 = C$ S.S.-XI D.E.-XII 5. Let $a_1, a_2..., a_n$ be a given A.P. whose common The solution of the differential equation 4. difference is an integer and $S_n = a_1 + a_2 + ..+ a_n$. $\frac{dy}{dx} - \frac{y+3x}{\log_2(y+3x)} + 3 = 0$ is :-If $a_1 = 1$, $a_n = 300$ and $15 \le n \le 50$, then the ordered pair ($S_{n-4}a_{n-4}$

(1)(2480, 249)(where C is a constant of integration.) (3) (2490, 248 5. माना a1, a2,..., (3) $x - \frac{1}{2} (\log_e(y+3x))^2 = C$

(1

a) is equal to :
(2) (2490, 249)
(3) (4) (2480, 248)
(4)
$$(2480, 248)$$

(4) $(2480, 248)$
(5) a_n एक दी गई समांतर श्रेढ़ी है, जिसका
 $S_n = a_1 + a_2 + \dots + a_n$
= 300 $15 \le n \le 50$,

an

..(1)

$$a_{1} = 1, a_{n} = 300 \qquad 15 \le n \le 50,$$

(S_{n-4}, a_{n-4}) :
) (2480, 249) (2) (2490, 249)

1

(1) $x-2 \log_{e}(y+3x)=C$

(2) $x-\log_e(y+3x)=C$



	Official Ans. by NTA (3)	LIMIT-				
Sol.	$\mathbf{a_n} = \mathbf{a_1} + (\mathbf{n} - 1)\mathbf{d}$	7.	Le			
	$\Rightarrow 300 = 1 + (n - 1) d$		su			
	$\Rightarrow (n-1)d = 299 = 13 \times 23$		~			
	since, $n \in [15, 50]$		li			
	\therefore n = 24 and d = 13					
	$a_{n-4} = a_{20} = 1 + 19 \times 15 = 248$ $a_{n-4} = -248$		11			
	$\rightarrow a_{n-4} - 2 + 0$		(1			
	$S_{-4} = \frac{20}{1+248} = 2490$					
	$S_{n-4} = 2$					
3D-X	D-XII					
6.	The distance of the point $(1, -2, 3)$ from the plane		14			
	x-y+z = 5 measured parallel to the line					
	$\frac{x}{2} = \frac{y}{2} = \frac{z}{6}$ is:		मा			
	2 3 -0		(1			
	(1) 7 (2) 1 (3) $\frac{1}{7}$ (4) $\frac{7}{5}$		(1			
6			0			
0.	x = y = z, $y = y = x$, $y = z$, $y = y = z$, $y = z$,					
	$\frac{\Lambda}{2} = \frac{y}{3} = \frac{z}{6}$ के समांतर मापी गई दूरी है :	Sol.	L			
	1 7		us			
	(1) 7 (2) 1 (3) $\frac{1}{7}$ (4) $\frac{7}{5}$					
	Official Ans. by NTA (2)		L			
	x y z		_			
Sol.	equation of line parallel to $\frac{1}{2} = \frac{1}{3} = \frac{1}{-6}$ passes		_			
	through $(1, -2, 3)$ is		\Rightarrow			
	x - 1 $y + 2$ $z - 3$					
	$\frac{1}{2} = \frac{1}{3} = \frac{1}{-6} = r$		⇒			
	$\mathbf{x} = 2\mathbf{r} + 1$					
	y = 3r - 2,		\Rightarrow			
	z = -6r + 3	DET				
	So $2r + 1 - 3r + 2 - 6r + 3 = 5$	DEI	EK 1C			
	\Rightarrow $-7r + 1 = 0$	ð.				
	$r = \frac{1}{2}$		х Эл			
	- 7		∠∧ 2 v			
	$x = \frac{9}{2}, y = \frac{-11}{2}, z = \frac{15}{2}$		ha			
	7 7 7 7		(1			
	Distance is = $(9 + 1)^2 + (2 + 11)^2 + (2 + 15)^2$		(1			
	Distance is $=\sqrt{\left(\frac{7}{7}-1\right)}+\left(\frac{2}{7}-\frac{7}{7}\right)+\left(\frac{3}{7}-\frac{7}{7}\right)$	8	्ड राहि			
	$(2)^2 (2)^2 (c)^2$	0.	91 V			
	$=\sqrt{\left(\frac{2}{7}\right)}+\left(\frac{3}{7}\right)+\left(\frac{6}{7}\right)$		х Эл			
			∠∧ 2 v			
	$=\frac{1}{-}\sqrt{4+9+36}$		38			
	7					
	$\sqrt{-}$					

-XII

7.	• Let $f: (0, \infty) \to (0, \infty)$ be a differentia such that $f(1) = c$ and						
	$\lim_{t \to x} \frac{t^2 f^2(x) - x}{t - x}$	$\frac{f^2 f^2(t)}{t} = 0$	I				
	If $f(x) = 1$, then x is equal to :						
	(1) 2e (2	2) $\frac{1}{2e}$	(3) e	(4) $\frac{1}{e}$			
7.	माना f : (0, ∞) - कि f(1) = e तथ	→ (0, ∞) ע ח	रक ऐसा अवव	कलनीय फलन है			
	$\lim_{t \to x} \frac{t^2 f^2(x) - x}{t - x}$ मान है	$\frac{f^2f^2(t)}{t} = 0$) हैं। यदि f(x)	= 1, है, तो x क			
	(1) 2e (2	$\frac{1}{2}$	(3) e	$(4) \frac{1}{-}$			
	Official Ans.	bv NTA	(4)	e			
	$t^2 f^2$	$x) - x^2 f^2$	(-) t)				
Sol.	$L = \lim_{t \to x} \frac{1}{t \to x}$	t – x	<u>··</u>				
	using L.H. rule	e					
	$L = \lim_{t \to x} \frac{2tf^{2}(x) - x^{2} \cdot 2f'(t) \cdot f(t)}{1}$						
	$\Rightarrow L = 2xf(x) (f(x) - x f'(x)) = 0 (given)$						
	$\Rightarrow f(x) = xf'(x) \Rightarrow \int \frac{f'(x)dx}{f(x)} = \int \frac{dx}{x}$						
	$\Rightarrow \ln \mathbf{f}(\mathbf{x}) = \ln \mathbf{x} + C$						
	$\therefore f(1) = e, x > 0$	> 0, f(x)	> 0				
	\Rightarrow f(x) = ex,	if f(x)	$=1 \Rightarrow x =$	$=\frac{1}{e}$			
DET	ERMINANT-X	XI					
8.	8. If the system of equations						
	x + y + z = 2	6					
	$2x + 4y - 2 =$ $3x + 2y + \lambda z =$	0 = 11					
	has infinitely many solutions, then :						
	(1) $\lambda - 2\mu = -$	-5	(2) 2λ –	μ = 5			
	$(3) 2\lambda + \mu = 1$	4	(4) $\lambda + 2$	$\mu = 14$			
8.	यदि समीकरणों व	र्नकाय					
	x + y + z = 2	6					
	2x + 4y - 2 = $3x + 2y + \lambda z =$	0 = 11					
		۳ :					



Official Ans. by NTA (3) Sol. For infinite solutions $\Delta = \Delta_{\rm x} = \Delta_{\rm y} = \Delta_{\rm z} = 0$ Now $\Delta = 0 \Rightarrow \begin{vmatrix} 1 & 1 & 1 \\ 2 & 4 & -1 \\ 3 & 2 & \lambda \end{vmatrix} = 0$ $\Rightarrow \lambda = \frac{9}{2}$ $\Delta_{x=0} \implies \begin{vmatrix} 2 & 1 & 1 \\ 6 & 4 & -1 \\ \mu & 2 & -\frac{9}{2} \end{vmatrix} = 0$ $\Rightarrow \mu = 5$ For $\lambda = \frac{9}{2}$ & $\mu = 5$, $\Delta_y = \Delta_z = 0$ Now check option $2\lambda + \mu = 14$ S.S.-XII 9. The minimum value of $2^{sinx} + 2^{cosx}$ is :-(1) $2^{1-\frac{1}{\sqrt{2}}}$ (2) $2^{-1+\sqrt{2}}$ $(4) \ 2^{-1+\frac{1}{\sqrt{2}}}$ (3) $2^{1-\sqrt{2}}$ 9. 2^{sinx} + 2^{cosx} का न्यूनतम मान है : (1) $2^{1-\frac{1}{\sqrt{2}}}$ (2) $2^{-1+\sqrt{2}}$ (4) $2^{-1+\frac{1}{\sqrt{2}}}$ (3) $2^{1-\sqrt{2}}$ Official Ans. by NTA (1) **Sol.** Usnign $AM \ge GM$ $\Rightarrow \frac{2^{\sin x} + 2^{\cos x}}{2} \ge \sqrt{2^{\sin x} \cdot 2^{\cos x}}$ $\Longrightarrow 2^{\sin x} + 2^{\cos x} \ge 2^{1 + \left(\frac{\sin x + \cos x}{2}\right)}$ $\Rightarrow \min(2^{\sin x} + 2^{\cos x}) = 2^{1 - \frac{1}{\sqrt{2}}}$ D.I.-XII **10.** $\int_{\pi/2}^{\pi/3} \tan^3 x \cdot \sin^2 3x (2 \sec^2 x \cdot \sin^2 3x + 3 \tan x \cdot \sin 6x) dx$ is equal to :

9

1

1

7

$$\int_{\frac{\pi}{6}}^{\frac{\pi}{6}} \tan^{3} x \cdot \sin^{2} 3x(2 \sec^{2} x \cdot \sin^{2} 3x + 3 \tan x \cdot \sin 6x) dx$$
For HIF $\frac{\pi}{6}$:
(1) $\frac{9}{2}$ (2) $-\frac{1}{9}$ (3) $-\frac{1}{18}$ (4) $\frac{7}{18}$
Official Ans. by NTA (3)
Sol. I = $\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} d((\sin 3x)^{4} (\tan x)^{4})$
 $\Rightarrow I = \frac{1}{2} \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} d((\sin 3x)^{4} (\tan x)^{4})$
 $\Rightarrow I = ((\sin 3x)^{4} (\tan x)^{4})_{\frac{\pi}{6}}^{\frac{\pi}{3}}$
 $\Rightarrow I = -\frac{1}{18}$
CIRCLE-XI
11. The circle passing through the intersection of the circles, $x^{2} + y^{2} - 6x = 0$ and $x^{2} + y^{2} - 4y = 0$, having its centre on the line, $2x - 3y + 12 = 0$, also passes through the point :
(1) (1, -3) (2) (-1, 3)
(3) (-3, 1) (4) (-3, 6)
11. $q \pi \tilde{1} x^{2} + y^{2} - 6x = 0 \pi q x^{2} + y^{2} - 4y = 0, \tilde{\pi} q \pi \bar{\pi} \bar{x}^{2} + \bar{y}^{2} - 6x = 0 \pi q x^{2} + y^{2} - 4y = 0, \tilde{\pi} q \pi \bar{q} \bar{\pi} \bar{x}^{2} + y^{2} - 6x = 0 \pi q x^{2} + y^{2} - 4y = 0, \tilde{\pi} q \pi \bar{q} \bar{\pi} \bar{x}^{2} + y^{2} - 6x = 0 \pi q x^{2} + y^{2} - 4y = 0, \tilde{\pi} q \pi \bar{q} \bar{\pi} \bar{x}^{2} + y^{2} - 6x = 0 \pi q x^{2} + y^{2} - 4y = 0, \tilde{\pi} q \pi \bar{q} \bar{\pi} \bar{x}^{2} + y^{2} - 6x = 0 \pi q x^{2} + y^{2} - 4y = 0, \tilde{\pi} q \pi \bar{q} \bar{\pi} \bar{x}^{2} + y^{2} - 6x = 0 \pi q x^{2} + y^{2} - 4y = 0, \tilde{\pi} q \pi \bar{q} \bar{\pi} \bar{x}^{2} + y^{2} - 6x = 0 \pi q x^{2} + y^{2} - 4y = 0, \tilde{\pi} q \pi \bar{q} \bar{\pi} \bar{q} \bar{\pi} \bar{x}^{2} + 12 = 0 q q R \bar{q} \pi \bar{q} \bar{\pi} \bar{x}^{2} + 12 = 0 q q R \bar{q} \pi \bar{q} \bar{\pi} \bar{x}^{2} + 12 = 0 q q R \bar{q} \pi \bar{q} \bar{\pi} \bar{x}^{2} + 12 = 0 q q R \bar{q} \pi \bar{q} \bar{\pi} \bar{x}^{2} + 12 = 0 q \bar{q} \bar{x}^{2} + 12 = 0 q \bar{x}^{2} + 12 = 0 q \bar{q} \bar{x}^{2} + 12 = 0 q \bar{x}^{2$

10.

$$\Rightarrow S : (x^2 + y^2 - 6x) + \lambda (x^2 + y^2 - 4y) = 0$$
$$\Rightarrow S : x^2 + y^2 - \left(\frac{6}{1+\lambda}\right)x - \left(\frac{4\lambda}{1+\lambda}\right) y = 0 \dots (1)$$

Centre
$$\left(\frac{3}{1+\lambda}, \frac{2\lambda}{1+\lambda}\right)$$
 lies on

 $2x - 3y + 12 = 0 \Rightarrow \lambda = -3$ put in (1) \Rightarrow S : $x^2 + y^2 + 3x - 6y = 0$ Now check options point (-3, 6)





 $= a + b\omega$ $16 + 32 \omega + 24 \omega^2 + 8 + \omega = a + b\omega$ $24 + 24 \omega^2 + 33\omega = a + b\omega$ $\Rightarrow -24\omega + 33\omega = a + b\omega$ In a game two players A and B take turns in throwing a pair of fair dice starting with player A and total of scores on the two dice,

 $(\omega^3 = 1)$

in each throw is noted. A wins the game if he throws a total of 6 before B throws a total of 7 and B wins the game if he throws a total of 7 before A throws a total of six The game stops as soon as either of the players wins. The probability of A winning the game is :

(1)
$$\frac{31}{61}$$
 (2) $\frac{5}{6}$ (3) $\frac{5}{31}$ (4) $\frac{30}{61}$

एक खेल में दो खिलाड़ी A तथा B बारी बारी से अनभिनत पासों के युग्म को फेंकते हैं, जबकि खिलाडी A खेल आरम्भ करता है, तथा प्रत्येक बार दोनों पासों पर आए अंकों का योग नोट किया जाता है यदि B द्वारा फेंके गए पासों के अंको का योग 7 आने से पहले A द्वारा फेंके एक पासों के अंकों का योग 6 आ जाता है, तो A जीतता है जबकि A द्वारा फेंके गए पासों के अंकों का योग 6 आने से पहले. B द्वारा फेंके गए पासों के अंकों का योग 7 आ जाता है, तो B जीतता है। किसी भी एक खिलाडी का जीतने पर खेल समाप्त हो जाता है। A के खेल को जीतने की प्रायिक्रता है :

$$\frac{31}{61} \qquad (2) \ \frac{5}{6} \qquad (3) \ \frac{5}{31} \qquad (4) \ \frac{30}{61}$$

Official Ans. by NTA (4)

Sol.
$$P(6) = \frac{5}{36}$$
, $P(7) = \frac{1}{6}$
 $P(A) = W + FFW + FFFFW +$
 $= \frac{5}{36} + \left(\frac{31}{36} \times \frac{5}{6}\right) \times \frac{5}{36} + \left(\frac{31}{36} \times \frac{5}{6}\right)^2 \times \frac{5}{36} + ...$
 $= \frac{\frac{5}{36}}{155} = \frac{5}{36} \times \frac{216}{61} = \frac{30}{61}$

ELLIPSE-XI Let x = 4 be a directrix to an ellipse whose centre 15. is at the origin and its eccentricity is $\frac{1}{2}$. If P (1, β), $\beta > 0$ is a point on this ellipse, then the equation of the normal to it at P is :-(1) 7x - 4y = 1(2) 4x - 2y = 1(4) 8x - 2y = 5(3) 4x - 3y = 2माना x = 4 एक ऐसे दीर्घवृत की एक नियता है, जिसका केन्द्र 15. मूल बिंदु पर है तथा जिसकी उत्केन्द्रता $\frac{1}{2}$ है, यदि P (1, β), β > 0 इस दीर्घवृत्त पर स्थित एक बिंदु है, तो इसके P पर खींचे गए अभिलंब का समीकरण है : (1) 7x - 4y = 1(2) 4x - 2y = 1(4) 8x - 2y = 5(3) 4x - 3y = 2Official Ans. by NTA (2) **Sol.** Ellipse : $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ directrix : $x = \frac{a}{e} = 4$ & $e = \frac{1}{2}$ \Rightarrow a = 2 & b² = a² (1-e²) = 3 \Rightarrow Ellipse is $\frac{x^2}{4} + \frac{y^2}{3} = 1$ P is $\left(1,\frac{3}{2}\right)$ Normal is : $\frac{4x}{1} - \frac{3y}{3/2} = 4 - 3$ $\Rightarrow 4x - 2y = 1$ MATHEMATICAL REASONING-XII 16. Contrapositive of the statement:

'If a function f is differentiable at a, then it is also continuous at a', is :-

- (1) If a function f is continuous at a, then it is not differentiable at a.
- (2) If a function f is not continuous at a, then it is differentiable at a.
- (3) If a function f is not continuous at a, then it is not differentiable at a.
- (4) If a function f is continuous at a, then it is

'यदि एक फलन f, a पर अवकलनीय है तो संतत भी है' यह а पर कथन है प्रतिधनात्मक का :-(1) यदि एक फलन f, a पर संतत है तो यह a पर अवकलनीय नहीं है। (2) यदि एक फलन f, a पर संतत नहीं है तो यह a पर अवकलनीय है। (3) यदि एक फलन f, a पर संतत नहीं है तो यह a पर अवकलनीय नहीं है । (4) यदि एक फलन f, a पर संतत है तो यह a पर अवकलनीय है। Official Ans. by NTA (3) p = function is differentiable at a

Sol. p = function is differentiable at a q = function is continuous at a contrapositive of statement $p \rightarrow q$ is $\sim q \rightarrow \sim p$

PARABOLA-XI

17. The area (in sq. units) of the largest rectangle ABCD whose vertices A and B lie on the x-axis and vertices C and D lie on the parabola, $y=x^2-1$ below the x-axis, is :

(1)
$$\frac{4}{3\sqrt{3}}$$
 (2) $\frac{1}{3\sqrt{3}}$ (3) $\frac{4}{3}$ (4) $\frac{2}{3\sqrt{3}}$

17. उस सबसे बड़ी आयत ABCD, जिसकें शीर्ष बिंदु A तथा B, x-अक्ष पर स्थित हैंतथा शीर्ष बिंदु C तथा D, x-अक्ष के नीचे, परवलय y = x² -1 पर स्थित हैं, का क्षेत्रफल (वर्ग इकाइयों में) है :

(1)
$$\frac{4}{3\sqrt{3}}$$
 (2) $\frac{1}{3\sqrt{3}}$ (3) $\frac{4}{3}$ (4) $\frac{2}{3\sqrt{3}}$

Official Ans. by NTA (1)

Sol. Area (A) =
$$2t \cdot (1 - t^2)$$

$$(0 < t < 1)$$

$$A = 2t - 2t^{3}$$

$$\frac{dA}{dt} = 2 - 6t^{2}$$

$$t = \frac{1}{\sqrt{3}}$$

$$(-t, t^{2} - 1)$$

$$(t, 0)$$

$$(-t, t^{2} - 1)$$

$$(-t, t^{2} - 1)$$

$$(-t, t^{2} - 1)$$

$$(-t, t^{2} - 1)$$

16.



OMIAL THEOREM-XII 18. If for some positive integer n, the coefficients of three consecutive terms in the binomial expansion $(1+x)^{n+5}$ are in the of ratio 5:10:14, then the largest coefficient in this expansion is :-(1)792(2) 252 (3) 462 (4) 330 माना किसी धनपूर्णाक n के लिए, (1+x)ⁿ⁺⁵ के द्विपद प्रसार 18. में तीन क्रमागत पदों के गुणांक 5 : 10 : 14 के अनुपात में हैं, 20. तो इस प्रसार में सब से बड़ा गुणांक है :-(2) 252(4) 330 (1)792(3) 462Official Ans. by NTA (3) **Sol.** Let n + 5 = N $N_{C_{r-1}}: N_{C_r}: N_{C_{r-1}} = 5:10:14$ $\Rightarrow \frac{N_{C_r}}{N_C} = \frac{N+1-r}{r} = 2$

19. If the perpendicular bisector of the line segment joining the points P (1, 4) and Q (k, 3) has y-intercept equal to -4, then a value of k is :-

 $\frac{N_{C_{r+1}}}{N_{C}} = \frac{N-r}{r+1} = \frac{7}{5}$

Largest coefficient = ${}^{11}C_6 = 462$

 \Rightarrow r = 4, N = 11

 $\Rightarrow (1 + x)^{11}$

STRAIGHT LINE-XI

(2) -2 (3) $\sqrt{14}$ (1) $\sqrt{15}$ (4) -4

19. यदि बिंदुओं P (1, 4) तथा Q (k, 3) को मिलाने वाले रेखाखण्ड के लंबसमद्विभाजक का y-अंत: खण्ड –4, है, तो k का एक मान है :-

> (1) $\sqrt{15}$ (2) - 2 $(3) \sqrt{14}$ (4) - 4

Official Ans. by NTA (4)



Equation of
$$\perp^{r}$$
 bisector is

$$y + 4 = (k - 1) (x - 0)$$

$$\Rightarrow y + 4 = x(k - 1)$$

$$\Rightarrow \frac{7}{2} + 4 = \frac{k + 1}{2} (k - 1)$$

$$\Rightarrow \frac{15}{2} = \frac{k^2 - 1}{2} \Rightarrow k^2 = 16 \Rightarrow k = 4, -4$$

MATRIX-XII

Suppose the vectors x_1, x_2 and x_3 are the solutions of the system of linear equations, Ax = b when the vector b on the right side is equal to b_1 , b_2 and b_3 respectively. If

$$\mathbf{x} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}, \mathbf{x}_2 = \begin{bmatrix} 0 \\ 2 \\ 1 \end{bmatrix}, \mathbf{x}_3 = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}, \mathbf{b}_1 = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

 $\mathbf{b}_2 = \begin{bmatrix} 0\\2\\0 \end{bmatrix}$ and $\mathbf{b}_3 = \begin{bmatrix} 0\\0\\2 \end{bmatrix}$, then the determinant of

A is equal to :-

(1)
$$\frac{1}{2}$$
 (2) 4 (3) $\frac{3}{2}$ (4) 2

माना सदिश x_1, x_2 तथा $x_3,$ रैखिक समीकरण निकाय 20. Ax = b के हल हैं, जबकि दांई ओर का सदिश b, क्रमश: b_1, b_2 तथा b_3 के बराबर है। यदि





Sol.

Official Ans. by NTA (4)

$$Ax_{1} = b_{1}$$

$$Ax_{2} = b_{2}$$

$$Ax_{3} = b_{3}$$

$$\Rightarrow |A| \begin{vmatrix} 1 & 0 & 0 \\ 1 & 2 & 0 \\ 1 & 1 & 1 \end{vmatrix} = \begin{vmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 2 \end{vmatrix}$$

$$\Rightarrow |A| = \frac{4}{2} = 2$$

P & C-XI

- 21. A test consists of 6 multiple choice questions, each having 4 alternative answers of which only one is correct. The number of ways, in which a candidate answers all six questions such that exactly four of the answers are correct, is _____
- 21. एक परीक्षा में 6 बहुविकल्पी प्रश्न हैं तथा प्रत्येक प्रश्न के उत्तर के लिए 4 विकल्प हैं जिसमें से केवल एक सही है। एक परीक्षार्थी द्वारा सभी 6 प्रश्नों के उत्तर इस प्रकार देने, ताकि उसके ठीक 4 प्रश्नों के उत्तर सही हों, के तरीकों की संख्या है ____

Official Ans. by NTA (135)

Sol. Ways = ${}^{6}C_{4} \cdot 1^{4} \cdot 3^{2}$ = 15 × 9 = 135

CIRCLE-XI

- 22. Let PQ be a diameter of the circle $x^2+y^2=9$. If α and β are the lengths of the perpendiculars from P and Q on the straight line, x + y = 2 respectively, then the maximum value of $\alpha\beta$ is _____
- 22. माना PQ वृत्त $x^2+y^2=9$ का एक व्यास है। यदि P तथा Q से रेखा x + y = 2 पर खींचे गए लंबों की लंबाइयाँ क्रमश: α तथा β हैं, तो $\alpha\beta$ का अधिकतम मान है _____| Official Ans. by NTA (7)



Let P $(3\cos\theta, 3\sin\theta)$ Q $(-3\cos\theta, -3\sin\theta)$

$$\Rightarrow \alpha\beta = \frac{\left|(3\cos\theta + 3\sin\theta)^2 - 4\right|}{2}$$

$$5+9\sin 2\theta$$

D.I.-XII

23. Let $\{x\}$ and [x] denote the fractional part of x and the greatest integer $\leq x$ respectively of a real

number x. If $\int_0^n \{x\} dx$, $\int_0^n [x] dx$ and $10(n^2 - n)$, $(n \in N, n > 1)$ are three consecutive terms of a G.P., then n is equal to_____

 माना {x} तथा [x], क्रमश: एक वास्तविक संख्या x के भिन्नात्मक भाग तथा महत्तम पूर्णाक ≤ x, को दर्शाते हैं। यदि

$$\begin{split} &\int_{0}^{n} \{x\} dx, \int_{0}^{n} [x] dx \; \pi \mbox{all n} 10(n^{2} - n), \; (n \in N, \; n > 1) \\ & \mbox{एक गुणोत्तर श्रेढी के तीन क्रमागत पद हैं, तो n का मान है} \\ & \mbox{Official Ans. by NTA (21)} \end{split}$$

Sol.
$$\int_{0}^{n} \{x\} dx = n \int_{0}^{1} \{x\} dx = n \int_{0}^{1} x \ dx = \frac{n}{2}$$
$$\int_{0}^{n} [x] dx = \int_{0}^{n} (x - \{x\}) dx = \frac{n^{2}}{2} - \frac{n}{2}$$
$$\Rightarrow \left(\frac{n^{2} - n}{2}\right)^{2} = \frac{n}{2} \cdot 10 \cdot n(n - 1) \text{ (where } n > 1)$$
$$\Rightarrow \frac{n - 1}{4} = 5 \Rightarrow n = 21$$

VECTOR-XII

- 24. If $\vec{a} = 2\hat{i} + \hat{j} + 2\hat{k}$, then the value of $\left|\hat{i} \times (\vec{a} \times \hat{i})\right|^2 + \left|\hat{j} \times (\vec{a} \times \hat{j})\right|^2 + \left|\hat{k} \times (\vec{a} \times \hat{k})\right|^2$ is equal to
- **24.** $\overline{a} = 2\hat{i} + \hat{j} + 2\hat{k}$, \hat{e} , \hat{n}
 - $|\hat{i} \times (\vec{a} \times \hat{i})|^2 + |\hat{j} \times (\vec{a} \times \hat{j})|^2 + |\hat{k} \times (\vec{a} \times \hat{k})|^2$ का मान है _____| Official Ans. by NTA (18)

Sol.
$$\Sigma |\vec{a} - (\vec{a} \cdot i)i|^2$$

 $\Rightarrow \Sigma (|a|^2 + (\vec{a} \cdot i)^2 - 2(\vec{a} \cdot i)^2$
 $\Rightarrow 3|\vec{a}|^2 - \Sigma (\vec{a} \cdot i)^2$
 $\Rightarrow 2|\vec{a}|^2$

,****™** CollegeDekho

STATISTICS-XII 25. If the variance of the following frequency distribution: Class : 10–20 20-30 30-40 Frequency : 2 2 х is 50, then x is equal to _____ यदि निम्न बारंबारता बंटन : 25. वर्ग : 10–20 20-30 30-40 बारंबारता : 2 2 х का प्रसरण 50 है, तो x का मान है ____| Official Ans. by NTA (4) **Sol.** : Variance is independent of shifting of origin $\Rightarrow \quad x_i: 15 \qquad 25 \quad 35 \quad \text{or} \ -10 \quad 0$ 10 x 2 2 x 2 f_i : 2 Variance $(\sigma^2) = \frac{\Sigma x_i^2 f_i}{\Sigma f_i} - (\vec{x})^2$ \Rightarrow $50 = \frac{200 + 0 + 200}{x + 4} - 0 \qquad \{\overline{x} = 0\}$ \Rightarrow 200 + 50x = 200 + 200 \Rightarrow x = 4 \Rightarrow