

1. Algebra:

- Question: Solve for x : $2x + 5 = 11$
- Answer: $x = 3$
- Explanation: Subtract 5 from both sides: $2x = 6$. Divide both sides by 2: $x = 3$.

2. Trigonometry:

- Question: What is the value of $\sin(30^\circ)$?
- Answer: $1/2$
- Explanation: In a right-angled triangle with an angle of 30° , the sine of that angle is the ratio of the length of the side opposite the angle to the length of the hypotenuse, which is $1/2$.

3. Geometry:

- Question: What is the formula for the area of a rectangle with length 'l' and width 'w'?
- Answer: $\text{Area} = l \times w$
- Explanation: The area of a rectangle is calculated by multiplying its length by its width.

4. Calculus:

- Question: What is the derivative of x^2 with respect to x ?
- Answer: $2x$
- Explanation: Using the power rule of differentiation, the derivative of x^n is nx^{n-1} . For x^2 , $n = 2$, so the derivative is $2x^{2-1} = 2x$.

5. Statistics:

- Question: What is the mean of the numbers 2, 4, 6, and 8?
- Answer: 5
- Explanation: The mean is calculated by summing the numbers and dividing by the count of the numbers. $(2 + 4 + 6 + 8) / 4 = 20 / 4 = 5$.

6. Number Systems:

- Question: What is the value of $5!$ (5 factorial)?
- Answer: 120
- Explanation: $5! = 5 \times 4 \times 3 \times 2 \times 1 = 120$.

7. Sets and Relations:

- Question: If $A = \{1, 2, 3\}$ and $B = \{3, 4, 5\}$, what is the union of A and B ($A \cup B$)?
- Answer: $\{1, 2, 3, 4, 5\}$
- Explanation: The union of two sets contains all the elements that are in either set A or set B or both.

8. Probability:

- Question: What is the probability of getting a head when a fair coin is tossed once?
- Answer: $1/2$
- Explanation: There are two possible outcomes (head or tail), and only one is a head. $\text{Probability} = (\text{favorable outcomes}) / (\text{total possible outcomes}) = 1/2$.

9. Coordinate Geometry:

- Question: What is the distance between the points (1, 2) and (4, 6)?
- Answer: 5 units
- Explanation: Using the distance formula: $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$. $\text{Distance} = \sqrt{(4 - 1)^2 + (6 - 2)^2} = \sqrt{3^2 + 4^2} = \sqrt{9 + 16} = \sqrt{25} = 5$.

10. Logarithms:

- Question: What is the value of $\log_{10}(100)$?
- Answer: 2
- Explanation: $\log_{10}(100)$ asks, "to what power must 10 be raised to get 100?" The answer is 2 since $10^2 = 100$.

11. Linear Equations:

- Question: What is the slope of the line represented by the equation $y = 3x - 2$?
- Answer: 3
- Explanation: In the slope-intercept form of a linear equation ($y = mx + c$), 'm' represents the slope. Here, $m = 3$.

12. Quadratic Equations:

- Question: What are the roots of the quadratic equation $x^2 - 5x + 6 = 0$?
- Answer: $x = 2$ and $x = 3$
- Explanation: Factoring the quadratic equation, we get $(x - 2)(x - 3) = 0$. Therefore, the roots are $x = 2$ and $x = 3$.

13. Inequalities:

- Question: Solve the inequality: $2x - 1 < 5$
- Answer: $x < 3$
- Explanation: Add 1 to both sides: $2x < 6$. Divide both sides by 2: $x < 3$.

14. Matrices:

- Question: If $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$, what is the determinant of A?
- Answer: -2
- Explanation: The determinant of a 2×2 matrix $\begin{bmatrix} a & b \\ c & d \end{bmatrix}$ is $ad - bc$. For A, determinant = $(1 * 4) - (2 * 3) = 4 - 6 = -2$.

15. Sequences and Series:

- Question: What is the next term in the arithmetic progression 2, 5, 8, ...?
- Answer: 11
- Explanation: The common difference between consecutive terms is $5 - 2 = 3$. So, the next term is $8 + 3 = 11$.

16. Permutations and Combinations:

- Question: How many different ways can you arrange the letters in the word "CAT"?
- Answer: 6
- Explanation: There are 3 distinct letters, so the number of permutations is $3! = 3 \times 2 \times 1 = 6$.

17. Ratio and Proportion:

- Question: If the ratio of boys to girls in a class is 2:3, and there are 20 boys, how many girls are there?
- Answer: 30 girls
- Explanation: Let the number of girls be 'x'. Then, $\frac{2}{3} = \frac{20}{x}$. Cross-multiplying gives $2x = 60$, so $x = 30$.

18. Mensuration:

- Question: What is the formula for the circumference of a circle with radius 'r'?
- Answer: Circumference = $2\pi r$
- Explanation: The circumference is the total distance around the circle.

19. Statistics:

- Question: What is the median of the numbers 1, 3, 5, 2, 4?
- Answer: 3
- Explanation: First, arrange the numbers in ascending order: 1, 2, 3, 4, 5. The median is the middle value, which is 3.

20. Complex Numbers:

- Question: What is the real part of the complex number $3 + 4i$?
- Answer: 3
- Explanation: A complex number is in the form $a + bi$, where 'a' is the real part and 'b' is the imaginary part. Here, the real part is 3.

21. Polynomials:

- Question: What is the degree of the polynomial $5x^3 - 2x + 7$?
- Answer: 3
- Explanation: The degree of a polynomial is the highest power of the variable in the polynomial. Here, the highest power of x is 3.

22. Trigonometry:

- Question: What is the value of $\cos(0^\circ)$?
- Answer: 1
- Explanation: The cosine of 0 degrees is the ratio of the adjacent side to the hypotenuse in a right-angled triangle where the angle is 0 degrees.

23. Geometry:

- Question: What is the sum of the interior angles of a triangle?
- Answer: 180 degrees
- Explanation: This is a fundamental property of triangles in Euclidean geometry.

24. Calculus:

- Question: What is the integral of $2x$ concerning x ?
- Answer: $x^2 + C$
- Explanation: The integral of x^n is $(x^{n+1}) / (n+1) + C$. For $2x$, $n = 1$, so the integral is $(2x^2) / 2 + C = x^2 + C$, where C is the constant of integration.