

JEE-Main-07-04-2025 (Memory Based)
[EVENING SHIFT]
Maths

Question: If $x|x - 3| + 3|x - 2| + 1 = 0$, then the number of real solutions is

Options:

- (a) 2
- (b) 4
- (c) 1
- (d) 6

Answer: (1)

Question: $\operatorname{Re} \left(\frac{2z + i}{z + i} \right) + \operatorname{Re} \left(\frac{2\bar{z} - i}{\bar{z} - i} \right) = 2$ is a circle of radius r and centre (a, b) ,
 then $\frac{15ab}{r^2}$ is equal to

Answer: (0)

Question: If two vectors \vec{a} and \vec{b} satisfy $\frac{|\vec{a} + \vec{b}| + |\vec{a} - \vec{b}|}{|\vec{a} + \vec{b}| - |\vec{a} - \vec{b}|} = \sqrt{2} + 1$, then the value of $\frac{|\vec{a} + \vec{b}|^2}{|\vec{a} - \vec{b}|^2}$ is equal to

Options:

- (a) $1 + \sqrt{2}$
- (b) $2 + 4\sqrt{2}$
- (c) $1 + 2\sqrt{2}$
- (d) $3 + 2\sqrt{2}$

Answer: (d)

Question: Let $f(x) = \frac{x - 5}{x^2 - 3x + 2}$ is range of $f(x)$ is $(-\infty, \alpha) \cup (\beta, \infty)$. Then $\alpha^2 + \beta^2$ equals to

Answer: (194)

Question: If a box contains 19 unbiased coins and 1 biased coin with both faces head. If a coin is randomly chosen out of this box and tossed. If the head appears, then the probability that the unbiased coin was selected

Options:

- (a) $\frac{19}{21}$
- (b) $\frac{1}{3}$

- (c) $\frac{1}{5}$
 (d) $\frac{1}{6}$

Answer: (a)

Question: If $f(\theta) = \frac{\tan(\tan \theta) - \tan(\sin \theta)}{\tan \theta - \sin \theta}$ is continuous at $\theta = 0$, then the value of $f(\theta)$ at $\theta = 0$ is equal to

Answer: (1)

Question: Let a random variable X take values 0, 1, 2, 3 with $P(x = 0) = P(x = 1) = P(x = 2) = P(x = 3)$ and $E(X^2) = 2E(x)$. Then the value of $8p - 1$ is

Answer: (2)

Question: Let a_n be the n^{th} term of an A.P. If $S_n = a_1 + a_2 + a_3 + \dots + a_n = 700$, $a_6 = 7$ and $S_7 = 7$, then a_n is equal to

Answer: (64)

Question: Let \vec{a} and \vec{b} be the vectors of the same magnitude

such that $\frac{|\vec{a} + \vec{b}| + |\vec{a} - \vec{b}|}{|\vec{a} + \vec{b}| - |\vec{a} - \vec{b}|} = \sqrt{2} + 1$, Then $\frac{|\vec{a} + \vec{b}|^2}{|\vec{a} - \vec{b}|^2}$ is

Answer: $2(1 + \cos \theta)$

Question: Let $y = y(x)$ and $(1 + x^2) y' - 2xy = (x^4 + 2x^2 + 1) \cos x$. If

$y(0) = 1$, then $\int_{-3}^3 y(x) dx$ equals to

Options:

- (a) 20
 (b) 15
 (c) 24
 (d) 10

Answer: (c)

Question: Let the length of a latus rectum of an ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ be 10. If its eccentricity is the minimum value of the function $f(t) = t^2 + t + \frac{11}{12}$, $t \in \mathbb{R}$, then $a^2 + b^2$ is equal to

Answer: (126)

Question: If a triangle is formed using lines $y = x + 1$, $y = 4x - 8$, $y = mx + c$. If the orthocentre of this triangle is $(3, -1)$, then $m - c$ is equal to

Options:

- (a) 0
 (b) 1
 (c) -1
 (d) 2

Answer: (a)

Question: Let the foot of perpendicular from $P(5, 1, -3)$ on the line $L_1 : x - 1 = y - 2 = z$ and $L_2 : x - 2 = y = z - 1$ is Q and R , respectively. The area of triangle PQR is equal to (in square units)

Options:

- (a) $\frac{7}{2}$
- (b) $\frac{7}{\sqrt{2}}$
- (c) $\frac{7\sqrt{3}}{2}$
- (d) 7

Answer: (c)

