

COMEDK 2024 Morning Shift

Physics

Question 1

The resistance of the galvanometer and shunt of an ammeter are 90 ohm and 10 ohm respectively, then the fraction of the main current passing through the galvanometer and the shut respectively are:

Options:

A. $\frac{1}{90}$ and $\frac{1}{10}$

B. $\frac{1}{10}$ and $\frac{1}{90}$

C. $\frac{1}{10}$ and $\frac{9}{10}$

D. $\frac{9}{10}$ and $\frac{1}{10}$

Answer: C

Question 2

A glass of hot water cools from

90°C to 70°C in 3 minutes when the

temperature of surroundings is 20°C. What is the time taken by the

glass of hot water to cool from 60°C to 40°C if the surrounding temperature remains the same at 20°C?

Options:

A. 15 minutes

B. 6 minutes

C. 12 minutes

D. 10 minutes

Answer: B

Question 3

When two objects are moving along a straight line in the same direction, the distance between them increases by 6 m in one second. If the objects move with their constant speed towards each other the distance decreases by 8 m in one second, then the speed of the objects are :

Options:

A. 14 ms^{-1} and 2 ms^{-1}

B. 7 ms^{-1} and 1 ms^{-1}

C. 3.5 ms^{-1} and 2 ms^{-1}

D. 3.5 ms^{-1} and 1 ms^{-1}

Answer: B

Solution:

Let the speeds of the two objects be v_1

and v_2 .

When the two objects are moving in the same direction, the relative speed is given by:

$$|v_1 - v_2|$$

According to the problem, this relative speed results in an increase in the distance between them by 6 m in one second. Therefore, we have:

$$|v_1 - v_2| = 6$$

When the two objects are moving towards each other, the relative speed is given by:

$$v_1 + v_2$$

In this case, the distance decreases by 8 m in one second, so we have:

$$v_1 + v_2 = 8$$

We now have two equations:

$$1. |v_1 - v_2| = 6$$

$$1. v_1 + v_2 = 8$$

We can solve these equations by considering the absolute value condition in two cases:

Case 1: $v_1 \geq v_2$

$$v_1 - v_2 = 6 \quad (\text{from } |v_1 - v_2| = 6)$$

$$v_1 + v_2 = 8$$

Adding these two equations:

$$(v_1 - v_2) + (v_1 + v_2) = 6 + 8$$

$$2v_1 = 14$$

$$v_1 = 7$$

Substituting $v_1 = 7$ into $v_1 + v_2 = 8$:

$$7 + v_2 = 8$$

$$v_2 = 1$$

Case 2: $v_1 < v_2$

$$v_2 - v_1 = 6 \quad (\text{from } |v_1 - v_2| = 6)$$

$$v_1 + v_2 = 8$$

Adding these two equations:

$$(v_2 - v_1) + (v_1 + v_2) = 6 + 8$$

$$2v_2 = 14$$

$$v_2 = 7$$

Substituting $v_2 = 7$ into $v_1 + v_2 = 8$:

$$v_1 + 7 = 8$$

$$v_1 = 1$$

From both cases, we find that the speeds of the objects are 7 ms^{-1} and 1 ms^{-1} .

Therefore, the correct answer is:

Option B: 7 ms^{-1} and 1 ms^{-1}

Question 4

In the Young's double slit experiment n th bright for red coincides with $(n+1)$ th bright for violet. Then the value of ' n ' is: (given: wave length of red light = 6300\AA and wave length of violet = 4200\AA).

Options:

A. 2 B. 4 C. 3 D. 1

Answer: A

Solution:

In Young's double slit experiment, the position of the

n^{th} bright fringe is given by the equation:

$$x_n = \frac{n\lambda D}{d}$$

where:

- n is the position of the fringe
- x is the order number of the fringe
- λ is the wavelength of the light used
- D is the distance between the slits and the screen
- d is the distance between the two slits

In this problem, we are given that the n th bright fringe for red light coincides with the $(n + 1)^{\text{th}}$ bright fringe for violet light. This means:

$$n\lambda^{\text{red}} = (n + 1)\lambda^{\text{violet}}$$

Given the wavelengths:

- $\lambda^{\text{red}} = 6300\text{\AA}$
- $\lambda^{\text{violet}} = 4200\text{\AA}$

We can substitute these values into the equation:

$$n \cdot 6300 = (n + 1) \cdot 4200$$

Simplifying this equation:

$$6300n = 4200n + 4200$$

$$2100n = 4200$$

$$n = 2$$

So, the value of 'n' is 2.

Thus, the correct option is:

Option A: 2

Question 5

A metal ball of 20 g is projected at an angle 30° with the horizontal with an initial velocity 10 ms^{-1} . If the mass and angle of projection are doubled keeping the initial velocity the same, the ratio of the maximum height attained in the former to the latter case is :

Options:

A. 1 : 2 B. 2 : 1 C. 1 : 3 D. 3 : 1

Answer: C

Solution:

To determine the ratio of the maximum heights attained in the two cases, let's start by deriving the formula for the maximum height reached by a projectile. The maximum height H for a projectile is given by:

$$H = \frac{u^2 \sin^2(\theta)}{2g}$$

Here:

- u is the initial velocity
- θ is the angle of projection
- g is the acceleration due to gravity

For the first case:

- Initial velocity, $u=10 \text{ m/s}$
- Angle of projection, $\theta=30^\circ$

Substituting these values into the formula:

$$H_1 = \frac{(10)^2 \sin^2(30^\circ)}{2 \times 9.8}$$

We know that $\sin(30^\circ) = \frac{1}{2}$, so:

$$H_1 = \frac{100 \times \frac{1}{4}}{2 \times 9.8} = \frac{100 \times 14}{2 \times 9.8} = \frac{25}{19.6}$$

For the second case, the mass and the angle of projection are doubled, but the mass does not affect the height. Therefore, the new angle of projection is:

- $\theta' = 2 \times 30^\circ = 60^\circ$

Using the same initial velocity $u = 10$ m/s, we substitute into the formula:

$$H_2 = \frac{(10)^2 \sin^2(60^\circ)}{2 \times 9.8}$$

We know that $\sin(60^\circ) = \frac{\sqrt{3}}{2}$, so:

$$H_2 = \frac{100 \times \frac{3}{4}}{2 \times 9.8} = \frac{100 \times 3}{2 \times 9.8} = \frac{75}{19.6}$$

Now, to find the ratio of the maximum heights, we calculate:

$$\text{Ratio} = \frac{H_1}{H_2} = \frac{\frac{25}{19.6}}{\frac{75}{19.6}} = \frac{25}{75} = \frac{1}{3}$$

Therefore, the ratio of the maximum height attained in the former to the latter case is 1 : 3, which corresponds to Option C.

Option C: 1 : 3

Question 6

The threshold frequency for a metal surface is ' n_0 '.

A photo electric current ' I ' is produced when it is exposed to a light of frequency ' n '. If both the frequency and intensity are halved, the new photoelectric current ' I_1 ' will become:

Options:

A. $I_1 = \frac{1}{4} I$

B. $I_1 = 2I$

C. $I_1 = 0$

D. $I_1 = \frac{1}{2} I$

Answer: C

Solution:

To solve this problem, let's go step by step and apply the photoelectric effect equations. According to the photoelectric effect, the photoelectric current I depends on the number of photons hitting the surface and is directly proportional to the intensity of the light.

1. Threshold Frequency (n_0): The minimum frequency of light required to eject electrons from the metal surface.

2. Given Frequency: The light has a frequency of $11 \frac{6}{5} n_0$, which is higher than the threshold frequency n_0 .

3. Initial Intensity (I_1): The initial intensity of the light is I_1 , producing a photoelectric current I_1 .

4. Reducing Frequency and Intensity: Both frequency and intensity are halved. Therefore, the new frequency is $\frac{1}{2} (11 \frac{6}{5} n_0) = \frac{11}{5} n_0$. The new intensity becomes $\frac{1}{4} I_1$.

When the frequency is reduced to $\frac{11}{5} n_0$, it becomes lower than the threshold frequency n_0 , which means no electrons will be ejected from the metal surface. Hence, no photoelectric current will be produced.

Therefore, the new photoelectric current will be zero:

Option C: $I_1 = 0$

Question 7

A 500 W heating unit is designed to operate on a 400 V line. If line voltage drops to 160 V, the percentage drop in heat output will be:

Options:

A. 74% B.

85% C.

84% D.

75%

Answer: C

Solution:

To determine the percentage drop in heat output, we first need to understand that the power output P of an electrical device is proportional to the square of the voltage V . Mathematically, this relationship is represented as:

$$P \propto V^2 \quad \text{or} \quad P = \frac{V^2}{R}$$

where R is the resistance of the heating unit. In this problem, we need to compare the power output at two different voltages, 400 V and 160 V.

Let's denote the initial power output at 400 V as P_1 and the power output at 160 V as P_2 . Given that the initial power output is 500 W, we can write:

$$P_1 = 500 \text{ W}$$

Since the power is proportional to the square of the voltage:

$$P_1 = k \cdot V_1^2$$

and

$$P_2 = k \cdot V_2^2$$

where k is a proportionality constant. We can divide these equations to find the ratio of P_2 to P_1 :

$$\frac{P_2}{P_1} = \frac{V_2^2}{V_1^2}$$

Substituting the given voltage values:

$$\frac{P_2}{P_1} = \left(\frac{160}{400} \right)^2 = \frac{25600}{160000} = \frac{16}{100} = 0.16$$

This means that the power output at 160 V is 0.16 times the power output at 400 V. To find P_2 , we multiply P_1 by 0.16:

$$P_2 = 0.16 \cdot 500 \text{ W} = 80 \text{ W}$$

The percentage drop in heat output is then given by:

$$\text{Percentage Drop} = \left(\frac{P_1 - P_2}{P_1} \right) \times 100$$

Substituting the values:

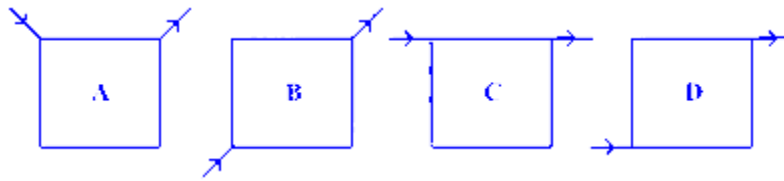
$$\text{Percentage Drop} = \left(\frac{500 \text{ W} - 80 \text{ W}}{500 \text{ W}} \right) \times 100 = \left(\frac{420}{500} \right) \times 100 = 84\%$$

Thus, the percentage drop in heat output is 84%. The correct answer is:

Option C - 84%.

Question 8

Current flows through uniform, square frames as shown in the figure. In which case is the magnetic field at the centre of the frame not zero?



Options:

A. A B. D C. C D. B

Answer: C

Question 9

A transformer which steps down 330 V to 33 V is to operate a device having impedance 110Ω . The current drawn by the primary coil of the transformer is :

Options:

A. 0.3 A

B. 0.03 A

C. 3 A

D. 1.5 A

Answer: B

Solution:

First, let's identify the voltage transformation ratio for the transformer. The primary voltage secondary voltage V_s is 33 V. The voltage transformation ratio k is given by:

V_p is 330 V and the

$$k = \frac{V_p}{V_s} = \frac{330}{33} = 10$$

This means the primary voltage is 10 times the secondary voltage.

Next, we need to determine the current in the secondary coil, which can be found using Ohm's Law. The impedance of the device connected to the secondary coil is given as 110Ω , and the voltage across it is 33V:

$$I_s = \frac{V_s}{Z} = \frac{33}{110} = 0.3 \text{ A}$$

Now, using the current transformation relation in a transformer, which is inversely proportional to the voltage transformation ratio:

$$I_p = \frac{I_s}{k} = \frac{0.3}{10} = 0.03 \text{ A}$$

The current drawn by the primary coil of the transformer is therefore 0.03 A.

So, the correct answer is:

Option B:

0.03 A

Question 10

A cell of emf E and internal resistance r is connected to two external resistances R_1 and R_2 and a perfect ammeter. The current in the circuit is measured in four different situations:

- (a) without any external resistance in the circuit.
- (b) with resistance R_1 only
- (c) with R_1 and R_2 in series combination.
- (d) with R_1 and R_2 in parallel combination.

The currents measured in the four cases in ascending order are

Options:

A. $c < b < d < a$ B. $a < b < d < c$ C. $c < d < b < a$ D. $a < d < b < c$

Answer: A

Question 11

Select the unit of the coefficient of mutual induction from the following.

Options:

A. volt. second / ampere

B. weber. ampere

C. ampere / weber

D. volt. ampere / second

Answer: A

Solution:

The coefficient of mutual induction, commonly denoted by M , is defined by the relationship between the induced electromotive force (EMF) in one coil and the rate of change of current in another coil. According to Faraday's Law of Induction, the induced EMF (E) in a coil is given by:

$$E = -M \frac{di}{dt}$$

Where:

- E is the induced EMF in volts (V).
- M is the mutual inductance.
- $\frac{di}{dt}$ is the rate of change of current in amperes per second (A/s).

Rearranging this equation to solve for M , we get:

$$M = - \frac{E}{\frac{di}{dt}}$$

From this relationship, the units of M can be derived. The unit of EMF (\mathcal{E}) is volts (V), and the unit of amperes per second (A/s). Thus, the unit of the coefficient of mutual induction is:

$\frac{d\Phi}{dt}$ is

$$M = \frac{V}{A/s} = \text{volt} \cdot \text{second/ampere}$$

Therefore, the correct unit for the coefficient of mutual induction is:

Option A: volt. second / ampere

Question 12

Steel is preferred to soft iron for making permanent magnets because,

Options:

- A. Susceptibility of steel is less than one
- B. Permeability of steel is slightly greater than soft iron
- C. Steel has more coercivity than soft iron
- D. Steel is more paramagnetic

Answer: C

Solution:

Steel is preferred to soft iron for making permanent magnets primarily due to its magnetic properties, particularly its coercivity. Coercivity is a measure of the resistance of a ferromagnetic material to becoming demagnetized. A higher coercivity means that the material can maintain its magnetization in the presence of external magnetic fields or physical disturbances.

Among the given options, the correct answer is:

Option C: Steel has more coercivity than soft iron

Here's a more detailed explanation: Coercivity is crucial for permanent magnets because it determines the ability of the material to retain its magnetic properties over time. Soft iron has a low coercivity, making it easy to magnetize and demagnetize. This property makes soft iron suitable for temporary magnets or electromagnets, where a quick magnetic response is needed.

On the other hand, steel has a much higher coercivity compared to soft iron. This higher coercivity allows steel to retain its magnetization even after the external magnetic field is removed. Hence, steel is more suitable for making permanent magnets, as it can maintain its magnetic state for a long period of time without significant loss of magnetic strength.

The concept of coercivity can be mathematically represented by the hysteresis loop of a material. The wider the loop, the higher the coercivity. For a permanent magnet, the area within the hysteresis loop is also significant as it indicates the energy stored in the magnet.

In mathematical terms, coercivity H_c can be understood from the hysteresis curve of the material. The point H_c is where the magnetization M or B , which represents the magnetic flux density, returns to zero when an external magnetic field is applied in the reverse direction:

H_c = Coercivity of the material

Therefore, the key property that makes steel more suitable than soft iron for making permanent magnets is its higher coercivity.

Question 13

A particle executes a simple harmonic motion of amplitude A . The distance from the mean position at which its kinetic energy is equal to its potential energy is

Options:

A. $0.91 A$ B. $0.71 A$ C. $0.81 A$ D. $0.51 A$

Answer: B

Solution:

In simple harmonic motion (SHM), the total mechanical energy of the system is conserved and is given by the sum of kinetic energy (KE) and potential energy (PE). At any point in the motion, the kinetic energy and potential energy can be expressed as:

The total energy (E) in SHM of amplitude A is

$$E = \frac{1}{2} k A^2$$

where k is the spring constant.

The potential energy (PE) at a distance x from the mean position is given by:

$$PE = \frac{1}{2} k x^2$$

The kinetic energy (KE) at a distance x from the mean position is:

$$KE = \frac{1}{2}k(A^2 - x^2)$$

We need to find the distance from the mean position where the kinetic energy is equal to the potential energy. Therefore, we set the kinetic energy equal to the potential energy:

$$\frac{1}{2}kx^2 = \frac{1}{2}k(A^2 - x^2)$$

By simplifying the equation, we get:

$$x^2 = A^2 - x^2$$

Adding x^2 to both sides, we have:

$$2x^2 = A^2$$

Dividing both sides by 2, we get:

$$x^2 = \frac{A^2}{2}$$

Taking the square root of both sides, we find:

$$x = \frac{A}{\sqrt{2}} = \frac{A \times \sqrt{2}}{\sqrt{2} \times \sqrt{2}} = \frac{\sqrt{2}}{2} A$$

We know that $\sqrt{2} \approx 1.41$ so:

$$x \approx \frac{1.41}{2} A \approx 0.71A$$

Therefore, the distance from the mean position at which the kinetic energy is equal to its potential energy is approximately $0.71A$. Hence, the correct answer is Option B.

Question 14

A body of mass 5 kg at rest is rotated for 25 s with a constant moment of force 10 Nm. Find the work done if the moment of inertia of the body is 5 kg m².

Options:

A. 625 J

B. 125 J

C. 6250 J

D. 1250 J

Answer: C

Solution:

To find the work done on the body, we need to understand the relationship between torque, angular acceleration, and work done in rotational motion.

We know the following:

- Mass of the body, $m=5 \text{ kg}$
- Time of rotation, $t=25 \text{ s}$
- Constant moment of force (torque), $\tau=10 \text{ Nm}$
- Moment of inertia, $I=5 \text{ kg m}^2$

First, we find the angular acceleration. Torque (τ) is related to angular acceleration (α) by the equation:

$$\tau = I\alpha$$

Solving for angular acceleration (α):

$$\alpha = \frac{\tau}{I} = \frac{10 \text{ Nm}}{5 \text{ kg m}^2} = 2 \text{ rad/s}^2$$

Next, we need to find the final angular velocity (ω) after time t . The initial angular velocity (ω_0) is zero because the body is at rest initially. Using the kinematic equation for rotational motion:

$$\omega = \omega_0 + \alpha t$$

Substitute the known values:

$$\omega = 0 + (2 \text{ rad/s}^2)(25 \text{ s}) = 50 \text{ rad/s}$$

Now, we can calculate the work done. The work done by a torque in rotational motion is given by:

$$W = \frac{1}{2} I \omega^2$$

Substitute the known values:

$$W = \frac{1}{2} (5 \text{ kg m}^2)(50 \text{ rad/s})^2$$

Calculate the work done:

$$W = \frac{1}{2} \times 5 \times (50)^2 = 12500 \text{ J}$$

The work done is 12500 J which corresponds to Option C.

Question 15

In the normal adjustment of an astronomical telescope, the objective and eyepiece are 32 cm apart. If the magnifying power of the telescope

is 7, find the focal lengths of the objective and eyepiece.

Options:

A. $f_o = 7 \text{ cm}$ and $f_e = 28 \text{ cm}$

B. $f_o = 28 \text{ cm}$ and $f_e = 7 \text{ cm}$

C. $f_e = 28 \text{ cm}$ and $f_o = 4 \text{ cm}$

D. $f_o = 28 \text{ cm}$ and $f_e = 4 \text{ cm}$

Answer: D

Solution:

In an astronomical telescope, the magnifying power (M) is given by the ratio of the focal length of the objective

(f_o) to the focal length of the eyepiece (f_e):

$$M = \frac{f_o}{f_e}$$

Given that the magnifying power is 7, we have:

$$7 = \frac{f_o}{f_e}$$

This implies:

$$f_o = 7f_e$$

Also, it is given that the objective and eyepiece are 32 cm apart. The separation between the objective and the eyepiece in a telescope adjusted for normal vision is equal to the sum of their focal lengths:

$$f_o + f_e = 32 \text{ cm}$$

Substituting the value of f_o from the first equation $f_o = 7f_e$ into the second equation, we get:

$$7f_e + f_e = 32$$

Combining like terms:

$$8f_e = 32$$

Solving for f_e , we get:

$$f_e = \frac{32}{8} = 4 \text{ cm}$$

Now, substituting this back to find f_o :

$$f_o = 7 \times 4 = 28 \text{ cm}$$

Therefore, the focal lengths of the objective and the eyepiece are:

$$f_o = 28 \text{ cm}$$

$$f_e = 4 \text{ cm}$$

Hence, the correct option is:

Option D: $f_o = 28 \text{ cm}$ and $f_e = 4 \text{ cm}$

Question 16

In a given semiconductor, the ratio of the number density of electron to number density of hole is 2:1. If $\frac{1}{7}$ th of the total current is due to the hole and the remaining is due to the electrons, the ratio of the drift velocity of holes to the drift velocity of electrons is :

Options:

A. $\frac{7}{3}$

B. $\frac{3}{1}$

C. $\frac{3}{2}$

D. $\frac{1}{3}$

Answer: D

Solution:

To find the ratio of the drift velocity of holes to the drift velocity of electrons, we need to analyze the given information about the current and the number densities of electrons and holes.

Let's denote the following:

- Number density of electrons: n_e
- Number density of holes: n_h
- Drift velocity of electrons: v_e
- Drift velocity of holes: v_h

According to the problem, the ratio of the number density of electrons to holes is:

$$\frac{n_e}{n_h} = 2 : 1$$

So we can write:

$$n_e = 2n_h$$

The total current density J can be expressed as the sum of the current densities due to electrons and holes:

$$J = J_e + J_h$$

We also know the relationship for the current density for electrons and holes:

$$J_e = n_e e v_e$$

$$J_h = n_h e v_h$$

Given that $\frac{1}{7}$ th of the total current is due to holes, we write:

$$J_h = \frac{1}{7}J$$

Therefore, the remaining current due to electrons is:

$$J_e = J - J_h = J - \frac{1}{7}J = \frac{6}{7}J$$

Now substituting the expressions for J_e and J_h , we get:

$$n_e e v_e = \frac{6}{7}J$$

$$n_h e v_h = \frac{1}{7}J$$

Dividing these two equations, we have:

$$\frac{n_h v_h}{n_e v_e} = \frac{1/7}{6/7}$$

$$\frac{n_h v_h}{n_e} = \frac{1}{6}$$

Substitute the ratio of the number densities $\frac{n_h}{n_e} = \frac{1}{2}$:

$$\frac{1}{2} \cdot v_h = \frac{1}{6}$$

$$v_h = \frac{1}{6} \cdot 2 = \frac{1}{3}$$

Therefore, the ratio of the drift velocity of holes to the drift velocity of electrons is:

$$\frac{v_h}{v_e} = \frac{1}{3}$$

So, the correct answer is Option D: 1:3 .

Question 17

If A is the areal velocity of a planet of mass M , then its angular momentum is

Options:

A. MA

$$\frac{MA}{2}$$

B. MA

C. $2MA$

D. $\frac{MA}{3}$

Answer: C

Solution:

The areal velocity of a planet is the rate at which its radius vector sweeps out area. It is given by:

$$A = \frac{1}{2} r^2 \omega$$

where r is the distance from the planet to the sun and ω is its angular velocity. The angular momentum of the planet is given by:

$$L = I\omega = Mr^2\omega$$

where I is the moment of inertia of the planet. Substituting the expression for ω from the areal velocity equation, we get:

$$L = Mr^2 \left(\frac{2A}{r^2} \right) = 2MA$$

Therefore, the angular momentum of the planet is $2MA$. So the answer is Option C.

Question 18

When a particular wave length of light is used the focal length of a convex mirror is found to be 10 cm. If the wave length of the incident light is doubled keeping the area of the mirror constant, the focal length of the mirror will be:

Options:

A. 5 cm

B. 20 cm C. 15 cm D. 10 cm

Answer: D

Solution:

The focal length of a convex mirror is independent of the wavelength of the incident light. This is because the focal length of a mirror is determined by the curvature of the reflecting surface and not by the properties of the light used.

Therefore, even if the wavelength of the incident light is doubled, the focal length of the mirror will remain the same. As given, the original focal length of the convex mirror is 10 cm. So, if the wavelength is doubled, the focal length will still be:

10 cm

Hence, the correct option is: Option D: 10 cm -----

Question 19

The mass of a particle A is double that of the particle B and the kinetic energy of B is $\frac{1}{8}$ th that of A then the ratio of the de- Broglie wavelength of A to that of B is:

Options:

A. 1 : 2 B. 2

: 1 C. 1 : 4

D. 4 : 1

Answer: C

Solution:

To solve this problem, let's start by understanding the relationship between the kinetic energy, mass, and de Broglie wavelength of the particles.

The de Broglie wavelength λ of a particle is given by:

$$\lambda = \frac{h}{p}$$

where h is Planck's constant and p is the momentum of the particle.

The momentum p can be expressed as:

$$p = \sqrt{2mK}$$

where m is the mass and K is the kinetic energy of the particle.

Let's denote the masses and kinetic energies of particles A and B as follows:

Mass of particle A: m_A

Mass of particle B: m_B

Since the mass of particle A is double that of particle B:

$$m_A = 2m_B$$

Kinetic energy of particle A: K_A

Kinetic energy of particle B: K_B

Given that the kinetic energy of particle B is $\frac{1}{8}$ th that of A:

$$K_B = \frac{K_A}{8}$$

Now, let's find the ratio of the de Broglie wavelengths of particles A and B. The de Broglie wavelength for particle A is:

$$\lambda_A = \frac{h}{\sqrt{2m_A K_A}}$$

The de Broglie wavelength for particle B is:

$$\lambda_B = \frac{h}{\sqrt{2m_B K_B}}$$

We need to find the ratio $\frac{\lambda_A}{\lambda_B}$:

$$\frac{\lambda_A}{\lambda_B} = \frac{\frac{h}{\sqrt{2m_A K_A}}}{\frac{h}{\sqrt{2m_B K_B}}} = \frac{\sqrt{2m_B K_B}}{\sqrt{2m_A K_A}} = \sqrt{\frac{m_B K_B}{m_A K_A}}$$

Substitute the given values:

$$\frac{\lambda_A}{\lambda_B} = \sqrt{\frac{m_B \cdot \frac{K_A}{8}}{2m_B K_A}} = \sqrt{\frac{m_B K_A}{2m_B K_A \cdot 8}} = \sqrt{\frac{1}{16}} = \frac{1}{4}$$

Thus, the ratio of the de Broglie wavelength of A to that of B is:

Question 20

A coil of inductance 1H and resistance 100Ω is connected to an alternating current source of frequency 50π Hz. What will be the phase difference between the current and voltage?

Options:

A. 90° B. 30° C. 60° D. 45°

Answer: D

Solution:

The phase difference between the current and the voltage in an AC circuit containing resistance and inductance (RL circuit) depends on the values of the resistance (R) and inductive reactance (X_L).

The inductive reactance is given by the formula:

$$X_L = 2\pi fL$$

where:

- f is the frequency of the AC source
- L is the inductance of the coil

Substituting the given values:

$$f = 50\pi \text{ Hz}$$

$$L = 1 \text{ H}$$

We get:

$$X_L = 2\pi (50\pi) \times 1$$

$$X_L = 100 \Omega$$

The phase angle ϕ between the current and the voltage is given by the equation:

$$\tan \phi = \frac{X_L}{R}$$

Given:

$$R = 100 \, \Omega$$

So:

$$\tan \phi = \frac{100}{100} = 1$$

The angle ϕ whose tangent is 1 is 45 degrees:

$$\phi = 45^\circ$$

Thus, the phase difference between the current and voltage is 45 degrees.

The correct answer is Option D: 45°.

Question 21

The current through a conductor is 'a' when the temperature is 'b' when the temperature is 100°C. The current through the conductor at 220°C is

Options:

A. $\frac{5ab}{11-6a}$

B. $\frac{5ab}{6-11b}$

C. $\frac{5ab}{11-6b}$

D. $\frac{11ab}{5-6b}$

Answer: C

Solution:

To find the current through the conductor at 220°C, we need to understand the relationship between temperature and resistance, assuming that the resistance of the conductor increases linearly with temperature. This relationship is given by:

$$R_T = R_0(1 + \alpha T)$$

Where:

- R is the resistance at temperature T .
- R_0 is the resistance at 0°C .
- α is the temperature coefficient of resistance.
- T is the temperature in degrees Celsius.

Since the current I is inversely proportional to the resistance R (Ohm's Law: $I = \frac{V}{R}$), we'll first express the given currents a and b at the corresponding temperatures in terms of resistance:

At 0°C :

$$I_0 = a = \frac{V}{R_0}$$

At 100°C :

$$I_{100} = b = \frac{V}{R_{100}} = \frac{V}{R_0(1+100\alpha)}$$

Dividing the equations for b by the equation for a , we get:

$$\frac{b}{a} = \frac{V/R_{100}}{V/R_0} = \frac{R_0}{R_0(1+100\alpha)} = \frac{1}{1+100\alpha}$$

Solving for α , we get:

$$1+100\alpha = \frac{a}{b}$$

$$100\alpha = \frac{a}{b} - 1$$

$$\alpha = \frac{1}{100} \left(\frac{a}{b} - 1 \right)$$

Now let's determine the current at 220°C :

At 220°C :

$$I_{220} = \frac{V}{R_{220}} = \frac{V}{R_0(1+220\alpha)}$$

Substituting the value of α from above:

$$I_{220} = \frac{V}{R_0 \left(1 + 220 \left(\frac{a}{b} - 1 \right) \right)}$$

$$I_{220} = \frac{V}{R_0 (1 + 2.2 \left(\frac{a}{b} - 1 \right))}$$

$$I_{220} = \frac{V}{R_0 (1 + 2.2 \frac{a}{b} - 2.2)}$$

$$I_{220} = \frac{V}{R_0 \left(\frac{a}{b} - 1.2 \right)}$$

$$I_{220} = \frac{Vb}{R_0 (a - 1.2b)}$$

$$I_{220} = \frac{Vb}{R_0 (2.2a - 1.2b)}$$

Using $I_0 = \frac{V}{R_0}$ from above:

$$I_{220} = \frac{-b/a}{2.2a - 1.2b}$$

$$I_{220} = \frac{-ba}{2.2a - 1.2b}$$

Multiplying numerator and denominator by 5, we get:

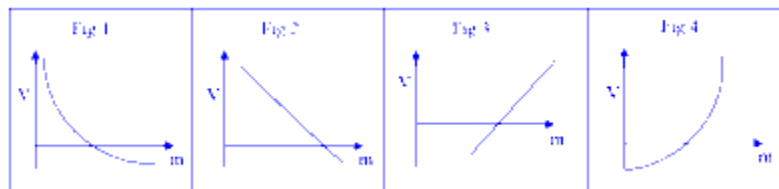
$$I_{220} = \frac{-5ab}{11a - 6b}$$

Therefore, the current through the conductor at 220 Ω is given by Option C:

$$\frac{-5ab}{11a - 6b}$$

Question 22

Which of the following graph shows the variation of velocity with mass for the constant momentum?



Options:

A. Fig 3 B.

Fig 1 C. Fig

2 D. Fig 4

Answer: B

Question 23

For a 30° prism when a ray of light is incident at an angle 60° on one of its faces, the emergent ray passes normal to the other surface. Then the refractive index of the prism is:

Options:

A. $\sqrt{3}$

B. $\frac{\sqrt{3}}{2}$

C. 1.5

D. 1.33

Answer: A

Solution:

To determine the refractive index of the prism, let's analyze the given conditions using Snell's law and the geometry of the prism. The prism has an apex angle of 30° and the incident angle on one of its faces is 60° . The emergent ray is normal to the other surface.

First, let's consider the refraction at the first surface of the prism where light enters. According to Snell's law:

$$n_i \sin(\theta_i) = n_r \sin(\theta_r)$$

where n_i is the refractive index of the medium the light is coming from (which we assume to be air, so $n_i = 1$), θ_i is the angle of incidence (60°), n_r is the refractive index of the prism, and θ_r is the angle of refraction.

We have:

$$\sin(60^\circ) = n \sin(\theta_r)$$

$$\frac{\sqrt{3}}{2} = n \sin(\theta_r)$$

Next, we need to find the relationship between θ_r and the internal angles of the prism. Since the prism angle is 30° and the emergent ray is normal to the surface (meaning the angle of emergence is 0°), we can use the fact that the sum of angles inside the prism should be equal to 90° (since the light travels through the prism and the final deviation angle should cancel out the prism angle). Therefore:

$$\theta_r + \phi = 90^\circ$$

Where ϕ is the internal angle of deviation. Given that $\phi + 0^\circ = 30^\circ$, it means θ_r should equal 30° .

Therefore we have:

$$\sin(30^\circ) = \frac{1}{2}$$

Substituting $\theta_r = 30^\circ$ into Snell's law equation:

$$\frac{\sqrt{3}}{2} = n \cdot \frac{1}{2}$$

Thus, solving for n , we find:

$$n = \sqrt{3}$$

Hence, the refractive index of the prism is:

Option A: $\sqrt{3}$

Question 24

A coil offers a resistance of 20 ohm for a direct current. If we send an alternating current through the same coil, the resistance offered by the coil to the alternating current will be :

Options:

A. 0Ω

B. Greater than

20Ω

C. Less than 20Ω

D. 20Ω

Answer: B

Solution:

A coil typically offers a certain resistance to a direct current (DC), which is also known as its ohmic resistance. In the case of an alternating current (AC), the coil presents additional opposition to the flow of current, which is known as impedance. This impedance is due to both the ohmic resistance and the inductive reactance of the coil. The inductive reactance X_L of a coil in an AC circuit is given by the formula:

$$X_L = 2\pi fL$$

where:

- f is the frequency of the alternating current
- L is the inductance of the coil

The total impedance Z of the coil in an AC circuit, considering both the resistance R and the inductive reactance X_L , is given by the formula:

$$Z = \sqrt{R^2 + X_L^2}$$

Since impedance Z takes into account both ohmic resistance and inductive reactance, the resistance offered by the coil to an alternating current will always be greater than its resistance to a direct current, assuming the inductance L is not zero.

Therefore, the resistance offered by the coil to the alternating current will be:

Option B: Greater than 20Ω

Question 25

A square shaped aluminium coin weighs 0.75 g and its diagonal measures 14 mm. It has equal amounts of positive and negative charges. Suppose those equal charges were concentrated in two charges (+ Q and $-Q$) that are separated by a distance equal to the side of the coin, the dipole moment of the dipole is

Options:

- A. 34.8 Cm
- B. 3.48 Cm
- C. 3480 Cm
- D. 348 Cm

Answer: D

Question 26

If the earth has a mass nine times and radius four times that of planet X, the ratio of the maximum speed required by a rocket to pull out of the gravitational force of planet X to that of the earth is

Options:

- A. $\frac{2}{3}$
- B. $\frac{9}{4}$
- C. $\frac{3}{2}$

D. $\frac{4}{9}$

Answer: A

Solution:

To find the ratio of the maximum speed required by a rocket to escape the gravitational force of planet of Earth, we must consider the escape velocity formula:

v_x to that

$$v_e = \sqrt{\frac{2GM}{R}}$$

where:

- v_e is the escape velocity
- G is the gravitational constant
- M is the mass of the planet
- R is the radius of the planet

Given:

- The mass of Earth (M_{Earth}) is nine times the mass of planet X (M_x),
- The radius of Earth (R_{Earth}) is four times the radius of planet X (R_x).

So, we have:

$$M_{\text{Earth}} = 9M_x$$

$$R_{\text{Earth}} = 4R_x$$

The escape velocity for planet X is:

$$v_{e,x} = \sqrt{\frac{2GM_x}{R_x}}$$

The escape velocity for Earth is:

$$v_{e,\text{Earth}} = \sqrt{\frac{2GM_{\text{Earth}}}{R_{\text{Earth}}}}$$

Substitute $M_{\text{Earth}} = 9M_x$ and $R_{\text{Earth}} = 4R_x$:

$$v_{e,\text{Earth}} = \sqrt{\frac{2G(9M_x)}{4R_x}} = \sqrt{\frac{18GM_x}{4R_x}} = \sqrt{9 \cdot \frac{2GM_x}{R_x}} = 3 \sqrt{\frac{2GM_x}{R_x}}$$

However, note that:

$$v_{e,x} = \sqrt{\frac{2GM_x}{R_x}}$$

So, the ratio of the escape velocity of planet X to Earth is:

$$\frac{v_{e,x}}{v_{e,\text{Earth}}} = \frac{\sqrt{\frac{2GM_x}{R_x}}}{3 \sqrt{\frac{2GM_x}{R_x}}} = \frac{1}{3}$$

$$\begin{aligned}
 &= \frac{\sqrt{\frac{2GM_X}{R_X}}}{3\sqrt{\frac{GM_X}{R_X}}} \\
 &= \frac{1}{\sqrt{3}} \cdot \frac{\sqrt{2GM_X}}{\sqrt{GM_X}} \cdot \frac{\sqrt{R_X}}{\sqrt{R_X}} \\
 &= \frac{1}{\sqrt{3}} \sqrt{2} \\
 &= \frac{\sqrt{2}}{\sqrt{3}}
 \end{aligned}$$

Therefore, the ratio of the maximum speed required by a rocket to escape the gravitational force of planet X to that of Earth is:

$$\frac{\sqrt{2}}{\sqrt{3}}$$

Question 27

Two similar coils A and B of radius ' r ' and number of turns ' N ' each are placed concentrically with their planes perpendicular to each other. If I and $2I$ are the respective currents passing through the coils then the net magnetic induction at the centre of the coils will be:

Options:

A.

$$\sqrt{3}(\mu_0 \frac{NI}{2r})$$

B. $\sqrt{5}(\mu_0 \frac{NI}{2r})$

C. $5\mu_0 \frac{NI}{2r}$

D. $3\mu_0 \frac{NI}{r}$

Answer: B

Solution:

To find the net magnetic induction at the center of the two coils, we can start by calculating the magnetic field produced by each coil separately.

For a coil with radius r and N turns carrying a current I , the magnetic field at the center of the coil is given by

$$B = \mu_0 \frac{NI}{2r}$$

Given that the first coil A carries a current I and the second coil B carries a current $\frac{I}{2}$, the magnetic fields due to each coil at the center can be calculated as:

For coil A:

$$B_A = \mu_0 \frac{NI}{2r}$$

For coil B:

$$B_B = \mu_0 \frac{N(2I)}{2r} = \mu_0 \frac{2NI}{2r} = \mu_0 \frac{NI}{r}$$

Since the coils are placed concentrically with their planes perpendicular to each other, the magnetic fields at the center will be perpendicular to each other. Therefore, the net magnetic induction at the center can be found by taking the vector sum of the two magnetic fields.

The net magnetic induction B can thus be calculated using the Pythagorean theorem:

$$B = \sqrt{B_A^2 + B_B^2}$$

Substituting the values of B_A and B_B , we get:

$$B = \sqrt{\left(\mu_0 \frac{NI}{2r}\right)^2 + \left(\mu_0 \frac{NI}{r}\right)^2}$$

Simplifying inside the square root:

$$B = \sqrt{\left(\mu_0 \frac{NI}{2r}\right)^2 + \left(\mu_0 \frac{NI}{r}\right)^2}$$

$$B = \sqrt{\left(\mu_0 \frac{NI}{2r}\right)^2 + 2 \cdot \mu_0 \frac{NI}{2r}}$$

$$B = \sqrt{\left(\mu_0 \frac{NI}{2r}\right)^2 + \left(\mu_0 \frac{2NI}{2r}\right)^2}$$

$$B = \sqrt{\left(\mu_0 \frac{NI}{2r}\right)^2 + 4\left(\mu_0 \frac{NI}{2r}\right)^2}$$

$$B = \sqrt{1\left(\mu_0 \frac{NI}{2r}\right)^2 + 4\left(\mu_0 \frac{NI}{2r}\right)^2}$$

$$B = \sqrt{5\left(\mu_0 \frac{NI}{2r}\right)^2}$$

$$B = \sqrt{5} \left(\mu_0 \frac{NI}{2r}\right)$$

Hence, the correct answer is:

Option B: —

$$\sqrt{5} \left(\mu_0 \frac{NI}{2r}\right)$$

Question 28

An ideal diode is connected in series with a capacitor. The free ends of the capacitor and the diode are connected across a 220 V ac source. Now the potential difference across the capacitor is :

Options:

A. 110 V

B. 311 V

C. $2\sqrt{110}$

D. $\sqrt{220 \text{ V}}$

Answer: B

Solution:

To analyze the potential difference across the capacitor, let's first understand the behavior of the circuit elements involved. An ideal diode allows current to flow only in one direction, blocking current in the reverse direction. A capacitor, on the other hand, stores energy in the form of an electric field and can charge and discharge based on the applied voltage.

The ac source has a voltage of 220 V. The given voltage is typically an RMS (Root Mean Square) value, which is a form of averaging used for ac voltages. The peak voltage (V_{peak}) of the ac source can be calculated using the relationship:

$$V_{\text{peak}} = V_{\text{RMS}} \times \sqrt{2}$$

Substituting the given RMS value, we have:

$$V_{\text{peak}} = 220 \text{ V} \times \sqrt{2}$$

$$V_{\text{peak}} \approx 220 \text{ V} \times 1.414$$

$$V_{\text{peak}} \approx 311 \text{ V}$$

Since the diode is ideal, during the positive half cycle of the ac voltage, the diode will conduct and allow current to flow, charging the capacitor to the peak voltage of the ac source, which is 311 V.

During the negative half cycle, the diode will be in reverse bias and will not conduct, thus isolating the capacitor and maintaining its charge. Therefore, the potential difference across the capacitor will be equal to the peak voltage of the ac source.

Hence, the potential difference across the capacitor is:

311 V

So, the correct answer is:

Option B

311 V

Question 29

Which of the following statement is true regarding the centre of mass of a system?

Options:

- A. The centre of mass depends on the size and shape but does not depend on the distribution of mass of the body.
- B. The centre of mass depends on the coordinate system.
- C. The centre of mass of a system depends on the size and shape of the body but independent of the co-ordinate system
- D. The centre of mass of a body always lies inside the body.

Answer: C

Question 30

A ray of light travelling through a medium of refractive index 5

4 is

incident on a glass of refractive index $\frac{3}{2}$. Find the angle of refraction in the glass, if the angle of incidence at the given medium - glass interface is 30° .

Options:

A. $\sin^{-1} \left(\frac{1}{2} \right)$

B. $\sin^{-1} \left(\frac{1}{3} \right)$

C. $\sin^{-1} \left(\frac{5}{12} \right)$

D. $\sin^{-1} \left(\frac{6}{5} \right)$

Answer: C

Solution:

To find the angle of refraction when light travels from one medium to another, we use Snell's law. Snell's law is given by:

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

Where:

$$n_1 = \text{refractive index of the first medium} = \frac{5}{4}$$

$$n_2 = \text{refractive index of the second medium (glass)} = \frac{3}{2}$$

$$\theta_1 = \text{angle of incidence} = 30^\circ$$

$$\theta_2 = \text{angle of refraction}$$

$$\theta$$

Now, substituting the known values into Snell's law:

$$\frac{5}{4} \sin 30^\circ = \frac{3}{2} \sin \theta_2$$

We know that $\sin 30^\circ = \frac{1}{2}$, so we substitute this into the equation:

$$\frac{5}{4} \cdot \frac{1}{2} = \frac{3}{2} \sin \theta_2$$

$$\frac{5}{8} = \frac{3}{2} \sin \theta_2$$

To solve for $\sin \theta_2$, we rearrange the equation:

$$\sin \theta_2 = \frac{5}{8} \cdot \frac{2}{3}$$

$$\sin \theta_2 = \frac{10}{24}$$

$$\sin \theta_2 = \frac{5}{12}$$

Therefore, the angle of refraction (in terms of sine inverse) is:

$$\theta_2 = \sin^{-1} \left(\frac{5}{12} \right)$$

So, the correct answer is Option C: $\sin^{-1} \left(\frac{5}{12} \right)$

Question 31

The ratio of the radii of the nucleus of two element $_X$ and $_Y$ having the mass numbers 232 and 29 is:

Options:

A. 4 : 1 B. 1 : 4 C. 1 : 2 D. 2 : 1

Answer: D

Solution:

The radius of a nucleus is related to the mass number (A) by the formula:

$$R = R_0 \cdot A^{1/3}$$

where:

R_0 is a constant (approximately 1.2×10^{-15} meters), and

A is the mass number.

Let's denote the radii of the nuclei of elements X and Y by $R(X)$ and $R(Y)$ respectively. Given the mass numbers:

For element X: $A(X)=232$

For element Y: $A(Y)=29$

The radii are then:

$$R(X) = R_0 \cdot (232)^{1/3}$$

$$R(Y) = R_0 \cdot (29)^{1/3}$$

We are asked to find the ratio of these radii:

$$\frac{R(X)}{R(Y)} = \frac{R_0 \cdot (232)^{1/3}}{R_0 \cdot (29)^{1/3}} = \left(\frac{232}{29} \right)^{1/3}$$

Calculating the cube root of the ratio:

$$\frac{232}{29} \approx 8$$

$$8^{1/3} = 2$$

Hence, the ratio of the radii of the nuclei of elements X and Y is:

2 : 1

The correct option is Option D: 2 : 1.

Question 32

When light wave passes from a medium of refractive index ' μ ' to another medium of refractive index ' 2μ ' the phase change occurs to the light is :

Options:

A. 180° B. 90° C. 60° D. zero

Answer: D

Solution:

The correct answer is Option D: zero. Here's why:

Phase change upon reflection occurs when light goes from a medium with a lower refractive index to a medium with a higher refractive index. This is because the reflected wave undergoes a 180° phase shift. However, in this case, the light is moving from a medium with a lower refractive index (μ) to a medium with a higher refractive index (2μ). Since there's no reflection involved in this scenario, there is no phase change.

Here's a breakdown of why phase change occurs during reflection:

When light waves travel from one medium to another, they undergo a change in speed due to the different refractive indices. At the boundary between the two media, a portion of the light is reflected back into the original medium. When the light is reflected from a denser medium (higher refractive index), the reflected wave undergoes a phase shift of 180° . This is because the electric field vector of the reflected wave is inverted.

In our case, the light is transmitted from the first medium to the second, not reflected back. Therefore, there is no phase change.

Question 33

On increasing the temperature of a conductor, its resistance increases because

Options:

A. Electron density decreases B. Relaxation time increases C. Number of collisions between electrons decreases D. Relaxation time decreases

Answer: D

Solution:

Let's analyze why the resistance of a conductor increases with the increase in temperature. A conductor has free electrons that move through the material, and this movement constitutes electric current.

The resistance of a conductor is determined by how easily these electrons can move through the material. The key factors influencing this movement are electron density, relaxation time, and the collision frequency of electrons with atoms.

Now, let's consider each of the options:

Option A: Electron density decreases

This is incorrect because the electron density in a conductor is not significantly affected by temperature. The number of free electrons available for conduction stays relatively constant.

Option B: Relaxation time increases

This is also incorrect. Relaxation time refers to the average time between collisions of electrons. Generally, with an increase in temperature, the atoms in the conductor vibrate more vigorously and electrons experience more frequent collisions, thereby decreasing the relaxation time.

Option C: Number of collisions between electrons decreases

This is incorrect. With an increase in temperature, the number of collisions between electrons actually increases because the thermal agitation of atoms in the conductor becomes more intense.

Option D: Relaxation time decreases

This is correct. The relaxation time (τ) is the average time interval between successive collisions of an electron. As the temperature increases, the thermal energy causes more vigorous vibrations of the atoms in the lattice

structure of the conductor. This leads to an increase in the collision rate of electrons with these vibrating atoms, which results in a decrease in relaxation time.

The resistance R of a conductor is given by the formula:

$$R = \frac{m}{ne^2\tau}$$

where:

m = mass of an electron

n = number of free electrons per unit volume

e = charge of an electron

τ = relaxation time

From the above equation, you can see that resistance R is inversely proportional to the relaxation time τ .

Therefore, as the relaxation time decreases with an increase in temperature, the resistance increases. Hence, the correct answer is:

Option D: Relaxation time decreases

Question 34

The difference in energy levels of an electron at two excited levels is 13.75 eV. If it makes a transition from the higher energy level to the lower energy level then what will be the wave length of the emitted radiation? [given

$$h = 6.6 \times 10^{-34} \text{ m}^2 \text{ kg s}^{-1}; c = 3 \times 10^8 \text{ ms}^{-1}; 1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}]$$

Options:

- A. 900 nm
- B. 90 A
- C. 9000 nm
- D. 900 ° A

Answer: D

Question 35

A string of length 25 cm and mass 10–3 kg is clamped at its ends. The tension in the string is 2.5 N. The identical wave pulses are generated at one end and at regular interval of time, Δt . The minimum value of Δt , so that a constructive interference takes place between successive pulses is

Options:

A. 0.2 s B. 1 s C. 40 ms D. 20 ms

Answer: D

Solution:

To solve for the minimum value of Δt that allows for constructive interference between successive pulses, we must determine the time it takes for a wave pulse to travel from one end of the string to the other and back. This time is essentially the period for which constructive interference will occur.

First, we find the wave speed, v , on the string. The wave speed is given by the formula:

$$v = \sqrt{\frac{T}{\mu}}$$

where:

1. T is the tension in the string, which is given as 2.5 N.
2. μ is the linear mass density of the string.

The linear mass density μ can be calculated using the formula:

$$\mu = \frac{m}{L}$$

Where:

1. m is the mass of the string, given as 10–3 kg
2. L is the length of the string, given as 25 cm (which we convert to meters as 0.25 m).

Thus,

$$\mu = \frac{10^{-3} \text{ kg}}{0.25 \text{ m}} = 4 \times 10^{-3} \text{ kg/m}$$

Now, substituting μ and T back into the wave speed formula:

$$v = \sqrt{\frac{2.5 \text{ N}}{4 \times 10^{-3} \text{ kg/m}}} = \sqrt{625 \text{ m}^2/\text{s}^2} = 25 \text{ m/s}$$

Now that we have the wave speed, we can calculate the time it takes for the wave pulse to travel the length of the string and back (i.e., a round trip). The total distance for a round trip is $2L$, so the time interval Δt is given by:

$$\Delta t = 2 \frac{L}{v}$$

Substituting the given values:

$$\Delta t = \frac{2 \times 0.25 \text{ m}}{25 \text{ m/s}} = \frac{0.5 \text{ m}}{25 \text{ m/s}} = 0.02 \text{ s} = 20 \text{ ms}$$

Thus, the minimum value of Δt for constructive interference between successive pulses is:

Option D: 20 ms

Question 36

A cubical box of side 1 m contains Boron gas at a pressure of 100 Nm^{-2} . During an observation time of 1 second, an atom travelling with the rms speed parallel to one of the edges of the cube, was found to make 500 hits with a particular wall, without any collision with other atoms. The total mass of gas in the box in gram is

Options:

A. 30

B. 0.3

C. 3

D. 0.03

Answer: B

Solution:

To determine the total mass of the gas in the box, we first need to understand the given problem and apply the principles of kinetic theory of gases. Let's summarize the given data:

- Side length of the cubical box, $L=1$ m
- Pressure of the gas, $P=100 \text{ Nm}^{-2}$
- Observation time, $t=1$ s
- Number of hits on the wall, $n=500$

We are given that the atom travels with the root mean square (rms) speed (denoted by v_{rms}) parallel to one edge of the cube, and makes 500 hits on the wall in 1 second. From this, we can find the v_{rms} as follows:

Each hit corresponds to the atom travelling across the side of the cube and bouncing back. The distance travelled between two consecutive hits is $2L$, as the atom goes to the wall and returns. Therefore, the total distance travelled in 1 second is:

$$500 \times 2L = 500 \times 2 \times 1 = 1000 \quad \text{m}$$

So, the rms speed v_{rms} is:

$$v_{rms} = \frac{1000 \text{ m}}{1 \text{ s}} = 1000 \text{ m/s}$$

Now, using the formula from the kinetic theory of gases for pressure:

$$P = \frac{1}{3} \rho v_{rms}^2$$

where ρ is the density of the gas. We can express density ρ as:

$$\rho = \frac{m}{V}$$

Here, m is the mass of the gas and V is the volume of the box. For a cubical box, $V = L^3$, so:

$$V = 1^3 \text{ m}^3 = 1 \text{ m}^3$$

Substituting the values into the pressure equation:

$$100 \text{ Nm}^{-2} = \frac{1}{3} \left(\frac{m}{1} \right) (1000)^2$$

Simplifying, we get:

$$100 = \frac{1}{3} m \times 1000000$$

$$100 = \frac{1000000}{3} m$$

$$m = \frac{100 \times 3}{1000000} = 0.0003 \text{ kg}$$

m

Converting this mass to grams:

$$m = 0.0003 \text{ kg} \times 1000 \frac{\text{g}}{\text{kg}} = 0.3 \text{ g}$$

Therefore, the total mass of the gas in the box is:

Option B: 0.3 grams

Question 37

Around the central part of an air cored solenoid of length 20 cm and area of cross section $1.4 \times 10^{-3} \text{ m}^2$ and 3000 turns, another coil of 250 turns is closely wound. A current 2 A in the solenoid is reversed in 0.2 s, then the induced emf produced is

Options:

A. $1.32 \times 10^{-1} \text{ V}$

B. $4 \times 10^{-1} \text{ V}$

C. $1.16 \times 10^{-1} \text{ V}$

D. $8 \times 10^{-2} \text{ V}$

Answer: A

Solution:

The magnetic field inside the solenoid is given by

$$B = \mu_0 n I = \mu_0 \frac{N}{L} I$$

where, N is the number of turns, L is the length of the solenoid, I is the current flowing through the solenoid, and μ_0 is the permeability of free space.

The magnetic flux through the smaller coil is given by

$$\phi = BA = \mu_0 \frac{N}{L} I A$$

where A is the area of the smaller coil.

The induced emf in the smaller coil is given by Faraday's law of electromagnetic induction as

$$e = - \frac{d\phi}{dt}$$

Substituting the value of ϕ in the above equation, we get

$$e = - \frac{d}{dt} (\mu_0 \frac{N}{L} I A) = - \mu_0 \frac{N}{L} A \frac{dI}{dt}$$

Given that the current is reversed in 0.2 s the rate of change of current is

$$\frac{dI}{dt} = \frac{2 - (-2)}{0.2} = 20 \text{ A/s}$$

Substituting the values, we get

$$e = -4\pi \times 10^{-7} \times \frac{3000}{0.2} \times 1.4 \times 10^{-3} \times 20 = 1.32 \times 10^{-1} \text{ V}$$

Therefore, the induced emf produced is $1.32 \times 10^{-1} \text{ V}$.

Question 38

A circular coil of radius 0.1 m is placed in the X–Y plane and a current 2 A is passed through the coil in the clockwise direction when looking from above. Find the magnetic dipole moment of the current loop

Options:

- A. $0.02\pi \text{ Am}^2$ in the -ve X - direction
- B. $0.02\pi \text{ Am}^2$ in the -ve Z– direction
- C. $0.02\pi \text{ Am}^2$ in the + ve Y– direction
- D. $0.02\pi \text{ Am}^2$ in the + ve Z– direction

Answer: B

Solution:

To determine the magnetic dipole moment of the current loop, we use the formula:

$$\mu = I \cdot A$$

where:

μ is the magnetic dipole moment,

I is the current, and

A is the area of the coil.

Given:

$$I = 2 \text{ A}$$

Radius of the coil, $r = 0.1 \text{ m}$

The area of the coil, A , is given by:

$$A = \pi r^2$$

Substituting the value of the radius:

$$A = \pi(0.1)^2$$

$$A = \pi \times 0.01$$

$$A = 0.01\pi \text{ m}^2$$

Now, we calculate the magnetic dipole moment:

$$\mu = I \cdot A$$

$$\mu = 2 \text{ A} \cdot 0.01\pi \text{ m}^2$$

$$\mu = 0.02 \text{ A} \pi \text{ m}^2$$

The direction of the magnetic dipole moment is given by the right-hand rule. Since the current is flowing in a clockwise direction when looking from above (positive Z-direction), the magnetic dipole moment points in the negative Z-direction.

Thus, the magnetic dipole moment of the current loop is:

$0.02\pi \text{ Am}^2$ in the negative Z-direction.

Therefore, the correct option is:

Option B: $0.02\pi \text{ Am}^2$ in the -ve Z- direction

Question 39

A body is moving along a circular path of radius 'r' with a frequency of revolution numerically equal to the radius of the circular path.

What is the acceleration of the body if radius of the path is $(\frac{\pi}{5})\text{m}$?

Options:

A. $100\pi \text{ ms}^{-2}$

B. $500\pi \text{ ms}^{-2}$

C. $25\pi \text{ ms}^{-2}$

D. $(\frac{500}{\pi})\text{ms}^{-2}$

Answer: D

Solution:

First, let's analyze the given information. The radius of the circular path, r , is given as 5 meters. The frequency of revolution, f , is numerically equal to the radius, so $f = r = 5 \pi \text{ Hz}$.

The acceleration we need to find is the centripetal acceleration, which is given by the formula:

$$a = \omega^2 r$$

Here, ω (omega) is the angular velocity, which can be calculated from the frequency f using the relationship:

$$\omega = 2\pi f$$

Substitute $f = 5\pi$ into the equation for ω :

$$\omega = 2\pi (5\pi) = 10\pi \text{ rad/s}$$

Now, substitute $\omega = 10\pi \text{ rad/s}$ and $r = 5 \text{ meters}$ into the centripetal acceleration formula:

$$a = \omega^2 r = (10\pi)^2 (5)$$

Thus, the acceleration a is:

$$a = 100 (\pi) = \frac{500}{\pi} \text{ m/s}^2$$

Therefore, the correct option is:

Option D: $(\frac{500}{\pi}) \text{ ms}^{-2}$

Question 40

Which of the given dimensional formula represents heat capacity

Options:

A. $\text{ML}^2 \text{T}^{-2} \text{K}^{-1}$
[]

B. $\text{ML}^2 \text{T}^{-1} \text{K}^{-1}$
[]

C. $\text{ML}^2 \text{T}^{-2} \text{K}^{-2}$
[]

D. $\text{MLT}^{-2} \text{K}^{-1}$
[]

Answer: A

Solution:

To determine which dimensional formula represents heat capacity, we need to analyze the quantities involved in the definition of heat capacity. Heat capacity, symbolized as C , is the amount of heat energy required to raise the temperature of a substance by one unit of temperature. Mathematically, it can be expressed as:

$$C = \frac{Q}{\Delta T}$$

where Q is the heat added (energy) and ΔT is the change in temperature.

Next, we need to express the dimensional formulas of the quantities involved:

1. Heat energy Q has the dimensional formula of energy, which is:

$$[Q] = [ML^2T^{-2}]$$

2. Temperature ΔT has the dimensional formula of:

$$[\Delta T] = [K]$$

Using these, we find the dimensional formula for heat capacity C :

$$[C] = \frac{[Q]}{[\Delta T]} = \frac{[ML^2T^{-2}]}{[K]} = [ML^2T^{-2}K^{-1}]$$

Therefore, the dimensional formula for heat capacity is:

$$[ML^2T^{-2}K^{-1}]$$

Comparing this with the options given, the correct answer is Option A:

$$[ML^2T^{-2}K^{-1}]$$

Question 41

If potential (in volt) in a region is expressed as $V(x,y,z)=6xy-y+2yz$, the electric field (in NC^{-1}) at point $(1,0,1)$ is

Options:

A. $-7j$

B. $+7j$

C. $-6\mathbf{i} + 7\mathbf{j}$

D. $6\mathbf{i} - 7\mathbf{j}$

Answer: A

Solution:

To determine the electric field from the given potential function, we need to use the relationship between electric field \mathbf{E} and electric potential V . The electric field is the negative gradient of the potential:

$$\mathbf{E} = -\nabla V$$

Given the potential function $V(x, y, z) = 6xy - y + 2yz$, we need to compute the partial derivatives of V with respect to x , y , and z .

First, calculate the partial derivative with respect to x :

$$\frac{\partial V}{\partial x} = \frac{\partial}{\partial x}(6xy - y + 2yz) = 6y$$

Next, calculate the partial derivative with respect to y :

$$\frac{\partial V}{\partial y} = \frac{\partial}{\partial y}(6xy - y + 2yz) = 6x - 1 + 2z$$

Finally, calculate the partial derivative with respect to z :

$$\frac{\partial V}{\partial z} = \frac{\partial}{\partial z}(6xy - y + 2yz) = 2y$$

Now, the components of the electric field are:

$$E_x = -\frac{\partial V}{\partial x} = -6y$$

$$E_y = -\frac{\partial V}{\partial y} = -(6x - 1 + 2z)$$

$$E_z = -\frac{\partial V}{\partial z} = -2y$$

We are asked to find the electric field at the point $(1, 0, 1)$

Substitute $x = 1$, $y = 0$, and $z = 1$ into the components of the electric field:

$$E_x(1, 0, 1) = -6(0) = 0$$

$$E_y(1, 0, 1) = -(6(1) - 1 + 2(1)) = -(6 - 1 + 2) = -(7) = -7$$

$$E_z(1, 0, 1) = -2(0) = 0$$

Therefore, the electric field at the point $(1, 0, 1)$ is:

$$\mathbf{E} = 0\mathbf{i} - 7\mathbf{j} + 0\mathbf{k} = -7\mathbf{j}$$

Hence, the correct option is:

Question 42

The closest approach of an alpha particle when it make a head on collision with a gold nucleus is 10×10^{-14} m, then the kinetic energy of the alpha particle is :

Options:

A. 3640 J

B. 3.64 J

C. 3.64×10^{-16} J

D. 3.64×10^{-13} J

Answer: D

Solution:

To determine the kinetic energy of the alpha particle when it makes a head-on collision with a gold nucleus, we can use the concept of electrostatic potential energy at the closest approach. The kinetic energy of the alpha particle will be completely converted into electrostatic potential energy at the point of closest approach.

The formula for the electrostatic potential energy between two charges is given by:

$$U = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r}$$

where:

- q_1 and q_2 are the charges of the alpha particle and gold nucleus, respectively
- r is the distance of closest approach
- ϵ_0 is the permittivity of free space, which is approximately 8.85×10^{-12} F/m

For an alpha particle, q_1 is the charge of 2 protons, so:

$$q_1 = 2e = 2 \times 1.6 \times 10^{-19} \text{ C}$$

For a gold nucleus (with atomic number 79), q_2 is the charge of 79 protons, so:

$$q_2 = 79e = 79 \times 1.6 \times 10^{-19} \text{ C}$$

The distance of closest approach, r , is given as:

$$r = 10 \times 10^{-14} \text{ m}$$

Now, substituting these values into the formula for electrostatic potential energy:

$$U = \frac{1}{4\pi\epsilon_0} \frac{(2 \times 1.6 \times 10^{-19})(79 \times 1.6 \times 10^{-19})}{10 \times 10^{-14}}$$

Simplifying the equation:

$$U = \frac{9 \times 10^9}{10 \times 10^{-14}} (2 \times 79 \times 1.62 \times 10^{-38})$$

Calculating each component:

$$U = \frac{9 \times 10^9}{10^{-13}} (2 \times 79 \times 2.56 \times 10^{-38})$$

Or:

$$U = 9 \times 1022 \times 404.48 \times 10^{-10}$$

Simplifying further:

$$U = 3.64 \times 10^{-13} \text{ J}$$

Therefore, the kinetic energy of the alpha particle is:

Option D: $3.64 \times 10^{-13} \text{ J}$

Question 43

A one kg block of ice at -1.5°C falls from a height of 1.5 km and is found melting. The amount of ice melted due to fall, if 60% energy is converted into heat is (Specific heat capacity of ice is $0.5 \text{ cal g}^{-1} \text{ }^\circ\text{C}^{-1}$, Latent heat of fusion of ice $= 80 \text{ cal g}^{-1}$)

Options:

A. 1.69 g B. 10 g C. 16.9 g D. 17.9 g

Answer: C

Question 44

64 rain drops of the same radius are falling through air with a steady velocity of 0.5 cm s^{-1} . If the drops coalesce, the terminal velocity would be

Options:

- A. 1.25 cm s^{-1}
- B. 0.08 ms^{-1}
- C. 0.8 ms^{-1}
- D. 1.25 ms^{-1}

Answer: B

Solution:

To solve this problem, let's start by understanding how the terminal velocity of a falling drop depends on its radius. The terminal velocity (v_t) of a spherical drop falling under gravity in a viscous medium is given by:

$$v_t \propto r^2$$

where r is the radius of the drop. Here, we are given that 64 drops of the same radius coalesce to form a single larger drop. To find the radius of the new larger drop, we use the volume conservation principle. The volume of a sphere is given by:

$$V = \frac{4}{3}\pi r^3$$

If 64 small drops, each with radius r , coalesce to form one larger drop, the volume of the larger drop will be 64 times the volume of one small drop. Therefore:

$$\frac{4}{3}\pi (r_{\text{large}})^3 = 64 \cdot \frac{4}{3}\pi r^3$$

From this equation, we can solve for the radius of the larger drop:

$$(r_{\text{large}})^3 = 64r^3$$

$$r_{\text{large}} = \sqrt[3]{64} \cdot r$$

$$r_{\text{large}} = 4r$$

So, the radius of the larger drop is 4 times the radius of one of the smaller drops. Since terminal velocity is proportional to the square of the radius, we get:

$$v^{\text{large}} \propto (r^{\text{large}})^2 = (4r)^2 = 16r^2$$

Therefore, the terminal velocity of the larger drop is 16 times the terminal velocity of one of the smaller drops. Given that the terminal velocity of the smaller drop is 0.5 cm/s, we have:

$$v^{\text{large}} = 16 \cdot 0.5 \text{ cm/s}$$

$$v^{\text{large}} = 8 \text{ cm/s}$$

We need to convert this to m/s as all provided options except A are in meters per second:

$$v^{\text{large}} = 8 \text{ cm/s} \times \frac{1 \text{ m}}{100 \text{ cm}}$$

$$v^{\text{large}} = 0.08 \text{ m/s}$$

Therefore, the correct answer is:

Option B 0.08 ms⁻¹

Question 45

The capacitance of a parallel plate capacitor is 400 pF. It is connected to an ac source of 100 V having an angular frequency 100 rad s⁻¹. If the rms value of the current is 4 μA, the displacement current is:

Options:

A. 4 × 10

B. 0.4 μA C. 4 μA

D. 4 A

Answer: C

Solution:

To determine the displacement current for a parallel plate capacitor connected to an AC source, we utilize the relationship between the capacitor's current, the voltage, and the given angular frequency.

The capacitive reactance, X_C , of the capacitor can be calculated using the formula:

$$X_C = \frac{1}{\omega C}$$

where:

ω (omega) = angular frequency = 100 rad s^{-1}

C = capacitance = $400 \text{ pF} = 400 \times 10^{-12} \text{ F}$

Substituting the given values:

$$X_C = \frac{1}{100 \text{ rad s}^{-1} \times 400 \times 10^{-12} \text{ F}}$$

$$X_C = \frac{1}{(100 \times 400) \times 10^{-12}}$$

$$X_C = \frac{1}{40000 \times 10^{-12}}$$

$$X_C = \frac{1}{4 \times 10^{-8}}$$

$$X_C = 2.5 \times 10^7 \Omega$$

Next, we need to find the RMS current. For a capacitor in an AC circuit, the RMS voltage, V_{rms} , and the RMS current, I_{rms} , are related by:

$$I_{\text{rms}} = \frac{V_{\text{rms}}}{X_C}$$

Given:

$$V_{\text{rms}} = 100 \text{ V}$$

Substituting the values:

$$I_{\text{rms}} = \frac{100 \text{ V}}{2.5 \times 10^7 \Omega}$$

$$I_{\text{rms}} = 4 \mu\text{A}$$

This matches the given value of the RMS current. The displacement current in an AC circuit is equivalent to the RMS current of the capacitor. Therefore, the displacement current is:

$$\text{Displacement current} = 4 \mu\text{A}$$

The correct answer is therefore:

Option C: $4 \mu\text{A}$

Question 46

Though Sn and Si are 4th group elements, Sn is a metal while Si is a semiconductor because
Options:

A. Sn has more electrons than Si

B. The energy gap of Sn is zero volt while that of

C. The energy gap of Sn is 1.1 eV volt while that of Si is 0.07 V

D. Sn has more holes than Si

Answer: B

Solution:

The correct option is:

Option B: The energy gap of Sn is zero volt while that of Si is 0.07 V

Explanation:

Both Sn (tin) and Si (silicon) belong to the 14th group of the periodic table, and they share some common properties. However, the key difference explaining why Sn behaves as a metal while Si behaves as a semiconductor lies in their energy band structure.

In metals, the valence band and conduction band overlap, which means there is no energy gap (E_g) between them. This allows electrons to move freely within the material, contributing to high electrical conductivity.

In semiconductors, there is a small energy gap between the valence band and the conduction band. For silicon, this energy gap is approximately 0.07 eV. This small but significant gap means that at room temperature, some electrons can gain enough thermal energy to jump from the valence band to the conduction band, allowing moderate electrical conductivity that can be manipulated through doping and other methods.

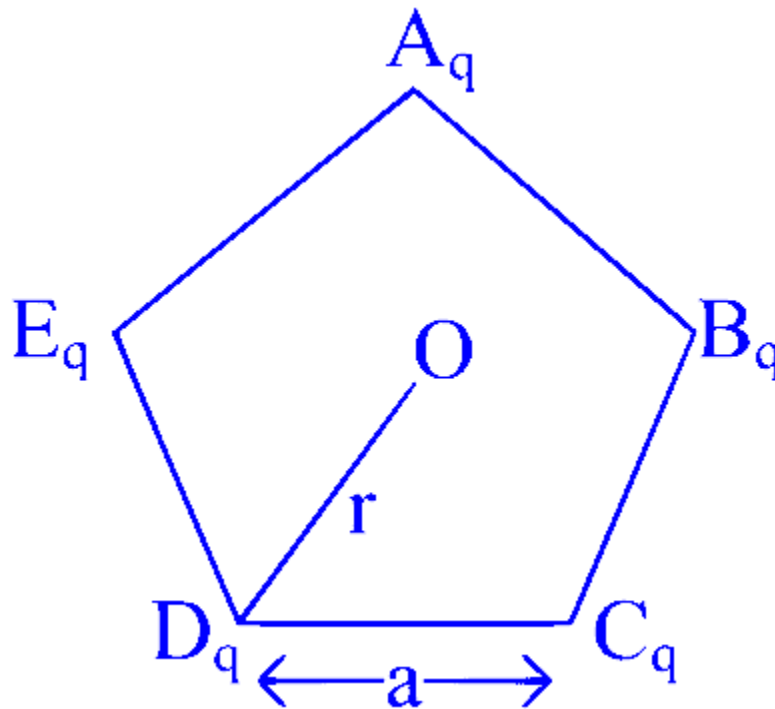
For tin, the energy gap is essentially zero because the valence and conduction bands overlap, which leads to metallic behavior with high electrical conductivity.

Thus, the primary reason why Sn is a metal and Si is a semiconductor is due to the difference in their energy gaps. The energy gap of Sn is effectively zero, while Si has a small but finite energy gap of 0.07 eV.

Question 47

Five charges, ' q ' each are placed at the comers of a regular pentagon of side ' α ' as shown in figure. First, charge from 'A' is removed with

other charges intact, then charge at 'A' is replaced with an equal opposite charge. The ratio of magnitudes of electric fields at O, without charge at A and that with equal and opposite charge at A is



Options:

A. 4 : 1 B. 2 : 1 C. 1 : 4 D. 1 : 2

Answer: D

Question 48

Two circular coils of radius ' a ' and ' $2a$ ' are placed coaxially at a distance ' x ' and ' $2x$ ' respectively from the origin along the X-axis. If their planes are parallel to each other and perpendicular to the X-axis and both carry the same current in the same direction, then the

ratio of the magnetic field induction at the origin due to the smaller coil to that of the bigger one is:

Options:

A. 2 : 1 B. 1 : 1 C. 1 : 4 D. 1 : 2

Answer: A

Solution:

To determine the ratio of the magnetic field induction at the origin due to the smaller coil to that of the bigger one, we need to use the formula for the magnetic field along the axis of a circular coil carrying current. This is given by:

$$B = \frac{\mu_0 I a^2}{2(x^2 + a^2)^{3/2}}$$

where:

- B is the magnetic field at a distance x from the coil along its axis.
- μ_0 is the permeability of free space.
- I is the current in the coil.
- a is the radius of the coil.
- x is the distance from the coil to the point where the field is being calculated.

For the smaller coil (radius a and distance x):

$$B_1 = \frac{\mu_0 I a^2}{2(x^2 + a^2)^{3/2}}$$

For the larger coil (radius $2a$ and distance $2x$):

$$B_2 = \frac{\mu_0 I (2a)^2}{2[(2x)^2 + (2a)^2]^{3/2}} = \frac{\mu_0 I 4a^2}{2[4x^2 + 4a^2]^{3/2}} = \frac{\mu_0 I 4a^2}{2[4(x^2 + a^2)]^{3/2}}$$

$$B_2 = \frac{\mu_0 I 4a^2}{2 \cdot 8(x^2 + a^2)^{3/2}} = \frac{\mu_0 I a^2}{4(x^2 + a^2)^{3/2}}$$

The ratio of the magnetic field induction at the origin due to the smaller coil to that of the larger coil can now be calculated as follows:

$$\text{Ratio} = \frac{B_1}{B_2} = \frac{\frac{\mu_0 I a^2}{2(x^2 + a^2)^{3/2}}}{\frac{\mu_0 I a^2}{4(x^2 + a^2)^{3/2}}} = \frac{4(x^2 + a^2)^{3/2}}{2(x^2 + a^2)^{3/2}} = \frac{4}{2} = 2$$

Therefore, the ratio of the magnetic field induction at the origin due to the smaller coil to that of the bigger one is:

Option A: 2 : 1

Question 49

A metallic rod of 2 m length is rotated with a frequency 100 Hz about an axis passing through the centre of the circular ring of radius 2 m. A constant magnetic field 2 T is applied parallel to the axis and perpendicular to the length of the rod. The emf developed across the ends of the rod is :

Options:

A. 800π volt

B. 1600π volt

C. 1600 volt

D. 400π volt

Answer: A

Solution:

To determine the electromotive force (emf) developed across the ends of the rotating rod, we can use the concept of motional emf generated in a rotating conductor in a magnetic field.

The formula for the motional emf in a rotating rod is given by:

$$\varepsilon = \frac{1}{2} B \omega L^2$$

where:

- B is the magnetic field strength
- ω is the angular velocity
- L is the length of the rotating rod

First, let's find the angular velocity ω . The frequency f is given as 100 Hz. The relationship between angular velocity ω and frequency f is:

$$\omega = 2\pi f$$

Plugging in the values:

$$\omega = 2\pi \cdot 100 = 200\pi \text{ rad/s}$$

The length of the rod L is given as 2m and the magnetic field strength B is given as $\frac{1}{2}$ T.

Now, substituting these values into the motional emf formula:

$$\varepsilon = \frac{1}{2} \cdot 2 \cdot 200\pi (2)^2$$

Simplifying this expression:

$$\begin{aligned}\varepsilon &= \frac{1}{2} \cdot 2 \cdot 200\pi \cdot 4 \\ &= 800\pi \text{ V}\end{aligned}$$

Therefore, the emf developed across the ends of the rod is:

Option A: 800π volt

Question 50

The power of a gun which fires 120 bullet per minute with a velocity 120 ms^{-1} is : (given the mass of each bullet is 100 g)

Options:

A. 86400 W

B. 14.4 kW

C. 1.44 kW

D. 1220 W

Answer: C

Solution:

To calculate the power of the gun, we need to use the formula for power which is given by:

$$P = \frac{W}{t}$$

where P is the power, W is the work done, and t is time.

First, we will calculate the work done to fire one bullet. The kinetic energy of a bullet can be calculated using the formula:

$$KE = \frac{1}{2}mv^2$$

Given:

- Mass of each bullet, $m=100\text{ g}=0.1\text{ kg}$
- Velocity of each bullet, $v=120\text{ ms}^{-1}$

Substituting these values into the kinetic energy formula gives:

$$KE = \frac{1}{2} \times 0.1 \times (120)^2$$

$$KE = 0.05 \times 14400$$

$$KE = 720\text{ J}$$

This is the work done to fire one bullet. Since the gun fires 120 bullets per minute:

$$= 120 \times 720\text{ J per minute}$$

W

$$= 86400\text{ J per minute}$$

W

To find the power, we need to convert this work into watts (joules per second). Since there are 60 seconds in a minute, we have:

$$P = \frac{86400\text{ J}}{60\text{ s}}$$

$$P = 1440\text{ W} = 1.44\text{ kW}$$

Therefore, the power of the gun is 1.44 kW.

The correct answer is:

Option C: 1.44 kW

Question 51

The width of the fringes obtained in the Young's double slit experiment is 2.6 mm when light of wave length 6000 \AA is used. If the whole apparatus is immersed in a liquid of refractive index 1.3 the new fringe width will be :

Options:

A. 2.6 mm B. 5.2 mm C. 2 mm

D. 4 mm

Answer: C

Question 52

An electric bulb of volume 300 cm³ was sealed off during manufacture at a pressure of 1 mm of mercury at 27°C. The number of air molecules contained in the bulb is, ($R=8.31 \text{ J mol}^{-1} \text{ K}^{-1}$ and

$$N_A = 6.02 \times 10^{23})$$

Options:

A. 9.67×10^{16}

B. 9.65×10^{15}

C. 9.67×10^{17}

D. 9.65×10^{18}

Answer: D

Solution:

We can approach this problem using the ideal gas equation:

$$PV = nRT$$

Here, P is the pressure, V is the volume, n is the number of moles of the gas, R is the gas constant, and T is the temperature in Kelvin.

First, let's convert the given quantities into SI units:

- Volume $V=300\text{cm}^3=300\times 10^{-6}\text{m}^3=3.00\times 10^{-4}\text{m}^3$
- Pressure $P=1\text{mm of mercury}=1\text{mmHg}$

To convert the pressure from mmHg to Pascals (Pa), we use the fact that $1 \text{ mmHg} = 133.322 \text{ Pa}$:

$$P = 1 \text{ mmHg} \times 133.322 \text{ Pa/mmHg} = 133.322 \text{ Pa}$$

The temperature must be in Kelvin, so we convert from Celsius to Kelvin:

$$T = 27^\circ\text{C} = 27 + 273.15 = 300.15 \text{ K}$$

Substituting these values into the ideal gas equation, we find the number of moles n :

$$n = \frac{pV}{RT} = \frac{133.322 \text{ Pa} \times 3.00 \times 10^{-4} \text{ m}^3}{8.31 \text{ J mol}^{-1} \text{ K}^{-1} \times 300.15 \text{ K}}$$

Now, we calculate:

$$n = \frac{133.322 \times 3.00 \times 10^{-4}}{8.31 \times 300.15} = \frac{39.9966 \times 10^{-4}}{2493.2465} \approx 1.60 \times 10^{-5} \text{ mol}$$

To find the number of air molecules, we use Avogadro's number N_A :

$$N = n \times N_A = 1.60 \times 10^{-5} \text{ mol} \times 6.02 \times 10^{23} \text{ molecules/mol}$$

Calculating this, we get:

$$N = 9.63 \times 10^{18} \text{ molecules}$$

However, rounding to significant figures (to match the options provided), we get:

$$N \approx 9.65 \times 10^{18} \text{ molecules}$$

Thus, the correct answer is:

Option D: 9.65×10^{18}

Question 53

Find the binding energy of the tritium nucleus: [Given: mass of $^1_1\text{H} = 3.01605 \text{ u}$; $m_p = 1.00782 \text{ u}$; $m_n = 1.00866 \text{ u}$.]

Options:

A. 8.5 MeV

B. 8.5 J

C. 0.00909 MeV

D. 0.00909 eV

Answer: A

Solution:

The binding energy of a nucleus is the energy required to disassemble the nucleus into its constituent protons and neutrons. The formula to calculate the binding energy is given by:

$$\text{Binding Energy} = (\text{Total mass of individual nucleons} - \text{Mass of the nucleus}) \times 931.5 \text{ MeV/u}$$

For tritium (${}^3_1\text{H}$), it consists of 1 proton and 2 neutrons. We are given the following masses:

Mass of tritium nucleus, $m_T = 3.01605 \text{ u}$

Mass of a proton, $m_p = 1.00782 \text{ u}$

Mass of a neutron, $m_n = 1.00866 \text{ u}$

First, we calculate the total mass of individual nucleons:

Total mass of nucleons $= 1 \times 1.00782 \text{ u} + 2 \times 1.00866 \text{ u}$

$$= 1.00782 \text{ u} + 2.01732 \text{ u}$$

$$= 3.02514 \text{ u}$$

Next, we calculate the mass defect (difference between the total mass of individual nucleons and the mass of the nucleus):

Mass defect =

$$= 3.02514 \text{ u} - 3.01605 \text{ u}$$

$$= 0.00909 \text{ u}$$

Now, we convert the mass defect into energy using the conversion factor 931.5 MeV/u :

$$\text{Binding Energy} = 0.00909 \text{ u} \times 931.5 \text{ MeV/u}$$

$$\approx 8.5 \text{ MeV}$$

Therefore, the binding energy of the tritium nucleus is approximately 8.5 MeV . Hence, the correct option is:

Option A: 8.5 MeV

Question 54

In a single slit diffraction experiment, for slit width ' α ' the width of the central maxima is ' β '. If we double the slit width then the corresponding width of the central maxima will be:

Options:

A. 4

B. $\frac{\beta}{2}$

- C. $\frac{\beta}{2}$
 D. 2β

Answer: C

Solution:

In a single slit diffraction experiment, the width of the central maxima is given by the diffraction pattern formula derived from the Huygens-Fresnel principle. The position of the first minima in the diffraction pattern is given by:

$$a \sin(\theta) = n\lambda$$

where a is the slit width, θ is the angle of the diffraction minimum, n is the order of the minimum (for the first minimum, $n=1$), and λ is the wavelength of the light used.

The angular width of the central maxima is approximately twice the angle to the first minimum:

$$\Delta\theta = 2 \frac{\lambda}{a}$$

When projecting this onto a screen at a distance D , the width of the central maximum can be approximated by:

$$\beta = 2D \tan(\theta) \approx 2D \left(\frac{\lambda}{a} \right)$$

If the slit width a is doubled, say to $2a$, then the new width of the central maximum β' becomes:

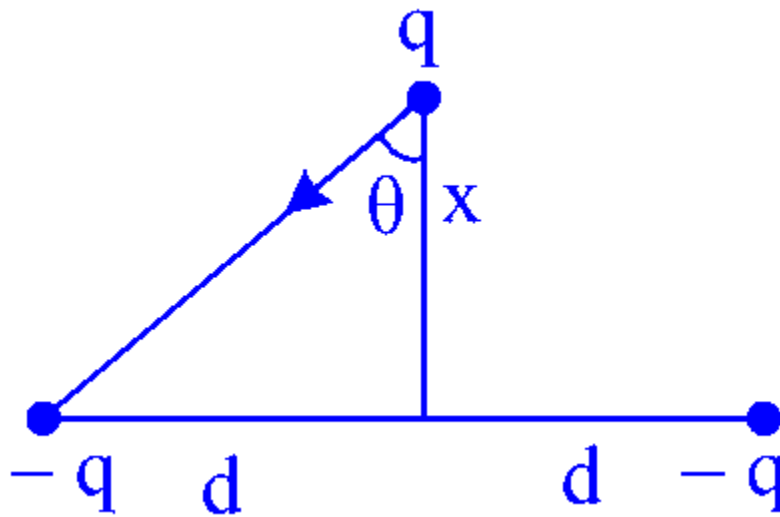
$$\beta' = 2D \left(\frac{\lambda}{2a} \right) = \frac{\beta}{2}$$

Thus, if the slit width is doubled, the corresponding width of the central maxima will be:

Option C: $\frac{\beta}{2}$.

Question 55

Two charges ' $-q$ ' each are fixed, separated by distance ' $2d$ '. A third charge ' q ' of mass ' m ' placed at the mid-point is displaced slightly by ' x ' ($x < d$) perpendicular to the line joining the two fixed charges as shown in Fig. The time period of oscillation of ' q ' will be



Options:

A. $T = \sqrt{\frac{\frac{0}{8\epsilon} \frac{\pi}{2} d^3}{q^2}}$

B. $T = \sqrt{\frac{\frac{0}{8\epsilon} \frac{\pi}{3} d^3}{q^3}}$

C. $T = \sqrt{\frac{\frac{0}{4\epsilon} \frac{\pi}{3} d^3}{q^2}}$

D. $T = \sqrt{\frac{\frac{0}{8\epsilon} \frac{\pi}{3} d^3}{q^2}}$

Answer: D

Question 56

Two metal spheres, one of radius R and the other of radius $2R$

respectively have the same surface charge density. They are brought in contact and separated. The ratio of their new surface charge densities is

Options:

A. $2 : 1$

B. 4 : 1

C. 1 : 4

D. 1 : 2

Answer: B

Solution:

To solve this problem, we need to understand a few key concepts about charge distribution and surface charge density. Let's walk through the problem step by step.

When two conductors are brought into contact, charge will redistribute between them until they reach the same electrical potential. For spheres, the surface charge density is related to the charge and the radius of the sphere. Before contact, both spheres have the same surface charge density. Let's denote this common surface charge density as σ .

For a sphere of radius R , the surface area A is given by:

$$A = 4\pi R^2$$

The charge Q on each sphere can be expressed as:

$$Q = \sigma \cdot A = \sigma \cdot 4\pi R^2$$

Given the radii of the two spheres, the charge on each sphere before contact is:

For the sphere with radius $\frac{R}{2}$:

$$Q_1 = \sigma \cdot 4\pi \left(\frac{R}{2}\right)^2 = \sigma \cdot \pi R^2$$

For the sphere with radius $2R$:

$$Q_2 = \sigma \cdot 4\pi (2R)^2 = \sigma \cdot 16\pi R^2$$

When the two spheres are brought into contact and then separated, the total charge will be redistributed between them. The total charge is:

$$Q_{total} = Q_1 + Q_2 = \sigma \cdot \pi R^2 + \sigma \cdot 16\pi R^2 = 17\sigma \cdot \pi R^2$$

Since the spheres are in contact, they will have the same potential. The potential (V) for a sphere is given by:

$$V = \frac{Q}{4\pi\epsilon_0 R}$$

Let Q_1' and Q_2' be the charges on the spheres with radii $\frac{R}{2}$ and $2R$ respectively after they have been separated. The potential of both spheres must be equal:

$$\frac{Q_1'}{\frac{R}{2}} = \frac{Q_2'}{2R}$$

Simplifying, we get:

$$\frac{Q'_1}{R/2} = \frac{Q'_2}{2R} \Rightarrow Q'_1 \cdot 2R = Q'_2 \cdot \frac{R}{2} \Rightarrow Q'_1 = \frac{Q'_2}{4}$$

We also know that the total charge is conserved:

$$Q'_1 + Q'_2 = 17\sigma\pi R^2$$

Substituting $Q'_1 = \frac{Q'_2}{4}$ into this equation, we get:

$$\frac{Q'_2}{4} + Q'_2 = 17\sigma\pi R^2 \Rightarrow \frac{5Q'_2}{4} = 17\sigma\pi R^2 \Rightarrow Q'_2 = \frac{68\sigma\pi R^2}{5}$$

And for the smaller sphere:

$$Q'_1 = \frac{Q'_2}{4} = \frac{68\sigma\pi R^2}{5} \cdot \frac{1}{4} = \frac{17\sigma\pi R^2}{5}$$

Now, we can find the new surface charge densities:

For the sphere with radius R :

$$\sigma'_1 = \frac{Q'_1}{4\pi R^2} = \frac{\frac{17\sigma\pi R^2}{5}}{\pi R^2} = \frac{17\sigma}{5}$$

For the sphere with radius $2R$:

$$\sigma'_2 = \frac{Q'_2}{4\pi(2R)^2} = \frac{\frac{68\sigma\pi R^2}{5}}{16\pi R^2} = \frac{68\sigma}{80} = \frac{17\sigma}{20}$$

Finally, the ratio of the new surface charge densities $\sigma'_1 : \sigma'_2$ is:

$$\frac{\sigma'_1}{\sigma'_2} = \frac{\frac{17\sigma}{5}}{\frac{17\sigma}{20}} = \frac{20}{5} = 4 : 1$$

So, the correct answer is Option B: 4:1.

Question 57

Find the value of 'n' in the given equation
pressure, ' ρ ' density and ' v ' velocity.

Options:

$$p = \rho n v^2 \text{ where 'p' is the}$$

A. $n = \frac{1}{2}$

B. $n = 1$

C. $n = 3$

D. $n = 2$

Answer: B

Solution:

The given equation is:

$$P = \rho n v^2$$

We need to find the value of n , and for this, we can perform dimensional analysis. Let's break down the dimensions of each quantity involved.

The dimensions of pressure P are:

$$[P] = \text{ML}^{-1}\text{T}^{-2}$$

The dimensions of density ρ are:

$$[\rho] = \text{ML}^{-3}$$

The dimensions of velocity v are:

$$[v] = \text{LT}^{-1}$$

Substitute these dimensions into the given equation:

$$[P] = [\rho]^n [v]^2$$

Let's plug in the dimensions:

$$[\text{ML}^{-1}\text{T}^{-2}] = [(\text{ML}^{-3})^n][(\text{LT}^{-1})^2]$$

Simplify the dimensions on the right-hand side:

$$[\text{ML}^{-1}\text{T}^{-2}] = [\text{M}^n \text{L}^{-3n}][\text{L}^2 \text{T}^{-2}]$$

Combine the terms on the right-hand side:

$$[\text{ML}^{-1}\text{T}^{-2}] = [\text{M}^n \text{L}^{-3n+2} \text{T}^{-2}]$$

Now, equate the exponents of corresponding dimensions from both sides:

$$\text{For mass (M): } 1 = n$$

$$\text{For length (L): } -1 = -3n + 2$$

$$\text{For time (T): } -2 = -2$$

We already get the value of n from the mass dimension equation:

$$n = 1$$

To verify, substitute $n = 1$ in the length dimension equation:

$$-1 = -3(1) + 2$$

$$-1 = -3 + 2$$

$$-1 = -1$$

This is correct, so the value of n is confirmed as:

$$n = 1$$

Therefore, the correct option is:

Option B: $n=1$

Question 58

A stone of mass 2 kg is hung from the ceiling of the room using two strings. If the strings make an angle 60° and 30° respectively with the

horizontal surface of the roof then the tension on the longer string is :

$$g = 10 \text{ ms}^{-2}$$

Options:

A. $\frac{2}{\sqrt{3}} \text{ N}$

B. $10\sqrt{3} \text{ N}$

C. 10 N

D. $\sqrt{3} \text{ N}$

Answer: C

Question 59

A parallel plate capacitor is filled by a dielectric whose relative permittivity varies with the applied voltage (U) as $\epsilon = 2U$. A similar

capacitor with no dielectric is charged to $U_0 = 78 \text{ V}$. It is then

connected to the uncharged capacitor with the dielectric. Find the final voltage on the capacitors.

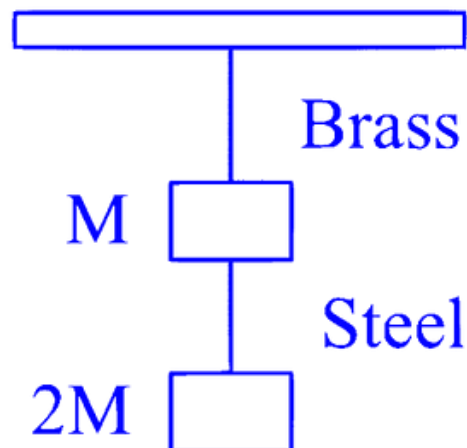
Options:

A. 6V B. 8V C. 2V D. 4V

Answer: A

Question 60

If the ratio of lengths, radii and Young's Moduli of steel and brass wires in the figure are a, b and c respectively, then the corresponding ratio of increase in their lengths would be



Options:

A. $\frac{a}{3b^2c}$

B. $\frac{3a}{2b^2c}$

C. $\frac{2a}{3b^2c}$

D. $\frac{2ab^2}{c}$

Answer: C
