04/04/2025 Morning





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## Memory Based Answers & Solutions

Time : 3 hrs. M.M. : 300

#### JEE (Main)-2025 (Online) Phase-2

(Physics, Chemistry and Mathematics)

#### IMPORTANT INSTRUCTIONS:

- (1) The test is of **3 hours** duration.
- (2) This test paper consists of 75 questions. Each subject (PCM) has 25 questions. The maximum marks are 300.
- (3) This question paper contains **Three Parts**. **Part-A** is Physics, **Part-B** is Chemistry and **Part-C** is **Mathematics**. Each part has only two sections: **Section-A** and **Section-B**.
- (4) Section A: Attempt all questions.
- (5) Section B : Attempt all questions.
- (6) **Section A (01 20)** contains 20 multiple choice questions which have **only one correct answer**. Each question carries **+4 marks** for correct answer and **–1 mark** for wrong answer.
- (7) Section B (21 25) contains 5 Numerical value based questions. The answer to each question should be rounded off to the **nearest integer**. Each question carries +4 marks for correct answer and -1 mark for wrong answer.

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#### **PHYSICS**

#### **SECTION - A**

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

#### Choose the correct answer:

- 1. Find the dimension of  $\frac{E}{B}$ , where E represents electric field and B represents magnetic field.
  - (1)  $ML^2T^{-1}$
  - (2) LT<sup>-1</sup>
  - (3)  $L^2T^{-1}$
  - (4) LT<sup>-2</sup>

#### Answer (2)

Sol. 
$$\frac{E}{B} = C$$

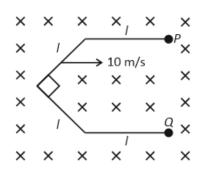
$$= LT^{-1}$$

- 2. Mean free path for an ideal gas is to be observed 20  $\mu m$  while average speed of molecules of gas is observed to be 600 m/s. Then frequency of collision is nearly
  - (1)  $4 \times 10^7$
  - (2)  $1.2 \times 10^7$
  - (3)  $3 \times 10^7$
  - (4)  $2 \times 10^{-7}$

#### Answer (3)

**Sol.** Mean free time 
$$\tau = \frac{\lambda}{v} \Rightarrow f = \frac{v}{\lambda} = \frac{600}{20 \times 10^{-6}} = 3 \times 10^{7}$$

3. 4 rods of equal length are joined as shown in the figure. Combined system is moving with speed 10 m/s in a perpendicular magnetic field of  $\frac{1}{\sqrt{2}}$  tesla. Find emf induced between point P and Q (I = 10 cm).



- (1) 1 volt
- (2) 0.1 volt
- (3) 2 volts
- (4)  $\sqrt{2}$  volt

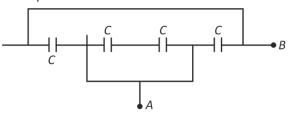
#### Answer (1)



$$L = \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} = \sqrt{2}I$$

$$emf = \frac{1}{\sqrt{2}} \times 10 \times \sqrt{2} \times 0.1$$

4. Find equivalent capacitance between A and B, where  $C = 16 \,\mu\text{F}$ 

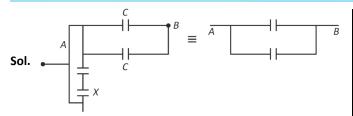


- (1) 48 μF
- (2) 8 μF
- (3) 32 μF
- (4)  $16 \mu F$

Answer (3)

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$$C_{\text{eq}}$$
 = 2 $C$  = 32  $\mu$ F

- A real object placed in front of a spherical mirror forms an image whose magnification is  $-\frac{1}{3}$ . If the distance between the image and object is 30 cm. The focal length of the mirror is cm.
  - (1) -11.25 cm
- (2) -22.5 cm
- (3) 45 cm
- (4) -60 cm

#### Answer (1)

Sol. Magnification is negative implies mirror is conversing.

$$m = -\frac{v}{u} = -\frac{1}{3}$$

Or 
$$v = \frac{u}{3}$$

Also, v - u = 30 cm

u = -45 cm

v = -15 cm

$$f = \frac{uv}{u+v} = -11.25 \text{ cm}$$

circuit is given 6. The current in a AC  $i = 100\sqrt{2}\sin\left(\frac{100\pi}{t}\right)A$ .

Find rms current and frequency is Hertz.

- (1) 100 A, 100 Hz
- (2) 50 A, 100 Hz
- (3) 200 A, 50 Hz
- (4) 100A, 50 Hz

#### Answer (4)

**Sol.** 1 rms =  $\frac{i_0}{\sqrt{z}} = \frac{100\sqrt{z}}{\sqrt{z}} = 100$ 

 $\omega t = 100 \pi t \Rightarrow \omega = 2\pi f = 100 \pi$ 

f = 50 Hz

- 7. An electric dipole with charges 2 µC and a separation 20 cm is placed close to an infinitely charge nonconducting sheet with surface charge density 100 C/m<sup>2</sup>. Find the torque acting on the dipole if the dipole makes an angle 30° with the normal to the sheet.

  - (1)  $\frac{12}{\epsilon_0} \times 10^{-5} \text{ N-m}$  (2)  $\frac{2}{\epsilon_0} \times 10^{-5} \text{ N-m}$
  - (3)  $\frac{4}{\epsilon_0} \times 10^{-5} \text{ N-m}$  (4)  $\frac{1}{\epsilon_0} \times 10^{-5} \text{ N-m}$

#### Answer (4)

**Sol.**  $\tau = pE\sin\theta$ 

p = qd

$$E = \frac{\sigma}{2\varepsilon_0}$$

 $\tau = qdE \sin\theta$ 

$$= \frac{(2 \times 10^{-6} \text{ C})(0.2 \text{ m}) \times 100}{2\varepsilon_0} \text{ C/m}^2 \sin 30^\circ = \frac{2}{\varepsilon_0} \times 10^{-5} \text{ N-m}$$

Assertion (A): The minimum kinetic energy required to take a body of mass m from surface of earth to infinity is mgR.

Reason (R): Potential energy at surface of earth is zero.

- (1) (A) and (R) both are correct and (R) is correct explanation of (A)
- (2) (A) and (R) both are correct and (R) is not correct explanation of (A)
- (3) (A) is correct but (R) is incorrect
- (4) (A) is incorrect but (R) is correct

#### Answer (3)

Sol. Conceptual.

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- Longitudinal sound waves travel in three different gases namely helium, methane and carbon dioxide. Mean temperature of three gases are equal then ratio of speeds of wave in three gases respectively is

  - (1)  $\sqrt{5}:\sqrt{7}:\frac{1}{\sqrt{11}}$  (2)  $\sqrt{3}:\sqrt{5}:\frac{1}{\sqrt{11}}$
  - (3)  $\sqrt{5}:1:\sqrt{\frac{21}{55}}$  (4)  $\frac{1}{\sqrt{3}}:\frac{1}{\sqrt{5}}:\frac{1}{2}$

#### Answer (3)

Sol. 
$$v = \sqrt{\frac{\gamma RT}{M_0}}$$

$$\begin{aligned} \text{Ratio} &\equiv \sqrt{\frac{\gamma_1}{M_1}} : \sqrt{\frac{\gamma_2}{M_2}} : \sqrt{\frac{\gamma_3}{M_3}} \\ &= \sqrt{\frac{5}{3 \times 4}} : \sqrt{\frac{4}{3 \times 16}} : \sqrt{\frac{7}{5 \times 44}} \equiv \sqrt{\frac{5}{3}} : \sqrt{\frac{1}{3}} : \sqrt{\frac{7}{55}} \end{aligned}$$

- 10. Ratio of radii of 5<sup>th</sup> orbit of He<sup>+</sup> and Li<sup>2+</sup> atom will be
  - $(1) \frac{5}{2}$

(3)  $\frac{3}{2}$ 

#### Answer (3)

**Sol.** 
$$r = \frac{\eta^2}{Z} a_0$$
  $\frac{r_{He^+}}{r_{Li^{2+}}} = \frac{\eta^2}{Z_{He^+}} \frac{Z_{Li^{2+}}}{\eta^2} = \frac{3}{2}$ 

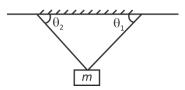
11. Assertion: In photoelectric effect, if intensity of monochromatic light is increased then stopping potential increases.

Reason: Increased intensity results in increment of photocurrent.

- (1) A is correct, R is correct and R is explanation of A
- (2) A is correct, R is correct and R is not explanation of Α
- A is incorrect and R is correct
- (4) A is correct and R is incorrect

#### Answer (3)

- Sol. (1) Frequency changes the stopping potential not intensity.
  - (2) Higher in tensity means higher number of electrons.
- A block of mass *m* kg is connected to two strings as shown. If  $T_1 = \sqrt{3}T_2$ , then choose correct option



(1) 
$$\theta_1 = 60^\circ$$
,  $\theta_2 = 30^\circ$ ,  $T_1 = \frac{mg}{2}$ 

(2) 
$$\theta_1 = 60^\circ$$
,  $\theta_2 = 30^\circ$ ,  $T_2 = \frac{mg}{2}$ 

(3) 
$$\theta_1 = 30^\circ$$
,  $\theta_2 = 60^\circ$ ,  $T_1 = \frac{3mg}{4}$ 

(4) 
$$\theta_1 = 30^\circ$$
,  $\theta_2 = 60^\circ$ ,  $T_2 = \frac{3mg}{4}$ 

#### Answer (2)

**Sol.**  $T_2 \cos \theta_2 = T_2 \cos \theta_1$ 

$$T_2 \cos \theta_2 = \sqrt{3} T_2 \cos \theta_1$$

$$\cos\theta_2 = \sqrt{3}\cos\theta_1$$

$$\theta_1 = 60^{\circ}, \, \theta_2 = 30^{\circ}$$

$$T_1 \sin \theta_1 + T_2 \sin \theta_2 = mg$$

$$\sqrt{3}T_2 \cdot \frac{\sqrt{3}}{2} + T_2 \cdot \frac{1}{2} = mg$$

$$2T_2 = mg$$

$$T_2 = \frac{mg}{2}$$

$$T_1 = \frac{\sqrt{3}}{2}mg$$

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- A Closed organ pipe having fundamental frequency  $f_0$ . Now  $\frac{1}{5}$  of volume its filled with water then % change in the fundamental frequency.
  - (1) +10%
  - (2) +25%
  - (3) -20%
  - (4) -10%

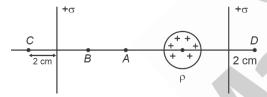
#### Answer (2)

**Sol.** 
$$f_0 = \frac{v}{4t}$$

$$f_0' = \frac{v}{4\left(\frac{4L}{5}\right)} = \frac{5}{4}\left(\frac{v}{4L}\right) = \frac{5}{4}f_0$$

$$= 1.25 f_0$$

14. In arrangement shown, has two non-conducting plane sheets with charge density  $\sigma$ , and a non-conducting sphere with volume charge density  $\rho$ .



Choose the correct relation between the magnitude of electric fields at A, B, C and D. Point A is at the middle of two sheets.

(1) 
$$E_A = E_B, E_C \neq E_D$$

(2) 
$$E_A > E_B, E_C \neq E_D$$

(3) 
$$E_A > E_B, E_C = E_D$$

(4) 
$$E_A \neq E_B$$
,  $E_C = E_D$ 

#### Answer (2)

**Sol.** 
$$\Rightarrow$$
  $|E_A| = \left| + \frac{\sigma}{2\varepsilon_0} - \frac{\sigma}{2\varepsilon_0} - \frac{1}{4\pi\varepsilon_0} \frac{Q}{r_A^2} \right| = \frac{Q}{4\pi\varepsilon_0 r_A^2}$ 

$$\Rightarrow |E_B| = \left| + \frac{\sigma}{2\varepsilon_0} - \frac{\sigma}{2\varepsilon_0} - \frac{1}{4\pi\varepsilon_0} \frac{Q}{r_B^2} \right| = \frac{Q}{4\pi\varepsilon_0 r_B^2}$$

$$\Rightarrow |E_{\Delta}| > |E_{R}| \text{ since } r_{\Delta} < r_{R}$$

$$\Rightarrow |E_c| = \left| -\frac{\sigma}{2\varepsilon_0} - \frac{\sigma}{2\varepsilon_0} - \frac{1}{4\pi\varepsilon_0} \frac{Q}{r_c^2} \right| = \frac{\sigma}{\varepsilon_0} + \frac{Q}{4\pi\varepsilon_0 r_c^2}$$

$$\Rightarrow |E_D| = \left| \frac{\sigma}{2\varepsilon_0} + \frac{\sigma}{2\varepsilon_0} + \frac{Q}{4\pi\varepsilon_0 r_D^2} \right| = \frac{\sigma}{\varepsilon_0} + \frac{Q}{4\pi\varepsilon_0 r_D^2}$$

$$\Rightarrow$$
  $|E_c| \neq |E_D|$  as  $r_c \neq r_D$ 

15. Two simple pendulums with amplitudes  $\theta_1$  and  $\theta_2$  have length of strings as  $I_1$  and  $I_2$  respectively. Choose the correct options if the maximum angular accelerations are same.

(1) 
$$\theta_1 I_1 = \theta_2 I_2$$

$$(2) \quad \theta_1 I_2 = \theta_2 I_1$$

(2) 
$$\theta_1 I_2 = \theta_2 I_1$$
  
(3)  $\theta_1 I_1^2 = \theta_2 I_2^2$ 

(4) 
$$\theta_1 I_2^2 = \theta_2 I_1^2$$

#### Answer (2)

**Sol.** 
$$\theta = \theta_0 \sin\left(\sqrt{\frac{g}{I}}t + \phi\right)$$

or 
$$\alpha = -\frac{g}{I}\theta$$

$$\alpha_{\text{max}} = \frac{g}{I} \theta_0$$

$$\left(\alpha_{\text{max}}\right)_{\text{1}} = \left(\alpha_{\text{max}}\right)_{\text{2}}$$

$$\frac{\theta_1}{l_1} = \frac{\theta_2}{l_2}$$

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- 16. In YDSE setup, distance between slits d = 0.2 mm. If d is changed to 0.4 mm, then % change in fringe width
  - (1) 25%
  - (2) 50%
  - (3) 100%
  - (4) 75%

Answer (2)

**Sol.** 
$$B = \frac{XD}{d}$$
  $B' = \frac{\lambda D}{2d} = \frac{B}{2}$ 

$$B' = \frac{\lambda D}{2d} = \frac{B}{2}$$

$$100 \times \frac{DB}{B} = 50\%$$

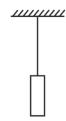
- 17. Regarding the rotational motion of rigid bodies, following two statements are given where symbols is are having usual meaning.
  - S1: Torgue  $\tau$  is given as  $\vec{\tau} = \frac{d\vec{L}}{dt}$  and angular momentum about inertial point is given as  $\vec{L} = \sum_{i} (\vec{r}_i \times \vec{p}_i)$ .
  - S2 : Torque  $\tau$  is given as  $\vec{\tau} = I\vec{r}$  and angular momentum about inertial point is given as  $\vec{L} = I\vec{\omega}$ .
  - (1) S1 is correct and S2 is incorrect
  - (2) S1 is incorrect and S2 is correct
  - (3) Both are incorrect
  - (4) Both are correct

Answer (1)

**Sol.** 
$$\vec{L} = I_{ang}\vec{\omega} + \vec{r} \times M\vec{v}_{CM}$$

Results in S2 is specific cases derived from results in S1.

18. A small mirror of mass *m* is suspended to a fix point with an ideal string of length I. A photon of energy E incident normally on the mirror. Find maximum angular deviation  $(\theta)$  of the mirror.



Answer (4)

Sol.



Moment imparted to the mirror =  $\frac{2E}{c}$ 

$$\Delta KE = -\Delta PE$$

$$\frac{\left(\frac{2E}{c}\right)^2}{2m} = mg(I - I\cos\theta)$$

$$\frac{2E^2}{mc^2} = mgI \cdot 2\sin^2\left(\frac{\theta}{2}\right)$$

$$\frac{2E^2}{mc^2} = mgl \cdot \frac{\theta^2}{2}$$

$$\theta = \frac{2E}{mc\sqrt{gI}}$$

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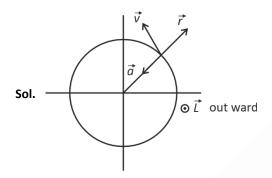




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- 19.  $\vec{L}$  and  $\vec{p}$  are angular momentum about origin and linear momentum of a particle. If position vector of particle is given as  $\vec{r} = a(\sin\omega t\hat{i} + \cos\omega t\hat{j})$  then direction of force is
  - (1) Opposite to  $\vec{L} \times \vec{r}$
  - (2) Opposite to  $\vec{p} \times \vec{r}$
  - (3) Opposite to  $\vec{L} \cdot \vec{r}$
  - (4) Opposite to  $\vec{p} \times \vec{L}$

#### Answer (4)



20.

#### **SECTION - B**

**Numerical Value Type Questions:** This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. A ring and a solid sphere released from rest from same height on enough rough inclined surface. Ratio of their speed when they reach at bottom is  $\sqrt{\frac{7}{x}}$  m/s, then x is

#### Answer (10)

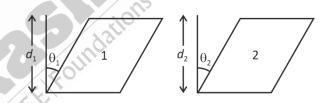
**Sol.** 
$$mgh = \frac{1}{2} 2mR^2 \frac{(v_r^2)}{R^2} = \frac{1}{2} \cdot \frac{7}{5} mR^2 \frac{(v_s^2)}{R^2}$$

$$\Rightarrow \frac{2(v_r^2)}{R^2} = \frac{7}{5} \frac{(v_s^2)}{R^2}$$

$$\Rightarrow \left(\frac{v_r}{v_s}\right)^2 = \frac{7}{10}$$

$$\Rightarrow \frac{v_r}{v_s} = \sqrt{\frac{7}{10}}$$

22. The figure shows two boxes with identical square cross-sections and heights  $h_1$  and  $h_2$  ( $h_1 = 2h_2$ ) are made of different materials. An equal force is applied on the square cross-sections such that the deformations  $\theta_1$  and  $\theta_2$  are realized ( $\theta_1 = 2\theta_2$ ). If shear modulus of box 1 is  $4 \times 10^9$  N/m<sup>2</sup> and that of box 2 is  $x \times 10^9$  N/m<sup>2</sup>, then x is \_\_\_\_\_\_.



Answer (8)

Sol. 
$$G = \frac{F}{A\theta}$$
 | Since  $F_1 = F_2$  and  $A_1 = A_2$   
 $G_1\theta_1 = G_2\theta_2$   
 $\Rightarrow G\theta = \frac{F}{A}$  |  $(4 \times 10^9 \text{ N/m}^2)\theta_1 = (x \times 10^9 \text{ N/m}^2)\theta_2$  |  $x = 8$ 

- 23.
- 24.
- 25.

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#### **CHEMISTRY**

#### **SECTION - A**

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

#### Choose the correct answer:

- Which of the following is the ratio of 5<sup>th</sup> Bohr orbit (r<sub>5</sub>) of He+ & Li2+ ions?
  - (1)  $\frac{2}{3}$

(3)  $\frac{9}{4}$ 

#### Answer (2)

**Sol.** 
$$r \propto \frac{n^2}{z}$$

$$\frac{(r_5)_{He^+}}{(r_5)_{Li^{2+}}} = \frac{\frac{5^2}{2}}{\frac{5^2}{3}} = \frac{3}{2}$$

- Which of the following pair of ions have equal number of unpaired electrons
  - (1)  $V^{2+}$  and  $Ni^{2+}$
  - (2)  $Cr^{2+}$  and  $Mn^{2+}$
  - (3)  $Fe^{2+}$  and  $Sc^{2+}$
  - (4)  $Mn^{3+}$  and  $Fe^{2+}$

#### Answer (4)

Sol. unequal 
$$\begin{cases} V^{2+} \Rightarrow s^0 d^3 \Rightarrow 3 \text{ unpaired } e^- \\ Ni^{2+} \Rightarrow s^0 d^8 \Rightarrow \text{unpaired } e^- \end{cases}$$

unequal 
$$\begin{cases} Cr^{2+} & \Rightarrow s^0 d^4 \Rightarrow 4 \text{ unpaired e}^- \\ Mn^{2+} & \Rightarrow s \ d^5 \Rightarrow 5 \text{ unpaired e}^- \end{cases}$$

## $\mbox{unequal} \begin{cases} \mbox{Fe}^{2+} & \Rightarrow \mbox{s}^0 d^6 \Rightarrow \mbox{4 unpaired e}^- \\ \mbox{Sc}^{2+} & \Rightarrow \mbox{s}^0 d' & \Rightarrow \mbox{1 unpaired e}^- \end{cases}$

unequal 
$$\begin{cases} Fe^{2+} \Rightarrow s^0 d^6 \Rightarrow 4 \text{ unpaired } e^- \\ Mn^{3+} \Rightarrow s \ \theta^4 \Rightarrow 4 \text{ unpaired } e^- \end{cases}$$

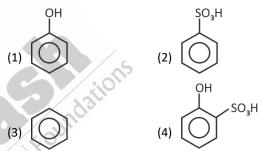
3. In the reaction sequence:

$$+$$
 oleum  $\longrightarrow$  (X)

$$(X)$$
  $\xrightarrow{\text{(i) NaOH,}}$   $(Y)$ 

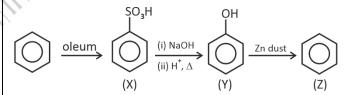
$$(Y)$$
  $\xrightarrow{Zn dust}$   $(Z)$ 

The compound (Z) is



#### Answer (3)

Sol.



- Incorrect order of atomic radius is
  - (1) B < Al
- (2) In < TI
- (3) Al < Ga
- (4) Ga < In

#### Answer (3)

Sol. B Ga 88 170 (pm) 143 135

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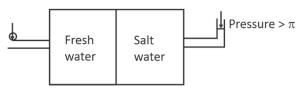




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5. Observe the following diagram.



For reverse osmosis, which of the following can be used for porous membrane?

- (1) Cellulose acetate
- (2) Porous silicate
- (3) Silicone
- (4) Glass membrane

#### Answer (1)

- **Sol.** Cellulose acetate is used as semipermeable membrane for reverse osmosis.
- 6. One mole of an ideal gas expands from 10 dm³ to 20 dm³ through isothermal reversible process. Find  $\Delta U$ , q & w
  - (1)  $\Delta U = 0$ , q = 0, w = 0
- (2)  $\Delta U = 0, q \neq 0, w \neq 0$
- (3)  $\Delta U \neq 0$ , q = 0, w  $\neq 0$
- (4)  $\Delta U \neq 0$ ,  $q \neq 0$ , w = 0

#### Answer (2)

**Sol.** For an ideal gas undergoing isothermal reversible process  $\Delta U = 0$  (As  $\Delta T = 0$ )

But 
$$q \neq 0$$

7. 
$$W \neq 0$$

$$(1) \text{ Sn, HCI}$$

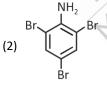
$$(2) \text{ Ac}_2\text{O, pyridine}$$

$$(3) \text{ Br}_2/\text{H}_2\text{O}$$

$$(4) \text{ H}_3\text{O}^{\dagger}$$

$$P \text{ (major product)}$$







Sol.

$$NO_{2} \longrightarrow NH_{2} \longrightarrow NH - \stackrel{O}{C} - CH_{3} \longrightarrow NH - \stackrel{O}{C} - CH_{3} \longrightarrow NH - \stackrel{O}{C} - CH_{3} \longrightarrow NH_{2}$$

$$\xrightarrow{Sn/HCl} \longrightarrow Ac_{2}O \longrightarrow Pridine \qquad (o - p \text{ directing group}) \qquad Br \qquad H_{3}O \longrightarrow Pridine \qquad (p) \qquad (p) \qquad (Major production)$$

$$(o - p \text{ directing group}) \qquad (o - p \text{ directing group}) \qquad (major production)$$

- 8. Which of the following is correct option regarding 1s orbital
  - (1) It is symmetrical
- (2) It is non-symmetrical
- (3) It is directional
- (4) It has two radial nodes

#### Answer (1)

Sol.



1s Orbital ⇒ Symmetrical, non-directional, zero radial node.

- 9. Total number of stereoisomers possible for complexes  $[Cr(Cl_3)(Py)_3]$  and  $[CrCl_2(C_2O_4)_2]$  respectively are
  - (1) 2, 3
- (2) 3, 2
- (3) 3, 3
- (4) 2, 2

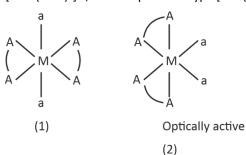
#### Answer (1)

**Sol.** [CrCl<sub>3</sub>(Py)<sub>3</sub>], this complex is type of [Ma<sub>3</sub>b<sub>3</sub>], where a and b are monodentate ligands.

There are two possible geometrical isomer facial isomers and meridional and both are optically inactive.

Total number of stereoisomers = 2

 $[CrCl_2(C_2O_4)_2]^{3-}$ , this complex is of type  $[Ma_2(AA)_2]$ 



Total stereoisomers = 3

#### Answer (4)





10. In lead storage battery during charging oxidation state of lead show changes

at anode from x1 to y1

at cathode from x2 to y2

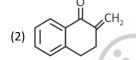
Find value of  $x_1$ ,  $y_1$ ,  $x_2$ ,  $y_2$ 

- (1)  $x_1 = +2, y_1 = 0$   $x_2 = +2, y_2 = +4$  (2)  $x_1 = +4, y_1 = 0$   $x_2 = +2, y_2 = +4$
- (3)  $\begin{array}{ccc} x_1=0, y_1=+2 \\ x_2=+4, y_2=+2 \end{array}$  (4)  $\begin{array}{ccc} x_1=+2, y_1=0 \\ x_2=+4, y_2=0 \end{array}$

#### Answer (1)

- **Sol.** On changing the lead storage battery PbSO<sub>4</sub>(s) at anode is converted into Pb and PbSO<sub>4</sub>(s) at cathode is converted into PbO<sub>2</sub>.
- 11. Which of the following compound is not a product of intramolecular aldol condensation reaction?





#### Answer (2)

OH

$$\begin{array}{c|c} & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\$$

... option (2) cannot be formed by intramolecular aldol condensation

Consider the reaction  $A + B \rightarrow Product$ 

$$R = k[A]^m[B]^n$$

When conc. of A & B taken are A<sub>1</sub> & B<sub>1</sub> respectively, then rate of reaction is R<sub>1</sub>. When conc. of A & B taken are 2A<sub>1</sub> &  $\frac{B_1}{2}$ , then rate of reaction is R<sub>2</sub>. Find  $\frac{R_2}{R}$ ?

- (1)  $2^{m+n}$
- (2) 2<sup>n-m</sup>
- $(3) 2^{m-n}$
- (4) 1

#### Answer (3)

**Sol.**  $R_1 = k[A_1]^m[B_1]^n$ 

$$R_2 = k[2A_1]^m \left[\frac{B_1}{2}\right]^n$$

$$\frac{R_2}{R_1} = \frac{\left[2A_1\right]^m \left[\frac{B_1}{2}\right]^n}{\left[A_1\right]^m \left[B_1\right]} = \frac{2^m}{2^n} = 2^{m-n}$$

- The complex ion having crystal field stabilization energy is zero and value of spin only magnetic moment is 5.92 BM.
  - (1)  $[FeF_6]^{4-}$
  - (2)  $[Mn(SCN)_6]^{4-}$
  - (3)  $[Co(NH_3)_6]^{3+}$
  - (4)  $[Fe(CN)_6]^{3-}$

Answer (2)

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**Sol.** Complex having d<sup>5</sup> configuration with weak field ligand has CFSE = 0

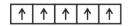
with Mn2+, SCN- is weak field ligand

$$\Rightarrow t_{2g}^3 e_g^2$$

CFSE = 
$$[3 \times (-0.4) + 2 \times (0.6)] \Delta_0$$

= 0

 $Mn^{2+} \Rightarrow d^5$ 



n = 5 (unpaired electron)

$$\mu = \sqrt{n(n+2)} \ BM$$

$$=\sqrt{5\times7}$$
 BM

$$=\sqrt{35}$$
 BM

= 5.92 BM

- 14. Statement-I: (A)  $C_2H_5$  CH =  $\overset{\circ}{C}H$   $\overset{\circ}{C}HO$  has higher dipole moment than
  - (B)  $C_2H_5 {^2}_{CH_2} {^1}_{CHO}$ .

Statement-II: C1 – C2 bond length in (A) is longer than

(B)

In the light of above statements, choose the correct option:

- (1) Both Statement-I and Statement-II are correct
- (2) Both Statement-I and Statement-II are incorrect
- (3) Statement-I is correct but Statement-II is incorrect
- (4) Statement-I is incorrect but Statement-II is correct

**Sol.** Due to resonance in (A) C1-C2 has partial  $\pi$ -bond character, hence shorter bond length than that in (B).

Due to resonance  $C_1H_1 - CH \stackrel{?}{=} CH \stackrel{?}{=} CH$ flow is in one direction hence higher dipole moment.

In following sequence of reaction. A is converted to D 15.

$$C_{3}\underset{A}{H_{6}}0 \xrightarrow{H_{2}/Pd} B \xrightarrow{HBr} C \xrightarrow{Mg/Ether} D$$

D is treated with A followed by hydrolysis to give 2,3dimethyl-butan-2-ol. Then identify A, B, C.

- (1)  $A = CH_3COCH_3$ 
  - $B = CH_3 CH(OH)CH_3$
  - C = CH<sub>3</sub>-CH(Br)CH<sub>3</sub>
- (2)  $A = CH_3CH_2CHO$ 
  - $B = CH_3CH_2CH_2OH$
  - $C = CH_3CH_2CH_2Br$
- (3)  $A = CH_2 = CH CH_2OH$ 
  - $B = CH_3CH_2CH_2OH$
  - $C = CH_3CH_2CH_2Br$
- (4) A = Cyclopropanol
  - B = Cyclopropenone
  - C = Bromo propane

Answer (1)

Sol.

$$CH_{3}COCH_{3} \xrightarrow{H_{2}/Pd} CH_{3}CH(OH)CH_{3} \xrightarrow{HBr} CH_{3}-CH-CH_{3}$$
(A)
(B)
$$Br \downarrow_{Mg/Ether}$$
(CH.) CHMgPr

(CH<sub>2</sub>)<sub>2</sub>CHMgBr

#### Answer (3)





















$$CH_{3}-COCH_{3} + (CH_{3})_{2}CHMgBr \longrightarrow CH_{3}-C-CH(CH_{3})_{2} \longrightarrow H^{+}$$

$$CH_{3}-C-CH(CH_{3})_{2} \longrightarrow H^{+}$$

$$CH_{3}-C-CH(CH_{3})_{2} \longrightarrow H^{+}$$

$$CH_{3}-C-CH(CH_{3})_{2} \longrightarrow H^{+}$$

- 16. The activation energy of forward reaction and backward reaction is 100 kJ/mole and 180 kJ/mole respectively. Find the correct statement if catalyst is added under same condition of temperature.
  - (1) Catalyst does not change  $\Delta G$  of reaction
  - (2) Catalyst can make non-spontaneous reaction spontaneous
  - (3) Catalyst changes  $\Delta H$  of reaction
  - (4) Enthalpy of reaction (ΔH) is 280 kJ/mole

#### Answer (1)

Sol. Catalyst does not change  $\Delta H$  of reaction. It only alters activation energy.

Catalyst cannot make non-spontaneous reaction spontaneous

$$\Delta H = (E_a)_f - (E_a)_b$$
  
= (100 – 180) kJ/mol

- = -80 kJ/mol
- 17. KMnO<sub>4</sub> oxidises others in acidic medium, Difference between two oxidation states of Mn is x. Neutral FeCl<sub>3</sub> reacts with oxalate ion to form a complex compound having y number of d-electrons. Find x + y.
  - (1) 5
  - (2) 10

- (3) 6
- (4) 8

#### Answer (2)

**Sol.** When KMnO<sub>4</sub> oxidises others in acidic medium difference between the two oxidation states of Mn is 5.

$$KMnO_4 \rightarrow Mn^{2+}$$

$$FeCl_3 + C_2O_4^{2-} \rightarrow [Fe(C_2O_4)_3]^{3-}$$

Fe is in +3 oxidation state.

 $[Fe(C_2O_4)_3]^{3-} \Rightarrow Coloured complex$ 

 $Fe^{3+} \Rightarrow d^5 \Rightarrow 5$  electrons are present in d-orbital

18.

19

20.

#### **SECTION - B**

**Numerical Value Type Questions:** This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. In the following, the number of molecules which are paramagnetic are :

O<sub>2</sub>, N<sub>2</sub>, F<sub>2</sub>, B<sub>2</sub>, Cl<sub>2</sub>

Answer (2)

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O<sub>2</sub> - Paramgnetic

N<sub>2</sub> - Diamagnetic

F<sub>2</sub> - Diamagnetic

According to Molecular

B<sub>2</sub> - Paramagnetic

Cl<sub>2</sub> - Diamagnetic

orbital theory

Species having unpaired electrons are paramagnetic.

22. 0.01 M HX ( $K_a = 4 \times 10^{-10}$ ) is diluted till the solution has pH = 6. If the new concentration is  $x \times 10^{-4}$  M then find х.

#### Answer (25)

**Sol.** 
$$H^+ = \sqrt{K_a \times C}$$

$$10^{-6} = \sqrt{4 \times 10^{-10} \times C}$$

$$10^{-12} = 4 \times 10^{-10} \times C$$

$$C = \frac{1}{4} \times 10^{-2} = 0.25 \times 10^{-2} = 25 \times 10^{-4}$$

23. In Dumas method for estimation of N, 0.5 g of an organic compound gave 150 mL of N2 collected at 300 K and 900 mmHg pressure (Aq tension is 15 mm Hg).

Find % of N

#### Answer (40)

**Sol.** Pressure of  $N_2 = 875$  mm

$$V_{N_2}$$
 at STP =  $\frac{273 \times 885 \times 150}{300 \times 760}$ 

= 158.95 ML

Mass of 
$$N_2 = \frac{158.95}{22400} \times 28$$

≈ 0.2g

% of N = 
$$\frac{0.2}{0.5} \times 100 = 40\%$$

Given below is a sample of DNA strand

5' GGCAATGCTACAG 3"

Find the number of hydrogen bonds present in this DNA strand.

#### Answer (33)

- **Sol.** In DNA, pairing of complementary bases are A = T and
  - Given strand:

'5 G G C A A T G C T A C A G 3"

111 111 111 11 11 11 111 111 11 11 111 11

CCGTTACGATGTC

Total number of hydrogen bonds = 33

25. A sample of 150 kg wheat contains Fe-metal. Find mass of FeSO<sub>4</sub>·7H<sub>2</sub>O in g. so that sample contains 12 ppm Femetal. (Atomic mass of Fe = 55.85 g/mol)

Answer (9)

**Sol.** 
$$12 = \frac{x}{150} \times 10^6$$

$$x = 12 \times 150 \times 10^{-6} = 1800 \times 10^{-6} = 1.8 \times 10^{-3} \text{ kg}$$

55.85 g Fe in 278.02 g FeSO<sub>4</sub>·7H<sub>2</sub>O

$$1.8\times 10^{-3} \text{ kg Fe} \rightarrow \frac{278.02}{55.85}\times 1.8\times 10^{-3} \text{ kg of FeSO}_4.7 \text{H}_2\text{O}$$

$$= 8.96 \times 10^{-3} \text{ kg}$$

 $\cong 9g$ 

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#### **MATHEMATICS**

#### **SECTION - A**

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

#### Choose the correct answer:

- 1. Solve  $\int_{-1}^{1} \frac{1+2x}{e^{-x}+e^{x}} dx$ 
  - (1)  $2\left(\tan^{-1}e \frac{\pi}{4}\right)$  (2)  $2\left(\tan^{-1}e \frac{\pi}{3}\right)$
  - (3)  $2\left(\tan^{-1}e \frac{\pi}{2}\right)$  (4)  $2\left(\frac{\pi}{2} \tan^{-1}e\right)$

#### Answer (1)

**Sol.** 
$$I = \int_{-1}^{1} \frac{1+2x}{a^x + a^{-x}} dx$$

$$I = \int_0^1 \frac{(1+2x) + (1-2x)}{e^x + e^{-x}} dx$$

$$=\int_0^1\frac{2e^x}{e^{2x}+1}dx$$

Let  $e^x = t$ 

$$=\int_1^e \frac{2dt}{t^2+1}$$

 $=2[\tan^{-1}t]^e$ 

$$=2\left(\tan^{-1}e-\frac{\pi}{4}\right)$$

Prop.  $\int_{-a}^{a} f(x)dx = \int_{0}^{a} (f(x) + f(-x))dx$ 

- The sum of the series  $1 + 3 + 5^2 + 7 + 9^2 + \dots$  upto 80 terms is
  - (1) 328160
  - (2) 338160
  - (3) 339400
  - (4) 326870

#### Answer (2)

- **Sol.**  $1+3+5^2+7+9^2+...$  $= (1^2 + 5^2 + 9^2 + ...) + (3 + 7 + 11 + ...)$  $= \left(\sum_{k=0}^{40} (4k-3)^2\right) + \frac{40}{2} (6 + (40-1)4)$  $= 16\sum_{k=0}^{40} k^2 + 9 \times 40 - 24\sum_{k=0}^{40} k + 3240$ 
  - $= 16 \left( \frac{40 \times 41 \times 81}{6} \right) + 360 24 \left( \frac{40 \times 41}{2} \right) + 3240$
  - = 354240 + 360 19680 + 3240 = 338160
- Let there be two A.P.'s with each having 2025 terms. Find the number of distinct terms in union of these two A.P.'s, i.e.,  $A \cup B$  if first A.P. is 1, 6, 11, ... and second A.P. is 9, 16, 23, ...
  - (1) 3761
- (2) 4035
- (3) 3022
- (4) 2025

#### Answer (1)

- **Sol.** 1<sup>st</sup> A.P. : 1, 6, 11...
- 2<sup>nd</sup> A.P.: 9, 16, 23...

Let's find when they are equal for the first time:

$$5n - 4 = 2 + 7m$$

- $\Rightarrow$  5n 7m = 6
- $\Rightarrow$  n = 4, m = 2
- $\Rightarrow$  16 is the first term, common difference will be

LCM  $(d_1, d_2) = LCM (5, 7) = 35$ 

⇒ Common terms will be 16, 51, 86 ...

The last term of 1st A.P.

- $= T_{2025} = 5 \times 2025 4 = 10121$
- ⇒ Common term must be less than that
- $\Rightarrow$  35n 19

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- $\Rightarrow$  35n 19  $\leq$  10121  $\Rightarrow$  35n  $\leq$  10140
  - $\Rightarrow n < 289.7$
  - $\Rightarrow n = 289$
- $\Rightarrow$  in  $n(A \cup B) = n(A) + n(B) n(A \cap B)$ 
  - = 2025 + 2025 289
  - = 3761
- Consider a committee of 12 members is formed randomly out of 4 Engineers, 2 Doctors and 10 Professors. Find the probability that the committee has exactly 3 Engineers and 1 Doctor.
  - (1) 91

- (3)

#### Answer (2)

**Sol.** 
$$P(3E,1D) = \frac{4_{C_3} \cdot 2_{C_1} \cdot 10_{C_8}}{16_{C_{12}}}$$

$$=\frac{4\times2\times\frac{10\times9}{2}}{\frac{16\times15\times14\times13}{24}}=\frac{360\times24}{13\times7\times30\times16}$$

$$=\frac{18}{91}$$

Explanation: 3 Engineers, 1 Doctors and remaining from Professors.

- The number of integral values of  $n \in N$  for which the equation  $x^2 + 4x - n = 0$ ,  $n \in [20,100]$  have integral roots, is
  - (1) 4

(2) 5

(3) 6

(4) 7

#### Answer (3)

**Sol.** 
$$(x+2)^2 = n+4 \Rightarrow x = -2 \pm \sqrt{n+4}$$

$$\therefore$$
 20 \le n \le 100 \Rightarrow 24 \le n + 4 \le 104

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$$\Rightarrow \sqrt{24} \le \sqrt{n+4} \le \sqrt{104}$$

$$\sqrt{n+4} \in \{5, 6, 7, 8, 9, 10\}$$

- $\Rightarrow$  For integral values of x,
- $\Rightarrow$  n = {5<sup>2</sup> 4, 6<sup>2</sup> 4, 7<sup>2</sup> 4, 8<sup>2</sup> 4, 9<sup>2</sup> 4, 10<sup>2</sup> 4}
- $\Rightarrow$  There are six integral values of n.
- If  $10\sin^4\theta + 15\cos^4\theta = 6$ , then find the value of 6.

$$\frac{27\cos e^{6}\theta + 8\sec^{6}\theta}{8\sec^{8}\theta}$$

(1)

(3)

#### Answer (1)

- **Sol.**  $10(\sin^4\theta + \cos^4\theta) + 5\cos^4\theta = 6$ 
  - $\Rightarrow$  10[1 2sin<sup>2</sup> $\theta$ cos<sup>2</sup> $\theta$ ] + 5cos<sup>4</sup> $\theta$  = 6
  - $\Rightarrow$  25cos<sup>4</sup> $\theta$  20cos<sup>2</sup> $\theta$  + 4 = 0
  - $\Rightarrow (5\cos^2\theta 2)^2 = 0$

  - $\Rightarrow$   $\sin^2 \theta = \frac{3}{5}$  and  $\sec^2 \theta = \frac{5}{2}$ ,  $\cos ec^2 \theta = \frac{5}{3}$

$$\Rightarrow \frac{27 \operatorname{cosec}^{6} \theta + 8 \sec^{6} \theta}{8 \sec^{8} \theta} = \frac{27 \cdot \left(\frac{5}{3}\right)^{3} + 8 \cdot \left(\frac{5}{2}\right)^{3}}{8 \cdot \left(\frac{5}{4}\right)^{4}} = \frac{4}{5}$$

- Find the length of latus rectum of an ellipse if foci are 7. (2, 5) and (2, -3) and the eccentricity of the ellipse is  $\frac{4}{5}$

Answer (3)

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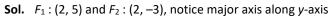












$$\Rightarrow F_1F_2 = 8 = 2be \Rightarrow b = \frac{8}{2e} = \frac{4}{4/5} = 5$$

$$\Rightarrow e^2 = 1 - \frac{a^2}{h^2} = 1 - \frac{a^2}{25} = \frac{16}{25}$$

$$\Rightarrow a^2 = 9 \Rightarrow a = 3$$

The length of latus rectum :  $\frac{2a^2}{h} = \frac{2(9)}{r} = \frac{18}{r}$ 

8. If 
$$\lim_{x\to 1^+} \frac{(x-1)[6+\lambda\cos(x-1)]+\mu\sin(x-1)}{(x-1)^3} = -1$$
.

Then the value of  $\lambda + \mu$  is

- (1) -6
- (2) -4
- (3) 4
- (4) 2

#### Answer (1)

Sol. 
$$\lim_{x \to 1^{+}} \frac{(x-1)[6+\lambda\cos(x-1)] + \mu\sin(x-1)}{(x-1)^{3}} = -1$$

$$\lim_{x \to 1^{+}} \frac{(x-1)\left[6+\lambda\cos\left(1-\frac{(x-1)^{2}}{2!} + \frac{(x-1)^{4}}{4!}\right)\right] + \mu\left((x-1) - \frac{(x-1)^{3}}{3!} + \dots\right)}{(x-1)^{3}}$$

$$\lim_{t \to 1^+} \frac{(x-1)(6+\lambda) - \frac{\lambda(x-1)^3}{2!} + \dots + \mu(x-1) - \mu \frac{(x-1)^3}{3!} + \dots}{(x-1)^3}$$

For limit to exist

$$6+\lambda+\mu=0$$

$$\Rightarrow \lambda + \mu = -6$$

- Let  $\alpha$  and  $\beta$  be the number of points where the function.  $f(x) = \max\{x, x^3, x^5, \dots x^{21}\}$  is not conations and not differentiable respectively, then  $\alpha + \beta$  equals to
  - (1) 6

(2) 3

(3) 2

(4) 4

#### Answer (2)

**Sol.** For 
$$x \ge 1$$
,  $x^{21} \ge x^{19} \ge .... \ge x$ 

$$\Rightarrow f(x) = \begin{cases} x & x < -1 \\ x^{21} & -1 \le x \le 0 \\ x & 0 < x < 1 \\ x^{21} & x \ge 1 \end{cases}$$

Closely, f(x) is continuous everywhere  $\Rightarrow \alpha = 0$ 

$$f'(x) = \begin{cases} 1 & , & x < -1 \\ 20x^{20} & , & -1 \le x \le 0 \\ 1 & , & 0 < x < 1 \\ 21x^{20} & , & x \ge 1 \end{cases}$$

$$\Rightarrow \beta = 3$$

$$\Rightarrow \alpha + \beta = 3$$

- 10. If  $f(x) = 1 2x + \int_{0}^{x} e^{x-t} f(t) dt$ , then the area bounded by the curve y = f(x) and coordinate axes is (in square units)

**Sol.** 
$$\therefore f(x) = 1 - 2x + \int_0^x e^{x-t} f(t) dt$$

or, 
$$f(x) = 1 - 2x + e^x \int_0^x e^{-t} f(t) dt$$

on differentiating both sides w.r.t. x we get

$$f'(x) = -2 + e^{x} \int_{0}^{x} e^{-t} f(t) dt + e^{x} \cdot e^{-x} f(x)$$

$$f'(x) = -2 + f(x) + 2x - 1 + f(x)$$
 {from eq. (1)}

$$f'(x) - 2f(x) = 2x - 3$$

I.F. = 
$$e^{\int -2dx} = e^{-2x}$$

$$\therefore e^{-2x} \cdot f(x) = \int e^{-2x} (2x - 3) dx$$

$$e^{-2x} \cdot f(x) = (2x-3) \cdot \frac{e^{-2x}}{-2} - \int 2 \cdot \frac{e^{-2x}}{-2} dx$$

$$e^{-2x} \cdot f(x) = \frac{(2x-3)e^{-2x}}{-20} + \frac{e^{-2x}}{-2} + c$$

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$$f(x) = -x + 1 + c'e^{2x}$$

$$f(x) = 1$$
 from eq. (1)

$$\therefore 1 = 0 + 1 + c' \Rightarrow c' = 0$$

$$f(x) = -x + 1$$

$$\Rightarrow$$
 Area =  $\frac{1}{2}$ 

11. The value of  $\sin^{-1}\left(\frac{\sqrt{3}x}{2} + \frac{1}{2}\sqrt{1-x^2}\right), -\frac{1}{2} < x < \frac{1}{\sqrt{2}}$  is equivalent to

(1) 
$$\frac{2\pi}{3} - \cos^{-1} x$$
,  $-\frac{1}{2} < x < \frac{1}{\sqrt{2}}$ 

(2) 
$$\pi - \cos^{-1} x$$
,  $-\frac{1}{2} < x < \frac{1}{\sqrt{2}}$ 

(3) 
$$\frac{\pi}{3} - \cos^{-1} x, -\frac{1}{2} < x < \frac{1}{\sqrt{2}}$$

(4) 
$$\frac{\pi}{2} - \sin^{-1} x, -\frac{1}{2} < x < \frac{1}{\sqrt{2}}$$

#### Answer (1)

**Sol.** 
$$\sin^{-1}\left(\frac{\sqrt{3}x}{2} + \frac{1}{2}\sqrt{1 - x^2}\right), -\frac{1}{2} < x < \frac{1}{\sqrt{2}}$$

Let 
$$x = \cos\theta$$
,  $\theta \in \left(-\frac{1}{2}, \frac{1}{\sqrt{2}}\right)$ 

$$\Rightarrow \sqrt{1-x^2} = \sin\theta$$
, as  $\sin\theta > 0$ 

$$\sin^{-1}\left(\frac{\sqrt{3}}{2}\cos\theta + \frac{1}{2}\sin\theta\right) = \sin^{-1}\left(\sin\frac{\pi}{3}\cos\theta + \cos\frac{\pi}{3}\cos\theta\right)$$

$$=\sin^{-1}\left(\sin\left(\frac{\pi}{3}+\theta\right)\right)$$

Since 
$$\frac{\pi}{3} + \theta \in \left(\frac{7\pi}{12}, \pi\right)$$

$$\Rightarrow \sin\left(\frac{\pi}{3} + \theta\right) = \sin\left(\pi - \left(\frac{\pi}{3} + \theta\right)\right) = \sin\left(\frac{2\pi}{3} - \theta\right)$$

$$\Rightarrow \sin^{-1}\!\left(\sin\!\left(\frac{\pi}{3}\!+\!\theta\right)\right)\!=\!\sin^{-1}\!\left(\sin\!\left(\frac{2\pi}{3}\!-\!\theta\right)\right)$$

Since 
$$\frac{2\pi}{3} - \theta \in \left(0, \frac{5\pi}{12}\right)$$

$$\Rightarrow = \frac{2\pi}{3} - \theta$$

$$=\frac{2\pi}{3}-\cos^{-1}x, x \in \left(-\frac{1}{2}, \frac{1}{\sqrt{2}}\right)$$

- There are 10 pens such that 3 pens are defective. Let X represent the number of defective pen selected. If two pens are selected at random then variance of X is

#### Answer (2)

Sol.

X	P(X)	XP(X)	$(X_i - \mu)^2$	$P_iX(X_i-\mu)^2$
<i>X</i> = 0	$\frac{{}^{7}C_{2}}{{}^{10}C_{2}}$	0	$\left(0-\frac{3}{5}\right)^2$	$\frac{7}{15} \left( \frac{9}{25} \right)$
X = 1	$\frac{{}^{7}C_{1} {}^{3}C_{1}}{{}^{10}C_{2}}$	7 15	$\left(1-\frac{3}{5}\right)^2$	$\frac{7}{15} \left(\frac{4}{25}\right)$
X = 2	$\frac{{}^{7}C_{0}{}^{3}C_{2}}{{}^{10}C_{2}}$	2 15	$\left(2-\frac{3}{5}\right)^2$	$\frac{1}{15} \left( \frac{49}{25} \right)$

$$\mu = \sum X_i P(X_i) = 0 + \frac{7}{15} + \frac{2}{15} = \frac{3}{5}$$

Variance (X) =

$$\sum P_i(X_i - \mu)^2 = \frac{7}{15} \left(\frac{9}{25}\right) + \frac{7}{15} \left(\frac{4}{25}\right) + \frac{1}{15} \left(\frac{49}{25}\right) = \frac{28}{75}$$

- 13.
- 14.
- 15.
- 16.
- 17.
- 18.
- 19.
- 20.

#### THE LEGACY OF SUCCESS CONTINUES

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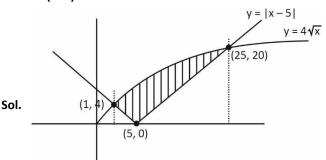


#### **SECTION - B**

Numerical Value Type Questions: This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. Let  $|x-5| \le y \le 4\sqrt{x}$ . If the Area enclosed is A, then 3A

#### **Answer (368)**



$$A = \int_{1}^{25} 4\sqrt{x} dx - \frac{1}{2} \times 4 \times 4 - \frac{1}{2} \times 20 \times 20$$

$$A = \begin{bmatrix} \frac{3}{4x^{\frac{3}{2}}} \\ \frac{3}{2} \end{bmatrix}_{1}^{25} - 8 - 200$$

$$A = \frac{8}{3}[125 - 1] - 208$$

$$=\frac{368}{3} \Rightarrow 3A = 368$$

22. Given two lines

$$L_1: \frac{x-3}{3} = \frac{y-\alpha}{1} = \frac{z+2}{-2}$$

and 
$$L_2: \frac{x+1}{2} = \frac{y+2}{1} = \frac{z-\beta}{-1}$$

If shortest distance between  $L_1$  and  $L_2$  is  $30\sqrt{3}$ . Then the value of |a + b| is

#### Answer (90)

**Sol.** 
$$L_1: \frac{x-3}{3} = \frac{y-\alpha}{1} = \frac{z+2}{-2}$$

$$L_2: \frac{x+1}{2} = \frac{y+2}{1} = \frac{z-\beta}{-1}$$

## Shortest distance, $d = \frac{\left| (\overrightarrow{a_2} - \overrightarrow{a_1}) \cdot (\overrightarrow{b_1} - \overrightarrow{b_2}) \right|}{\left| (\overrightarrow{b_1} \times \overrightarrow{b_2}) \right|}$

$$\left(\overrightarrow{a_2} - \overrightarrow{a_1}\right) \cdot \left(\overrightarrow{b_1} - \overrightarrow{b_2}\right) = \begin{vmatrix} 4 & \alpha + 2 & -2 - \beta \\ 3 & 1 & -2 \\ 2 & 1 & -1 \end{vmatrix}$$

$$= 4 (-1 + 2) - (\alpha + 2) (-3 + 4)$$

$$-(2 + \beta)(3 - 2)$$

$$= 4 - \alpha - 2 - 2 - \beta$$

$$=-\alpha-6$$

Also 
$$|\overrightarrow{b_1} \times \overrightarrow{b_2}| = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & 1 & -2 \\ 2 & 1 & -1 \end{vmatrix}$$

$$=|\hat{i}-\hat{j}+\hat{k}|$$

$$=\sqrt{3}$$

$$30\sqrt{3} = \frac{\left|-\alpha - \beta\right|}{\sqrt{3}}$$

$$\Rightarrow |\alpha + \beta| = 90$$

23. If  $\vec{v}=2\hat{i}+\hat{j}-\lambda\hat{k}$ ,  $(\lambda>0)$ ,  $\vec{u}=3\hat{i}-\hat{j}$  and  $\vec{v}_1$  is parallel to  $\vec{u}$  ,  $\vec{v}_2$  is perpendicular to  $\vec{u}$  and  $\vec{v} = \vec{v}_1 + \vec{v}_2$  . If angle between  $\vec{v}$  and  $\vec{v}_1$  is  $\cos^1\left(\frac{\sqrt{5}}{2\sqrt{7}}\right)$ , then  $|\vec{v}_1|^2 + |\vec{v}_2|^2$ 

equals to

#### Answer (14)

**Sol.** 
$$\vec{\mathbf{v}} = \vec{\mathbf{v}}_1 + \vec{\mathbf{v}}_2$$

$$\vec{v} \cdot \vec{u} = \vec{v}_1 \cdot \vec{u} + \vec{v}_2 \cdot \vec{u} = (k\vec{u}) \cdot \vec{u} + 0$$

$$6 - 1 + 0 = k(0)$$

$$\begin{vmatrix} \vec{v}_1 \parallel \vec{u} \\ \vec{v}_2 \perp \vec{u} \end{vmatrix}$$

$$\Rightarrow \vec{v}_1 = k\vec{u}$$

$$\begin{bmatrix} \vec{v}_1 \parallel \vec{u} \\ \vec{v}_2 \perp \vec{u} \end{bmatrix}$$

$$\Rightarrow \vec{v}_1 = k\vec{u}$$

$$\Rightarrow k = \frac{1}{2}$$

$$\vec{v}_1 = \frac{1}{3}(3\hat{i} - \hat{j}) = \frac{3}{2}\hat{i} - \frac{\hat{j}}{2}$$

Cosine of angle between  $\vec{v}$  and  $\vec{v}_1$ 

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99.99 Amogh Bansal



$$= \frac{\mathbf{v} \cdot \vec{\mathbf{v}}_1}{|\vec{\mathbf{v}}||\vec{\mathbf{v}}_1|} = \frac{3 - \frac{1}{2} + 0}{\sqrt{\frac{9}{4} + \frac{1}{4}} \sqrt{4 + 1 + \lambda^2}}$$

$$\Rightarrow \frac{\sqrt{5}}{2\sqrt{7}} = \frac{\frac{5}{2}}{\sqrt{\frac{5}{2}}\sqrt{\lambda^2 + 5}}$$

 $\lambda^2 = 9$ ,  $\lambda = 3$ 

$$\Rightarrow \frac{5}{4 \times 7} = \frac{\frac{5}{2}}{(\lambda^2 + 5)} \Rightarrow (\lambda^2 + 5) = 14$$

$$\vec{v}_2 = \vec{v} - \vec{v}_1 = (2\hat{i} + \hat{j} - 3\hat{k}) - \left(\frac{3}{2}\hat{i} - \frac{\hat{j}}{2}\right)$$

$$=\frac{1}{2}\hat{i}+\frac{3}{2}\hat{j}-3\hat{k}$$

$$\left|\vec{v}_1\right|^2 + \left|\vec{v}_2\right|^2 = \left(\frac{9}{4} + \frac{1}{4}\right) + \left(\frac{1}{4} + \frac{9}{4} + 9\right)$$

$$=\frac{10}{4}+\frac{10}{4}+9=14$$

- 24.
- 25.



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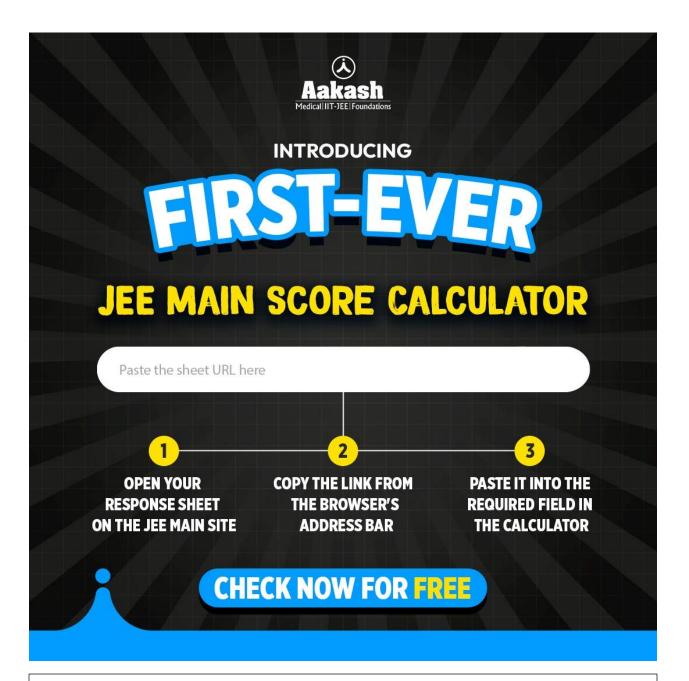


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