

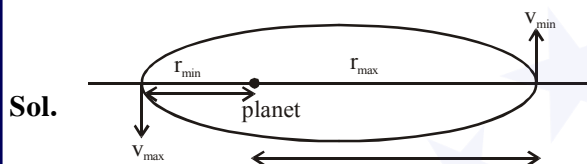
PHYSICS

TEST PAPER WITH ANSWER & SOLUTION

1. A satellite is in an elliptical orbit around a planet P. It is observed that the velocity of the satellite when it is farthest from the planet is 6 times less than that when it is closest to the planet. The ratio of distances between the satellite and the planet at closest and farthest points is :

- (1) 1 : 6 (2) 3 : 4
 (3) 1 : 3 (4) 1 : 2

Official Ans. by NTA (1)



By angular momentum conservation

$$r_{\min} v_{\max} = r_{\max} v_{\min} \quad \dots (i)$$

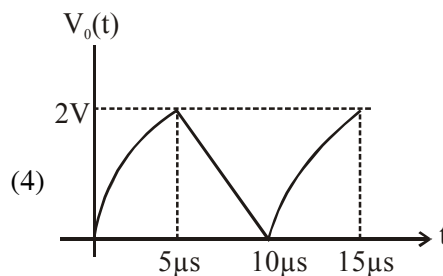
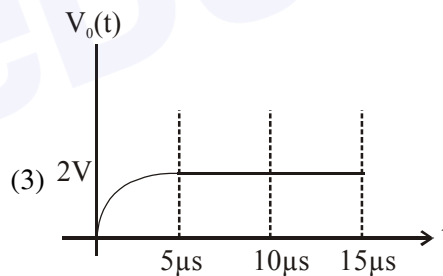
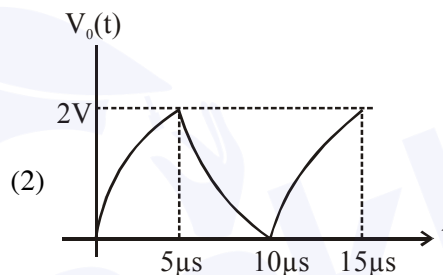
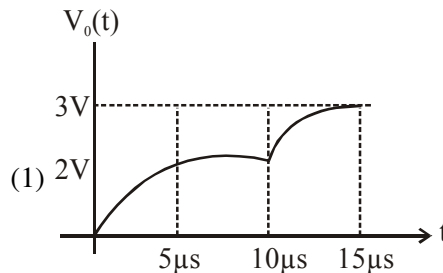
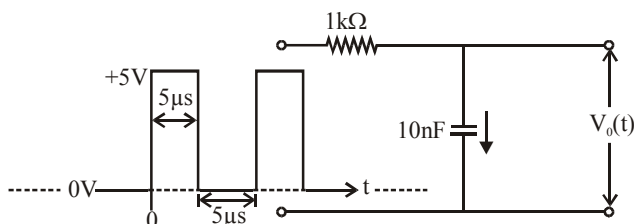
Given $v_{\min} = \frac{v_{\max}}{6}$

from equation (i)

$$\frac{r_{\min}}{r_{\max}} = \frac{v_{\min}}{v_{\max}} = \frac{1}{6}$$

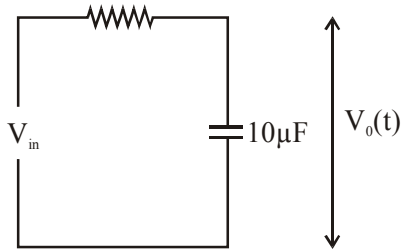
Ans. (1)

2. For the given input voltage waveform $V_{in}(t)$, the output voltage waveform $V_D(t)$, across the capacitor is correctly depicted by:



Official Ans. by NTA (1)

Sol.



$$V_0(t) = V_{in} \left(1 - e^{-\frac{t}{RC}} \right)$$

at $t = 5\mu s$

$$V_0(t) = 5 \left(1 - e^{-\frac{5 \times 10^{-6}}{10^3 \times 10 \times 10^{-9}}} \right)$$

$$= 5 (1 - e^{-0.5}) = 2V$$

Now $V_{in} = 0$ means discharging

$$V_0(t) = 2e^{-\frac{t}{RC}} = 2e^{-0.5}$$

$$= 1.21 V$$

Now for next $5 \mu s$

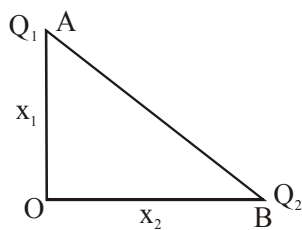
$$V_0(t) = 5 - 3.79e^{-\frac{t}{RC}}$$

after $5 \mu s$ again

$$V_0(t) = 2.79 \text{ Volt} \approx 3V$$

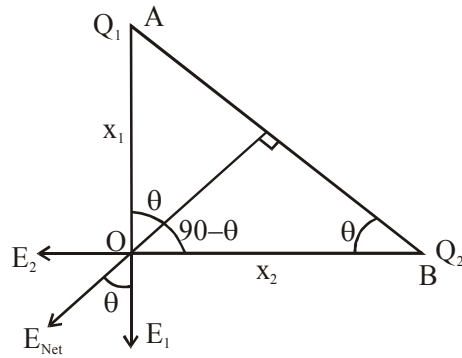
Most appropriate Ans. (1)

3. Charges Q_1 and Q_2 are at points A and B of a right angle triangle OAB (see figure). The resultant electric field at point O is perpendicular to the hypotenuse, then Q_1/Q_2 is proportional to :



- (1) $\frac{x_2^2}{x_1^2}$ (2) $\frac{x_1^3}{x_2^3}$ (3) $\frac{x_1}{x_2}$ (4) $\frac{x_2}{x_1}$

Sol.



$E_2 =$ electric field due to Q_2

$$= \frac{kQ_2}{x_2^2}$$

$$E_1 = \frac{kQ_1}{x_1^2}$$

From diagram

$$\tan \theta = \frac{E_2}{E_1} = \frac{x_1}{x_2}$$

$$\frac{kQ_2}{x_2^2} \times \frac{x_1^2}{kQ_1} = \frac{x_1}{x_2}$$

$$\frac{Q_2 x_1^2}{Q_1 x_2^2} = \frac{x_1}{x_2}$$

$$\frac{Q_2}{Q_1} = \frac{x_2}{x_1}$$

$$\frac{Q_1}{Q_2} = \frac{x_1}{x_2}$$

Ans. (3)

4. A screw gauge has 50 divisions on its circular scale. The circular scale is 4 units ahead of the pitch scale marking, prior to use. Upon one complete rotation of the circular scale, a displacement of 0.5 mm is noticed on the pitch scale. The nature of zero error involved, and the least count of the screw gauge, are respectively :
- (1) Negative, $2 \mu m$
 (2) Positive, $10 \mu m$
 (3) Positive, $0.1 \mu m$
 (4) Positive, 0.1 mm

Sol. Least count of screw gauge

$$= \frac{\text{Pitch}}{\text{no. of division on circular scale}}$$

$$= \frac{0.5}{50} \text{ mm} = 1 \times 10^{-5} \text{ m}$$

$$= 10 \mu\text{m}$$

Zero error in positive

Ans. (2)

5. An object of mass m is suspended at the end of a massless wire of length L and area of cross-section, A . Young modulus of the material of the wire is Y . If the mass is pulled down slightly its frequency of oscillation along the vertical direction is:

$$(1) f = \frac{1}{2\pi} \sqrt{\frac{YA}{mL}}$$

$$(2) f = \frac{1}{2\pi} \sqrt{\frac{YL}{mA}}$$

$$(3) f = \frac{1}{2\pi} \sqrt{\frac{mA}{YL}}$$

$$(4) f = \frac{1}{2\pi} \sqrt{\frac{mL}{YA}}$$

Official Ans. by NTA (1)

Sol. An elastic wire can be treated as a spring with

$$k = \frac{YA}{\ell}$$

$$T = 2\pi \sqrt{\frac{m}{k}}$$

$$f = \frac{1}{2\pi} \sqrt{\frac{k}{m}} = \frac{1}{2\pi} \sqrt{\frac{YA}{m\ell}}$$

Ans. (1)

6. A particle of charge q and mass m is moving with a velocity $-v\hat{i}$ ($v \neq 0$) towards a large screen placed in the $Y-Z$ plane at a distance d . If there is a magnetic field $\vec{B} = B_0\hat{k}$, the minimum value of v for which the particle will not hit the screen is:

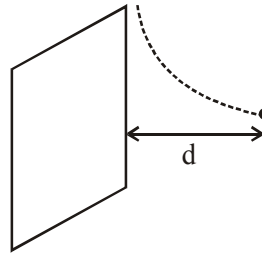
$$(1) \frac{qdB_0}{2m}$$

$$(2) \frac{qdB_0}{m}$$

$$(3) \frac{2qdB_0}{m}$$

$$(4) \frac{qdB_0}{3m}$$

Sol.



In uniform magnetic field particle moves in a circular path, if the radius of the circular path is ' d ', particle will not hit the screen.

$$d = \frac{mv}{qB_0}$$

$$v = \frac{qB_0 d}{m}$$

\therefore correct option is (2)

7. An insect is at the bottom of a hemispherical ditch of radius 1 m. It crawls up the ditch but starts slipping after it is at height h from the bottom. If the coefficient of friction between the ground and the insect is 0.75, then h is :

$$(g = 10\text{ms}^{-2})$$

$$(1) 0.80 \text{ m}$$

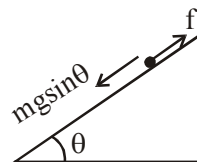
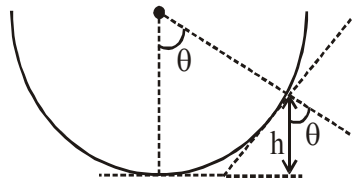
$$(2) 0.60 \text{ m}$$

$$(3) 0.45 \text{ m}$$

$$(4) 0.20 \text{ m}$$

Official Ans. by NTA (4)

Sol.



For balancing $mgsin\theta = f$

$$mgsin\theta = \mu mgcos\theta$$

$$\tan\theta = \mu$$

$$I_A : I_B : I_C = 4I : 2I : 0 \\ = 2 : 1 : 0$$

∴ correct option is (4)

10. An electron, a doubly ionized helium ion (He^{++}) and a proton are having the same kinetic energy. The relation between their respective de-Broglie wavelengths λ_e , $\lambda_{\text{He}^{++}}$ and λ_p is:

(1) $\lambda_e < \lambda_p < \lambda_{\text{He}^{++}}$ (2) $\lambda_e < \lambda_{\text{He}^{++}} = \lambda_p$

(3) $\lambda_e > \lambda_{\text{He}^{++}} > \lambda_p$ (4) $\lambda_e > \lambda_p > \lambda_{\text{He}^{++}}$

Official Ans. by NTA (4)

Sol.
$$\lambda = \frac{h}{P} = \frac{h}{\sqrt{2m(\text{KE})}}$$

$$\lambda \propto \frac{1}{\sqrt{m}} \Rightarrow \lambda = \frac{C}{\sqrt{m}}$$

$$m_{\text{He}^{++}} > m_p > m_e$$

$$\therefore \lambda_{\text{He}^{++}} < \lambda_p < \lambda_e$$

∴ correct option is (4)

11. An electron is moving along + x direction with a velocity of $6 \times 10^6 \text{ ms}^{-1}$. It enters a region of uniform electric field of 300 V/cm pointing along + y direction. The magnitude and direction of the magnetic field set up in this region such that the electron keeps moving along the x direction will be:

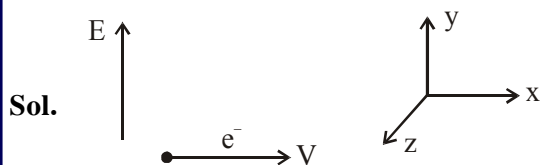
(1) $5 \times 10^{-3} \text{ T}$, along +z direction

(2) $3 \times 10^{-4} \text{ T}$, along -z direction

(3) $3 \times 10^{-4} \text{ T}$, along +z direction

(4) $5 \times 10^{-3} \text{ T}$, along -z direction

Official Ans. by NTA (1)



\vec{B} must be in +z axis.

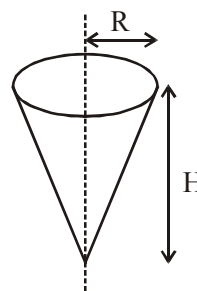
$$\vec{V} = 6 \times 10^6 \hat{i}$$

$$\vec{E} = 300 \hat{j} \text{ V/cm} = 3 \times 10^4 \text{ V/m}$$

$$E = VB$$

$$B = \frac{E}{V} = \frac{3 \times 10^4}{6 \times 10^6} = 5 \times 10^{-3} \text{ T}$$

12. Shown in the figure is a hollow icecream cone (it is open at the top). If its mass is M, radius of its top, R and height, H, then its moment of inertia about its axis is:



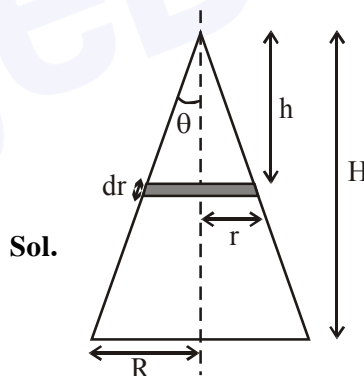
(1) $\frac{MR^2}{2}$

(2) $\frac{MH^2}{3}$

(3) $\frac{MR^2}{3}$

(4) $\frac{M(R^2 + H^2)}{4}$

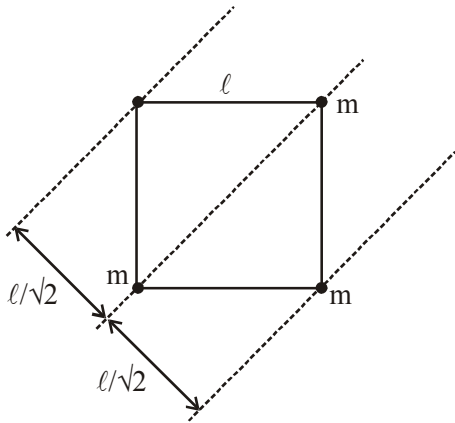
Official Ans. by NTA (1)



$$\text{Area} = \pi R \ell = \pi R (\sqrt{H^2 + R^2})$$

$$\text{Area of element } dA = 2\pi r d\ell = 2\pi r \frac{dh}{\cos \theta}$$

$$\text{mass of element } dm = \frac{M}{\pi R \sqrt{H^2 + R^2}} \times \frac{2\pi r dh}{\cos \theta}$$



Sol.

$$I = m(0)^2 + m\left(\frac{l}{\sqrt{2}}\right)^2 \times 2 + m(\sqrt{2}l)^2$$

$$= \frac{2m\ell^2}{2} + 2m\ell^2 = 3m\ell^2$$

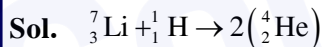
Angular momentum $L = I\omega$
 $= 3m\ell^2\omega$

16. You are given that Mass of ${}^7_3\text{Li} = 7.0160 \text{ u}$,
 Mass of ${}^4_2\text{He} = 4.0026 \text{ u}$
 and Mass of ${}^1_1\text{H} = 1.0079 \text{ u}$.

When 20 g of ${}^7_3\text{Li}$ is converted into ${}^4_2\text{He}$ by proton capture, the energy liberated, (in kWh), is: [Mass of nucleon = $1 \text{ GeV}/c^2$]

- (1) 8×10^6 (2) 1.33×10^6
 (3) 6.82×10^5 (4) 4.5×10^5

Official Ans. by NTA (2)



$$\Delta m \Rightarrow [m_{\text{Li}} + m_{\text{H}}] - 2[M_{\text{He}}]$$

Energy released in 1 reaction $\Rightarrow \Delta mc^2$.

In use of 7.016 u Li energy is Δmc^2

In use of 1gm Li energy is $\frac{\Delta mc^2}{m_{\text{Li}}}$

In use of 20 gm energy is $\Rightarrow \frac{\Delta mc^2}{m_{\text{Li}}} \times 20\text{gm}$

$$\Rightarrow \frac{[(7.016 + 1.0079) - 2 \times 4.0026] \text{u} \times c^2}{7.016 \times 1.6 \times 10^{-24} \text{gm}} \times 20\text{gm}$$

$$\Rightarrow \left(\frac{0.0187 \times 1.6 \times 10^{-19} \times 10^9}{-24} \times 20\text{gm} \right) \text{Joule}$$

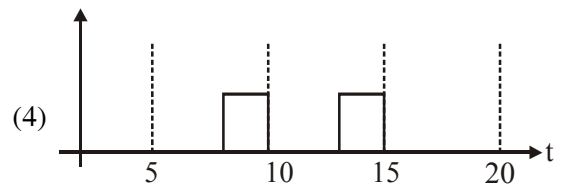
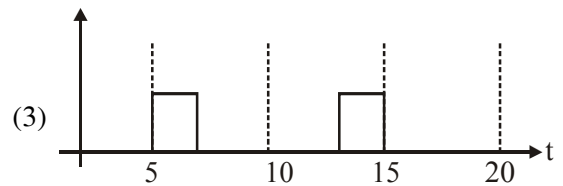
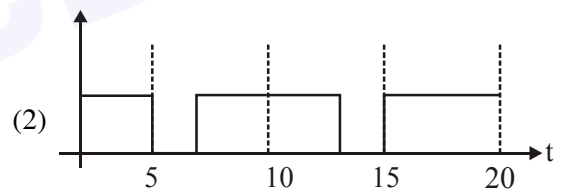
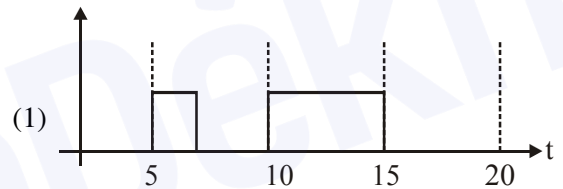
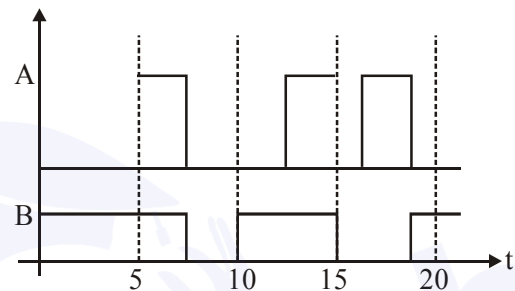
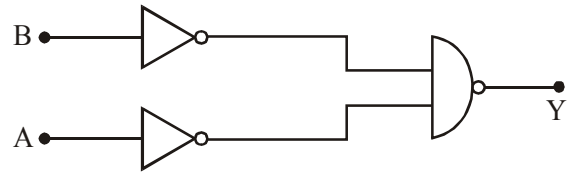
$$\Rightarrow 0.05 \times 10^{14} \text{ J}$$

$$\Rightarrow 1.4 \times 10^6 \text{ kWh}$$

$$[1 \text{ J} \Rightarrow 2.778 \times 10^{-7} \text{ kWh}]$$

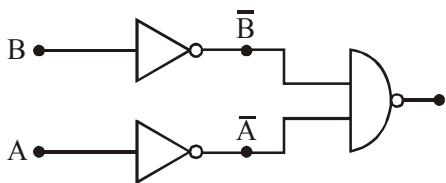
Ans. (2)

17. Identify the correct output signal Y in the given combination of gates (as shown) for the given inputs A and B.

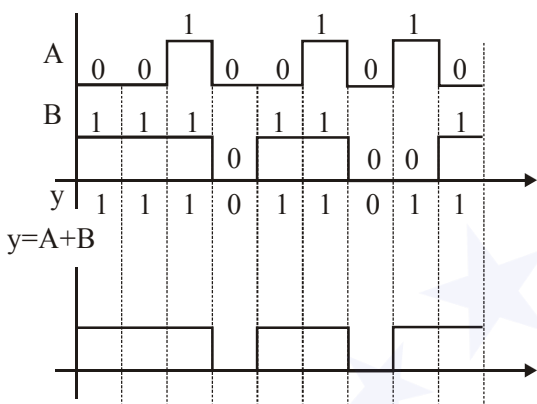


Official Ans. by NTA (3)

Sol.



$$y = \overline{\overline{A} \cdot \overline{B}} = \overline{\overline{A}} + \overline{\overline{B}} = A + B$$



18. Molecules of an ideal gas are known to have three translational degrees of freedom and two rotational degrees of freedom. The gas is maintained at a temperature of T. The total internal energy, U of a mole of this gas, and

the value of $\gamma \left(= \frac{C_p}{C_v} \right)$ given, respectively, by:

(1) $U = \frac{5}{2}RT$ and $\gamma = \frac{6}{5}$

(2) $U = 5RT$ and $\gamma = \frac{7}{5}$

(3) $U = 5RT$ and $\gamma = \frac{6}{5}$

(4) $U = \frac{5}{2}RT$ and $\gamma = \frac{7}{5}$

Sol. Total degree of freedom = 3 + 2 = 5

$$U = \frac{nfRT}{2} \Rightarrow \frac{5RT}{2}$$

$$\gamma \Rightarrow \frac{C_p}{C_v} \Rightarrow 1 + \frac{2}{f} \Rightarrow 1 + \frac{2}{5} \Rightarrow \frac{7}{5}$$

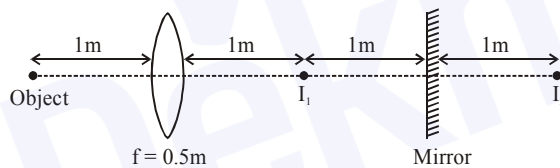
Ans. (4)

19. A point like object is placed at a distance of 1m in front of a convex lens of focal length 0.5 m. A plane mirror is placed at a distance of 2 m behind the lens. The position and nature of the final image formed by the system is :

- (1) 1 m from the mirror, virtual
- (2) 1 m from the mirror, real
- (3) 2.6 m from the mirror, real
- (4) 2.6 m from the mirror, virtual

Official Ans. by NTA (1,4)

Sol.



Object is at 2f. So image will also be at '2f'. (I_1).

Image of I_1 will be 1m behind mirror. i.e. $\Rightarrow I_2$

Now I_2 will be object for lens.

$$\therefore u \Rightarrow -3m$$

$$f \Rightarrow +0.5 m$$

$$\frac{1}{v} \Rightarrow \frac{1}{f} + \frac{1}{u}$$

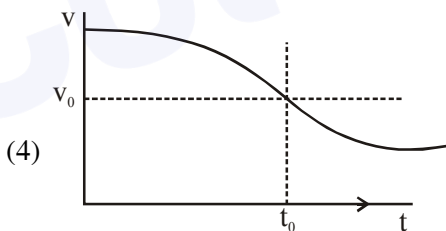
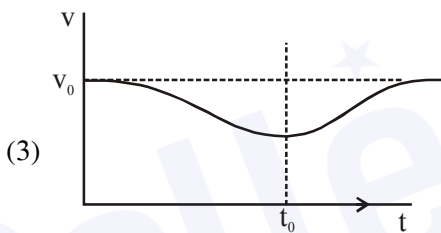
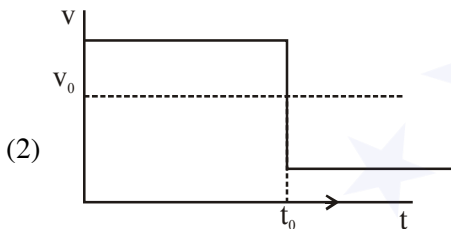
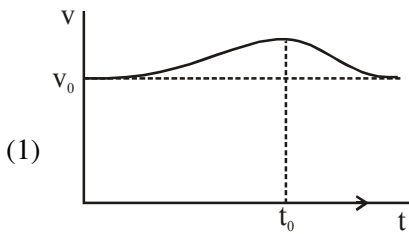
$$\Rightarrow \frac{1}{+0.5} + \frac{1}{-3}$$

$$v \Rightarrow \frac{3}{5} \Rightarrow 0.6m$$

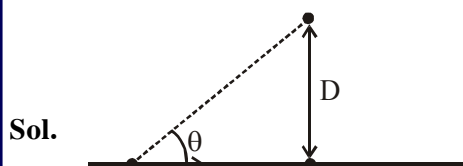
So total distance from mirror $\Rightarrow 2 + 0.6 \Rightarrow 2.6 m$ and real image

Ans. (3)

20. A sound source S is moving along a straight track with speed v , and is emitting sound of frequency ν_0 (see figure). An observer is standing at a finite distance, at the point O, from the track. The time variation of frequency heard by the observer is best represented by :
(t_0 represents the instant when the distance between the source and observer is minimum)



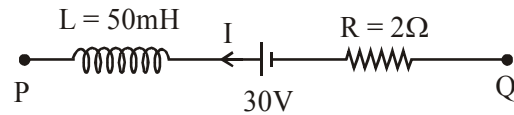
Official Ans. by NTA (4)



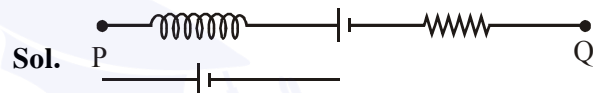
$$f_{\text{observed}} \Rightarrow \left(\frac{v_{\text{sound}}}{v_{\text{sound}} - v \cos \theta} \right) f_0$$

initially θ will be less $\Rightarrow \cos \theta$ more
 $\therefore f_{\text{observed}}$ more, then it will decrease.
 \therefore Ans. (4)

21. A part of a complete circuit is shown in the figure. At some instant, the value of current I is 1 A and it is decreasing at a rate of 10^2 A s^{-1} . The value of the potential difference $V_P - V_Q$, (in volts) at that instant, is.



Official Ans. by NTA (33.00)



$$\frac{L di}{dt} = 5$$

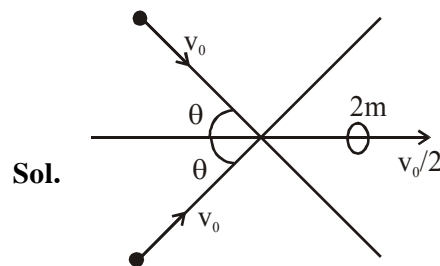
$$V_P - 5 - 30 + 2 \times 1 = V_Q$$

$$V_P - V_Q = 33 \text{ volt}$$

Ans. 33.00

22. Two bodies of the same mass are moving with the same speed, but in different directions in a plane. They have a completely inelastic collision and move together thereafter with a final speed which is half of their initial speed. The angle between the initial velocities of the two bodies (in degree) is.

Official Ans. by NTA (120.00)



Momentum conservation along x

$$2m v_0 \cos \theta = 2m \frac{v_0}{2}$$

$$\cos\theta = \frac{1}{2}$$

$$\theta = 60$$

Angle is $2\theta = 120$

Ans. 120.00

23. Suppose that intensity of a laser is

$\left(\frac{315}{\pi}\right) \text{W/m}^2$. The rms electric field, in units

of V/m associated with this source is close to the nearest integer is

($\epsilon_0 = 8.86 \times 10^{-12} \text{C}^2 \text{Nm}^{-2}$; $c = 3 \times 10^8 \text{ms}^{-1}$)

Official Ans. by NTA (275.00)

Sol. $I = \epsilon_0 E_{\text{rms}}^2 C$

$$E_{\text{rms}}^2 = \frac{I}{\epsilon_0 C}$$

$$= \frac{315}{\pi \epsilon_0} \times \frac{1}{C}$$

$$= \frac{4 \times 315}{4\pi \epsilon_0} \times \frac{1}{3 \times 10^8}$$

$$= \frac{4 \times 315 \times 9 \times 10^9}{3 \times 10^8}$$

$$E_{\text{rms}}^2 = 4 \times 315 \times 30$$

$$E_{\text{rms}} = 2\sqrt{315 \times 30}$$

$$= 194.42$$

Ans. 194.00

24. The density of a solid metal sphere is determined by measuring its mass and its diameter. The maximum error in the density

of the sphere is $\left(\frac{x}{100}\right)\%$. If the relative errors

in measuring the mass and the diameter are 6.0% and 1.5% respectively, the value of x is .

Official Ans. by NTA (1050.00)

Sol. $\rho = \frac{M}{V} = \frac{M}{\frac{4}{3}\pi\left(\frac{D}{2}\right)^3}$

$$\rho = \frac{6}{\pi} M D^{-3}$$

taking log

$$\ell n \rho = \ell n \left(\frac{6}{\pi}\right) + \ell n M - 3 \ell n D$$

Differentiates

$$\frac{d\rho}{\rho} = 0 + \frac{dM}{M} - 3 \frac{d(D)}{D}$$

for maximum error

$$100 \times \frac{d\rho}{\rho} = \frac{dM}{M} \times 100 + \frac{3dD}{D} \times 100$$

$$= 6 + 3 \times 1.5$$

$$= 10.5 \%$$

$$= \frac{1050}{100} \% \text{ so } x = 1050.00$$

25. Initially a gas of diatomic molecules is contained in a cylinder of volume V_1 at a pressure P_1 and temperature 250 K. Assuming that 25% of the molecules get dissociated causing a change in number of moles. The pressure of the resulting gas at temperature 2000 K, when contained in a volume $2V_1$ is given by P_2 . The ratio P_2/P_1 is.

Official Ans. by NTA (5.00)

Sol. $PV = nRT$

$$P_1 V_1 = nR \cdot 250$$

$$P_2 (2V_1) = \frac{5n}{4} R \times 2000$$

Divide

$$\frac{P_1}{2P_2} = \frac{4 \times 250}{5 \times 2000}$$

$$\frac{P_1}{P_2} = \frac{1}{5}$$

$$\frac{P_2}{P_1} = 5$$

Ans. 5.00