

General instructions :

The question paper is divided into FOUR sections.

(1)	Section A :	Q.1 contains Eight multiple choice type
		questions carrying Two marks each.
		Q. 2 contains Four very short answer type
		questions carrying One mark each.
(2)	Section B :	This section contains Twelve short answer type questions carrying Two marks each.
		(Attempt any Eight)
(3)	Section C :	This section contains Twelve short answer type
		questions carrying Three marks each.
		(Attempt any Eight)
(4)	Section D :	This section contains Eight long answer type
		questions carrying Four marks each.
		(Attempt any Five)

- (5) Use of log table is allowed. Use of calculator is not allowed.
- (6) Figures to the right indicate full marks.

0 3 1 2

- (7) Use of graph paper is <u>not</u> necessary. Only rough sketch of graph is expected.
- (8) For each multiple choice type of questions, only the first attempt will be considered for evaluation.
- (9) Start answer to each section on a new page.

SECTION – A

Q. 1. Select and write the correct answer of the following [16] multiple choice type of questions :

- (i) If $A = \{1, 2, 3, 4, 5\}$ then which of the following is not true?
 - (a) $\exists x \in A$ such that x + 3 = 8
 - (b) $\exists x \in A \text{ such that } x + 2 < 9$
 - (c) $\forall x \in A, x+6 \ge 9$
 - (d) $\exists x \in A$ such that x + 6 < 10 (2)

(ii) In $\triangle ABC$, $(a + b) \cdot \cos C + (b + c) \cos A + (c + a) \cdot \cos B$ is equal to _____. (a) a - b + c

- (b) a + b c
- (c) a + b + c
- $(d) \quad a-b-c \tag{2}$

(iii) If $|\overline{a}| = 5$, $|\overline{b}| = 13$ and $|\overline{a} \times \overline{b}| = 25$ then $|\overline{a} \cdot \overline{b}|$ is equal to

- (a) 30 (b) 60
- (c) 40 (d) 45 (2)

2 3 1 0

0 3 1 2

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Q. 2. Answer the following questions :

(i) Write the negation of the statement : $\exists n \in N$ such that n+8>11' (1)

(ii) Write unit vector in the opposite direction to

$$\overline{u} = 8\hat{i} + 3\hat{j} - \hat{k}.$$
 (1)

(iii) Write the order of the differential equation

$$\sqrt{1 + \left(\frac{dy}{dx}\right)^2} = \left(\frac{d^2y}{dx^2}\right)^{\frac{3}{2}}$$
(1)

(iv) Write the condition for the function f(x), to be strictly increasing, for all $x \in R$. (1)

SECTION – B

Attempt any EIGHT of the following questions :

0 3 1 2

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[4]

[16]

Q.8. Find the vector equation of the plane passing through the point having position vector $2\hat{i}+3\hat{j}+4\hat{k}$ and perpendicular to the vector $2\hat{i}+\hat{j}-2\hat{k}$. (2)

Q.9. Divide the number 20 into two parts such that sum of their squares is minimum. (2)

Q. 10. Evaluate:
$$\int x^9 \sec^2(x^{10}) dx$$
 (2)

Q. 11. Evaluate :
$$\int \frac{1}{25 - 9x^2} dx$$
 (2)

Q. 12. Evaluate :
$$\int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \frac{1}{1-\sin x} dx$$
 (2)

- Q. 13. Find the area of the region bounded by the parabola $y^2 = 16x$ and its latus rectum. (2)
- Q. 14. Suppose that X is waiting time in minutes for a bus and its p.d.f. is given by :

$$f(x) = \frac{1}{5}, \text{ for } 0 \le x \le 5$$

= 0, otherwise.

Find the probability that :

- (i) waiting time is between 1 to 3 minutes.
- (ii) waiting time is more than 4 minutes.



(2)

SECTION - C

Attempt any EIGHT of the following questions :

Q. 15. Express the following switching circuit in the symbolic form of logic. Construct the switching table and interpret it :



Q. 16. Prove that: $2\tan^{-1}\left(\frac{1}{3}\right) + \cos^{-1}\left(\frac{3}{5}\right) = \frac{\pi}{2}$. (3)

Q. 17. In $\triangle ABC$ if a = 13, b = 14, c = 15 then find the values of (i) $\sec A$ (ii) $\csc \frac{A}{2}$. (3)

Q . 18.	A line passes through the points $(6, -7, -1)$ and $(2, -3, 1)$. Find the direction ratios and the direction cosines of the line. Show that the line does not pass through the origin.	(3)
Q. 19.	Find the cartesian and vector equations of the line passing through A (1, 2, 3) and having direction ratios 2, 3, 7.	(3)
Q. 20 .	Find the vector equation of the plane passing through points $A(1, 1, 2)$, $B(0, 2, 3)$ and $C(4, 5, 6)$.	(3)
Q . 21.	Find the <i>n</i> th order derivative of <i>log x</i> .	(3)
Q . 22.	The displacement of a particle at time t is given by $s = 2t^3 - 5t^2 + 4t - 3$. Find the velocity and displacement at the	

time when the acceleration is 14 ft/sec^2 .

2 3 1 0

(3)

Q.23. Find the equations of tangent and normal to the curve

$$y = 2x^3 - x^2 + 2 \text{ at point } \left(\frac{1}{2}, 2\right).$$
 (3)

Q. 24. Three coins are tossed simultaneously, X is the number of heads.
 Find the expected value and variance of X. (3)

Q. 25. Solve the differential equation :
$$x \frac{dy}{dx} = x \tan\left(\frac{y}{x}\right) + y$$
. (3)

- **Q. 26.** Five cards are drawn successively with replacement from a wellshuffled deck of 52 cards. Find the probability that :
 - (i) all the five cards are spades.
 - (ii) none is spade. (3)

SECTION – D

Q. 27. Find the inverse of
$$\begin{bmatrix} \cos\theta & -\sin\theta & 0\\ \sin\theta & \cos\theta & 0\\ 0 & 0 & 1 \end{bmatrix}$$
 by elementary row

transformations. https://www.maharashtrastudy.com (4)

- Q. 28. Prove that homogeneous equation of degree two in x and y, $ax^2 + 2hxy + by^2 = 0$ represents a pair of lines passing through the origin if $h^2 - ab \ge 0$. Hence show that equation $x^2 + y^2 = 0$ does not represent a pair of lines. (4)
- Q. 29. Let \overline{a} and \overline{b} be non-collinear vectors. If vector \overline{r} is coplanar with \overline{a} and \overline{b} then show that there exist unique scalars t_1 and t_2 such that $\overline{r} = t_1 \overline{a} + t_2 \overline{b}$. For $\overline{r} = 2\hat{i} + 7\hat{j} + 9\hat{k}$, $\overline{a} = \hat{i} + 2\hat{j}$, $\overline{b} = \hat{j} + 3\hat{k}$, find t_1, t_2 . (4)



[00]

Q. 30. Solve the linear programming problem graphically.

Maximize: z = 3x + 5ySubject to: $x + 4y \le 24$, $3x + y \leq 21$ $x + y \leq 9$ $x \ge 0, y \ge 0$

Also find the maximum value of z

If x = f(t) and y = g(t) are differentiable functions of t so that y Q. 31.

a function of x and if
$$\frac{dx}{dt} \neq 0$$

then prove that
$$\frac{dy}{dx} = \frac{\frac{dy}{dt}}{\frac{dx}{dt}}$$
.

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1 Hence find the derivative of 7^x w.r.t. r^7 . (4)

Q. 32. Evaluate:
$$\int e^{\sin^{-1}x} \left(\frac{x + \sqrt{1 - x^2}}{\sqrt{1 - x^2}} \right) dx$$
 (4)

Q.33. Prove that:
$$\int_{a}^{b} f(x)dx = \int_{a}^{b} f(a+b-x)dx$$

Hence evaluate :
$$\int_{0}^{3} \frac{\sqrt{x}}{\sqrt{x} + \sqrt{3 - x}} dx$$
 (4)

If a body cools from 80°C to 50°C at room temperature of 25°C Q. 34. in 30 minutes, find the temperature of the body after 1 hour.

(4)

(4)



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